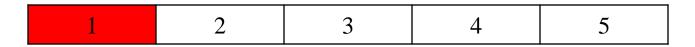
16IT302 – DESIGN AND ANALYSIS OF ALGORITHM

- Pre- Requisite for DAA Algorithm / DS
- What you are going to Study in DAA
 - Recipe for food preparation
 - Algorithms (steps) are instructions for building programs
 - Designing Algorithm
 - Analyzing Algorithm
- Why Designing and Analyzing Algorithm is important.
 - Without a proper blueprint you cannot construct a house
 - Proper design and analyzing of algorithm will give a best solution for a problem
 - Requirement (Algorithm should be designed)

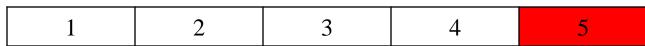
Problem \square how to solve \square steps to solve \square Analyze

Why Designing and Analyzing Algorithm? Example

- Example: searching
- Search 1



• Search 5



- Search technique
 - Google 500-600 times each year search algorithm is changed
 - MS Word Boyer Moore algorithm

*

Binary Search



SYLLABUS

UNIT I INTRODUCTION	9+6			
Notion of an Algorithm - Fundamentals of Algorithmic Problem Solving - Important Problem Types -				
Fundamentals of the Analysis of Algorithm Efficiency – Analysis Framework – Asymptotic No.	otations and its			
properties – Mathematical analysis for Recursive and Nonrecursive algorithms.				
UNIT II BRUTE FORCE AND DIVIDE-AND-CONQUER	9+6			
Brute Force: Insertion Sort, Bubble Sort, Sequential Search, Closest-Pair and Convex-Fi	Iull Problems-			
Traveling Salesman Problem - Knapsack Problem - Assignment problem. Divide and conquer	methodology:			
Merge sort – Quick sort – Binary search – Multiplication of Large Integers – Strassen's Matrix M	Multiplication			
UNIT III DYNAMIC PROGRAMMING AND GREEDY TECHNIQUE	9+6			
Dynamic Programming: Computing a Binomial Coefficient – Warshall's and Floyd's algorit	hm – Optimal			
Binary Search Trees – Knapsack Problem and Memory functions. Greedy Technique Prim's algorithm-				
Kruskal's Algorithm - Dijkstra's Algorithm-Huffman Trees – Job Sequence Scheduling				
UNIT IV ITERATIVE IMPROVEMENT	9+6			
The Simplex Method-The Maximum-Flow Problem – Maximum Matching in Bipartite Graphs- The Stable				
marriage Problem.				
UNIT V COPING WITH THE LIMITATIONS OF ALGORITHM	9+6			
Limitations of Algorithm - Lower-Bound Arguments-Decision Trees-P, NP and NP-Complete Problems -				
Coping with the Limitations – Backtracking: n-Queens problem – Hamiltonian Circuit Problem – Subset Sum				
Problem-Branch and Bound: Assignment problem - Knapsack Problem - Traveling Salesman Problem-				
Approximation Algorithms for NP Hard Problems				
TEXT BOOKS				
Anany Levitin, "Introduction to the Design and Analysis of Algorithms", Pearson Education, 3rd				
Edition, 2012. (Unit I,II,III,IV,V)				

UNIT I – NOTION OF ALGORITHM

Algorithm

- unambiguous instructions to solve a problem
- Solution to a problem / procedure for getting that solution
- Different forms
- Single problem multiple solutions multiple algorithms requirements
- instructions computers / human beings
- Example:

greatest common divisor of 2 numbers (GCD) -3 methods

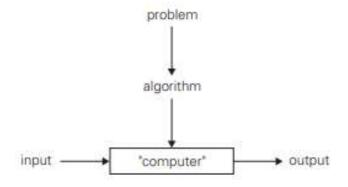


Fig: Notion of Algorithm

UNIT I – NOTION OF ALGORITHM GCD of two numbers – Euclid's Algorithm

- GCD of two numbers
 - Euclid's algorithm
 - Consecutive integer checking algorithm
 - Middle school procedure
 - Euclid's algorithm

```
gcd(m,n) = gcd(n, m \mod n)

Example 1: gcd(60,24) = gcd(24, 60 \mod 24)

= gcd(24, 12)

= gcd(12, 24 \mod 12)

= gcd(12,0)

Example 2: gcd(70, 35)

Example 3: gcd(30,14) = gcd(n, m \mod n)

= gcd(14, 30 \mod 14)

= gcd(?)
```

