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DEPARTMENT OF MATHEMATICS UNIT – II TESTING OF HYPOTHESIS

JEST OF SIGNIFICANCE OF LARGE SAMPLES : + Tabulated values . JEST JOR BINGLE MEAN: Null Hypothesis, Ho : H= Mo Test statistics, $z = \frac{\bar{n} - \mu}{\sigma / v_n}$ (or) $z = \frac{\bar{n} - \mu}{s / v_n}$ 1) A sample of 900 members is found to have a mean of 3.4 cm and s.D. 2.61 cms. Is the sample from a large population of mean 3.25 cm and s. p. 2.61 cms. of the population & normal and its mean is unbrown find the 95% confidential (ficherial) limits of the mean. Soln: given: n= 900, n= 3.4, µ= 3.25, 0= 2.61 Step1: Formulating Ho & HI : Ho : H = 3.25 H1: p1 7 8 25 (two tailed test) Step 2: Level of right ficances = 5% = 0.05





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step 3 : Test statestie, z = 2-14 = 3.4-3.25 <u>2.61</u> V900 Step 4: Critical value at 5%. is Zx=1.96. Step 5 : Conclusion: Since 121=1.724 < 1.96= 24, Ho is accepted at 5%. Level & Significance. . The sample & taken from population where mean is 3.25 cm , Confidence simila: $\mu = \hat{n} \pm z_{\alpha} \frac{\nabla}{V_{\alpha}}$ = 3.4 ± 1.96 × 2.61 = 3.4 ± 0.17 = 3.23, 3.54 (ù) 3·23 × µ × 3·57





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2) A random sample a 200 employees at a large arporation showed their average to be 42.8 years with a s.D. g 6.89 years. Test The hypotheses Ho: $\mu = 40$. Hi: $\mu > 40$ at $\alpha = 0.01$ level g significance Soln: Miren: n = 200, $\overline{n} = 42.8$, $\mu = 40$, $\nabla = 6.89$ Step 1: Formulating Ho and H,: Ho: $\mu = 40$ Ho: $\mu = 40$ Ho: $\mu > 40$ Cone fail test - sight) step 2: Level of significance, $\alpha = 0.01$. steps: Test statistic, Z = 5- H $\frac{\frac{6\cdot 89}{1200}}{=5\cdot 747}$ step 4: Crétical value at 1.1. (one tailed - light) is $Z_{x} = 2.33$ = 42.8-40





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step 5: Conclusion: Rince 121=5.747 > 2.33=24 . Ho & rejected at 14 level 9 Rightificance . The hypothesis, M, 14>40 is accepted.

3) The mean height g college students in a cilij are normally distributed with S.D. 6 cms. A sample g 100 students has mean height g 158 cms. Test the hypothesis that the mean height g college students in the city 160 cm's. Also obtain 99% confidence limits for the true mean.
Solo: Given: n= 100, n= 158, μ= 160, σ=6

Step 1. Formulating Ho and H, : Ho: N= 160 H1: M 7 160 (two dailed test)

(step 2 : Level q rightficance, $\alpha = 1/k$ slip 3 : Test statistic, $z = \frac{\overline{a} - \mu}{\sqrt{n}}$ $= \frac{158 - 160}{6/\sqrt{100}}$ = 3.33





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Step 4: critical value at 17. (two ride test) is $z_{\alpha} = 2.58$ Step 5: Conclusion; Enrice 121 = 3.33 > 2.58 = z_{α} : Ho is rejicited at 17. Jevel of rightficance. : The mean height of the cottage students in the city is 160 cms is not true. Confidence limit: $\mu = \bar{n} \pm z_{\alpha} \frac{\overline{v_n}}{\overline{v_n}}$ = 158 $\pm 2.58 \times \frac{6}{\overline{v_{10}c}}$ = 158 ± 1.548 (i) 156.452 $\times \mu \times 159.548$, here $\mu = 160$ does not Lies is the interval.