Euclids Algorithm

Iteration	m	n	r = m % n
1	50	35	15
2	35	15	-5
3	15	5	0
4	5 (GCD)	0 (Stop)	

UNIT I – NOTION OF ALGORITHM GCD of two numbers – Euclid's Algorithm

Euclid's algorithm for computing gcd(m, n)

- **Step 1** If n = 0, return the value of m as the answer and stop; otherwise, proceed to Step 2.
- **Step 2** Divide m by n and assign the value of the remainder to r.
- **Step 3** Assign the value of n to m and the value of r to n. Go to Step 1.

Alternatively, we can express the same algorithm in pseudocode:

```
ALGORITHM Euclid(m, n)

//Computes gcd(m, n) by Euclid's algorithm

//Input: Two nonnegative, not-both-zero integers m and n

//Output: Greatest common divisor of m and n

while n ≠ 0 do

r ← m mod n

m ← n

n ← r

return m
```

UNIT I – NOTION OF ALGORITHM GCD of two numbers – Consecutive Integer Checking Algorithm

• GCD – common divisor cannot be greater than the smaller of these numbers $t = min \{m, n\}$

•	gcd	(60,24)	\Box	$24 \square$	de	crease	e 24 by
	$1 \square$	23 □	$22\square$	• • • • • •		12	

m	n	t
60	24	24
60	24	23
60	24	22
60	24	21
60	24	20
60	24	19
60	24	18

m	n	t
60	24	17
60	24	16
60	24	15
60	24	14
60	24	13
60	24	12

Consecutive Integer Checking Algorithm

- Step 1 Assign the value of min(m, n) to t.
- Step 2 Divide m by t. If the remainder of this division is 0, go to Step 3; otherwise, go to Step 4.
- Step 3 Divide n by t. If the remainder of this division is 0, return the value of t as the answer and stop; otherwise, proceed to Step 4.
- Step 4 Decrease the value of t by 1. Go to Step 2.

UNIT I – NOTION OF ALGORITHM GCD of two numbers – Middle School procedure

- Step 1 Find the prime factors of m.
- **Step 2** Find the prime factors of n.
- Step 3 Identify all the common factors in the two prime expansions found in Step 1 and Step 2. (If p is a common factor occurring p_m and p_n times in m and n, respectively, it should be repeated min{p_m, p_n} times.)
- Step 4 Compute the product of all the common factors and return it as the greatest common divisor of the numbers given.

Thus, for the numbers 60 and 24, we get

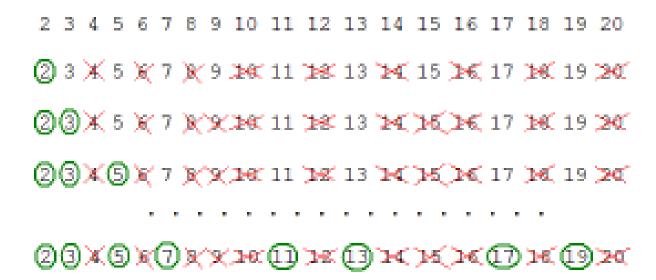
$$60 = 2 \cdot 2 \cdot 3 \cdot 5$$

 $24 = 2 \cdot 2 \cdot 2 \cdot 3$
 $\gcd(60, 24) = 2 \cdot 2 \cdot 3 = 12$. $\gcd(60, 24) = 2 \cdot 2 \cdot 3 = 12$.

- Middle school procedure Sieve of Eratosthenes
- Euclid's Algorithm is Simpler and fast

UNIT I – NOTION OF ALGORITHM GCD of two numbers – Middle School procedure

• Sieve of Eratosthenes – prime factors



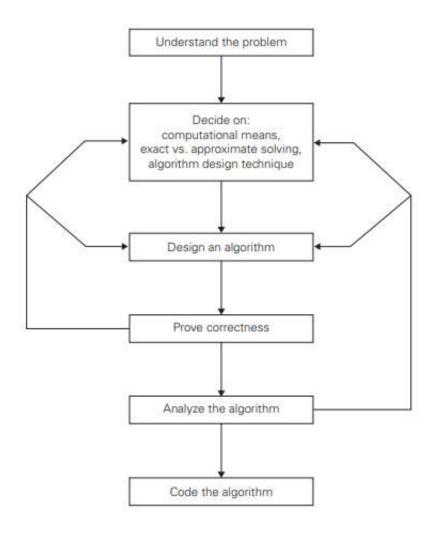


Fig: Algorithm Design and Analysis Process

- Understanding the problem
 - What, doubts, examples, use cases
 - − Inputs − *instance of the problem*
- Ascertaining the capabilities of a computational device
 - Random Access Machine Sequential Algorithm
 - Instructions concurrent Parallel algorithm
 - Speed and memory of computer system Depends on Application type
- Choosing between exact and approximate problem solving
 - Exact algorithm
 - Approximation algorithm
- Deciding on Appropriate data structures
 - Data Structure representing the data

- Algorithm design techniques
 - Methods/ process to solve a problem
 - Example : Linear (Linear programming)

VS

Binary serach (Divide and Conquer programming)

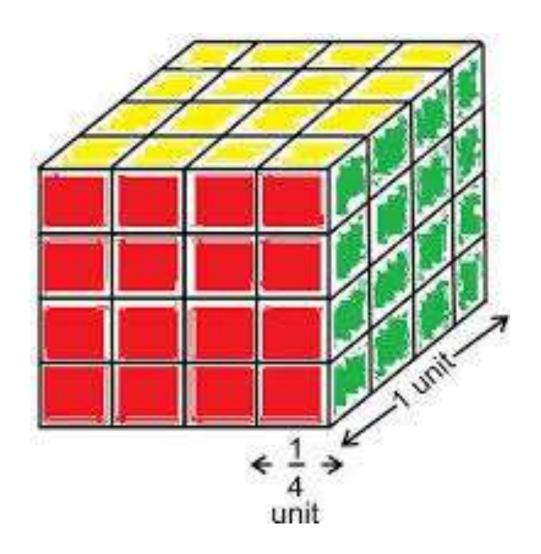
- Methods to specifying an algorithm
 - Natural language
 - Pseudo code (Natural language + programming constructs)
 - Flowchart

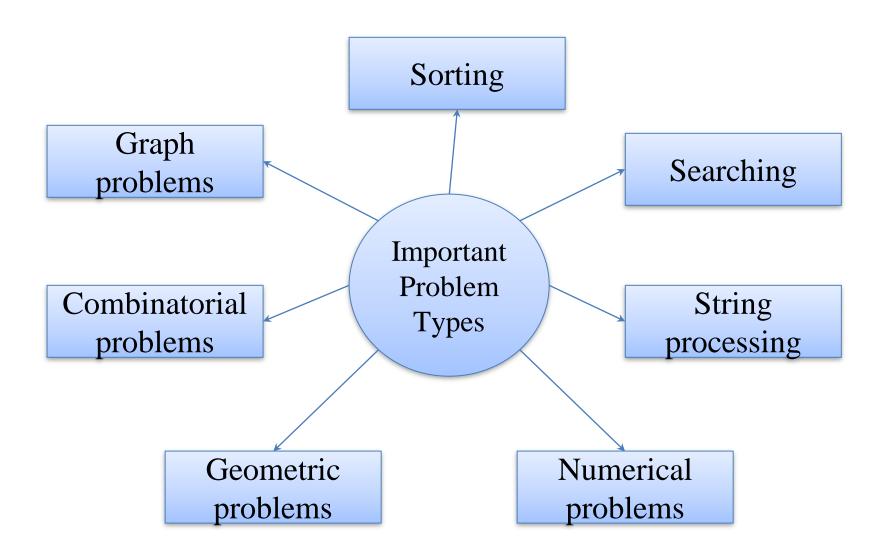
- Proving an algorithm's correctness
 - Correctness GCD (Euclids algorithm) □ n value decreases and last reaches 0
 - Complex mathematical induction (iteration)
 - Algorithm incorrect 1 instance
- Analyzing an algorithm
 - Time efficiency
 - Space efficiency
 - Simplicity easier to understand and program
 - Generality
- Coding an algorithm

A cube painted red in two adjacent sides and opposite to red it is painted green. The remaining sides painted black.