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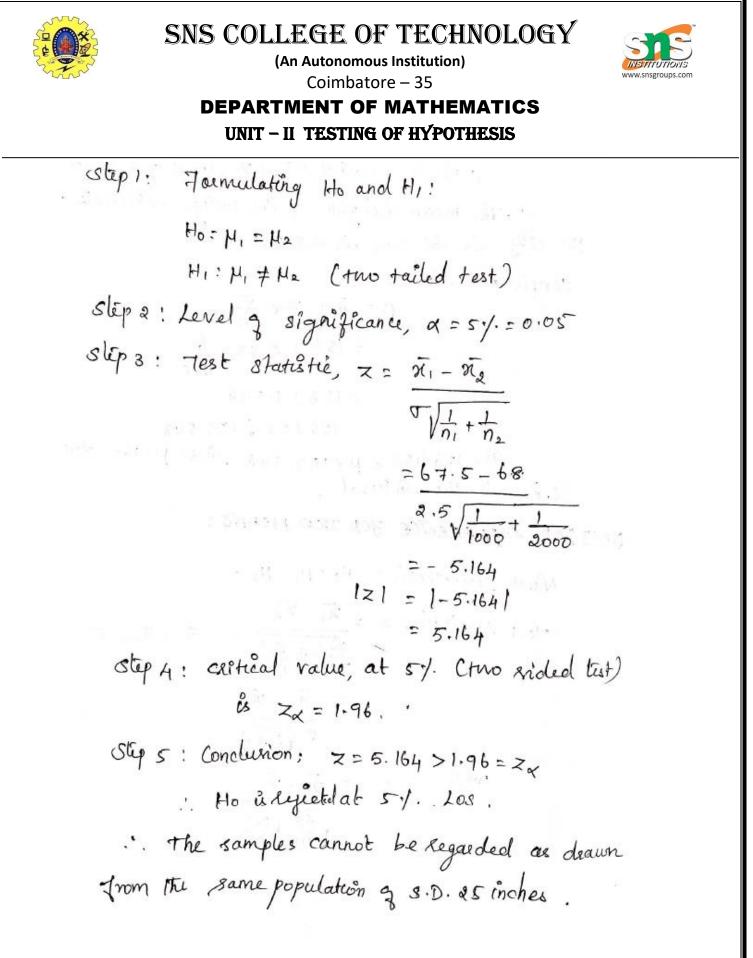
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JEST FOR DIFFERENCE FOR TWO MEANS :

Null hypothesis : Ho :
$$H_1 = H_2$$

Hest Statistic, $z = \frac{\overline{\chi_1} - \overline{\chi_2}}{\sqrt{\frac{\overline{\sigma_1}^2}{\overline{\Omega_1}} + \frac{\overline{\sigma_2}^2}{\overline{\Omega_2}}}$ $\overline{\nabla_1} = \overline{\nabla_2} = \overline{\nabla}$
 $= \frac{\overline{\chi_1} - \overline{\chi_2}}{\overline{\nabla\sqrt{\frac{1}{\overline{\Omega_1}} + \frac{1}{\overline{\Omega_2}}}}$
(or) $z = \frac{\overline{\chi_1} - \overline{\chi_2}}{\sqrt{\frac{\overline{\delta_1}^2}{\overline{\Omega_1}} + \frac{\overline{\delta_2}^2}{\overline{\Omega_2}}}$

Whe means q two timple large samples q 1000 and
2000 members are 67.5 inches and 68 inches rey.
Can the samples be regarded as drawn from the
same population q standard deviation of 25 inches,
Test at 5% level of Rignificence (105)
Soln:
$$\eta_1 = 1000$$
, $\pi_1 = 67.5$,
 $\eta_2 = 2000$, $\pi_2 = 68$, $\Re = 9.5$







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mean g 67.85 inches and s. D. g 2.56 inches while a simple sample of heighte of 1600 soldiers Thas a mean of 68.55 Inches and 3. D. of 2.50 inches. Do the data, indicate that soldiers are on the average talles than sailors ? use 51 Los. <u>soln</u>: equien: Bailors: n, = 6400, 5, =67.85, 8, =2,56 Soldiers: no = 1600, no= 68.55, So= 2.52 Step 1: Farmulating Ho and Hi Ho: H1 = H2 H1: M1 < M2 cone tailed test- Left) Step 2 : Los at 5 1. as x=0.05 step 3: Test statistic, Z = II - N2 $\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}$ = 67.85-68-55 $\sqrt{\frac{(2.56)^2}{(2.52)^2}} + \frac{(2.52)^2}{(2.52)^2}$ = -9.91 |z| = |-9, 9|= 9,91 slep 4 : critical value at 5% (one tail test) i zu= 1.645





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stip 5: Conclusion: z=9.91>1.645=zx . Ho is rejected at 5% g Los ... The data indicates that soldiers are on the average taller than sailors

* A semple sample og height og 6400 English men has a 7 mean g 170 cm & s. D. g 64 cm, while a simple sample q heights of 1600 Americans has a mean of 172 cm & 3. D. of 6.3 cm Do the data indicate that Americans are the any. talles than the English men? [Z=11.32, M, < M2. Americans are taller than English men]

3% The average hously ways & a sample & 150 workers in plant A was Rs 2.56 with a s.D. g Rs 1.08. The average waye q a sample q 200 wolkers in plant B was Rs 2.87 with a S.D. g Rs 1.28 can an applicant sayely assume that the houry ways paid by plant & are higher than those paid by plant A? Istn: given: plant A: n,=150, n,=2.56, 31=1.08

plant B: ng = 200, Ng = 2.87, Sg = 1.28





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Step 1: formulating Ho and H, Ho: H1= H2 : 1 HI: MI< HO Cone-tailed test) sup 2: 205, x=51/. = 0.05 sleps: Test statistic, Z = x1 - x2 $\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}$ 20° 20 199 192 -= 2.56 - 2.84 10 P. 17 = 2.453 step 4: certical value, at 5%. Los & Zx = 1.645 steps: Conclusion: z= 2.453 >1.645 = Zx Ho is repetied at 5 %. Los. . The hourly ways paid by plant B are higher than those paid by plant A.