This cube is divided into 64 equal sized smaller cubes.

How many smaller cubes will be there with no sides colored?





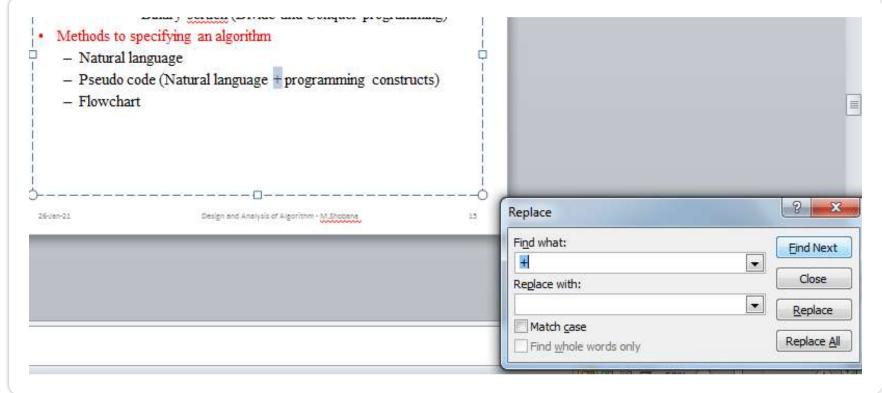
Sorting

- Key
- Colleges, hospitals, office
- Ease of search dictionaries,
 telephone books, class list
- Several algorithm not good for all the situations
- Searching is made easier
- Properties of sorting algorithm
 - Stable
 - In place



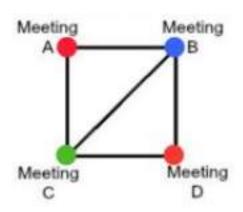
- Searching
 - Search key
 - Several algorithm
- String processing
 - String string matching

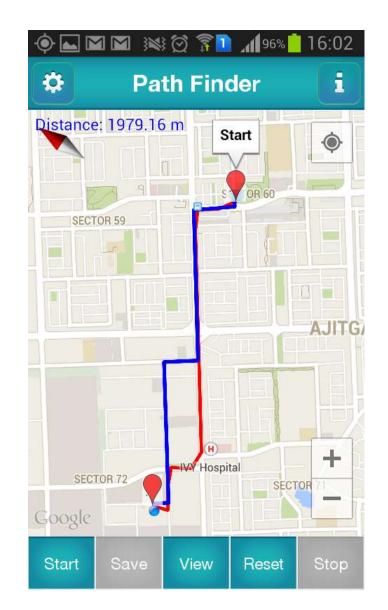




Graph problems

- Vertices, edges
- Graph traversal, shortest path
- Flight network, Google map –
 shortest path
- Ex: travelling salesman problem,
- Graph coloring event scheduling





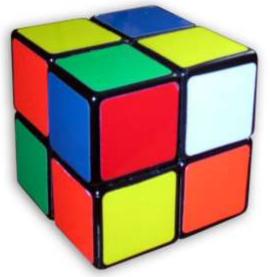
Combinatorial problems

Finding optimal object from a finite set of objects
 (permutation, combination, subset from a finite set)

- Example:

- How many ways are there to make a 2-letter word
- How many ways are there to select 5 integers from {1, 2,, 20}

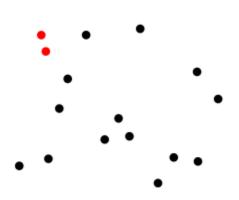


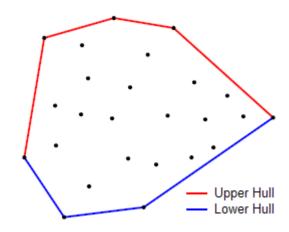


- Geometric Problems
 - Points, lines, polygons
 - Computer graphics (circle, smiley)
 - Example

Closest pair problem

Convex hull problem





<u>Real-time application</u>Nuclear/chemical leak EvacuationTracking Disease epidemic

• Numerical Problems

- Integrals, functions
- Approximate
- Real numbers