



## DEPARTMENT OF MATHEMATICS

### UNIT – II TESTING OF HYPOTHESIS

#### STUDENT'S $t$ -TEST :

##### TEST FOR DIFFERENCE OF MEAN:

Null hypothesis ;  $H_0 : \mu_1 = \mu_2$

$$\text{Test statistics, } t = \frac{\bar{x}_1 - \bar{x}_2}{s \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$$

$$\text{where } s^2 = \frac{n_1 s_1^2 + n_2 s_2^2}{n_1 + n_2 - 2} \quad (\text{or}) \quad s^2 = \frac{\sum (x_1 - \bar{x}_1)^2 + \sum (x_2 - \bar{x}_2)^2}{n_1 + n_2 - 2}$$

Degree of freedom ;  $\nu = n_1 + n_2 - 2$ .

- 1) In a test examination given to two groups of students, the marks obtained were as follows:

Group I : 18 20 36 50 49 36 34 49 41

Group II : 29 28 26 35 30 44 46

Examine whether the significance of difference between the average marks secured by the students of the above two groups.

Soln: Given: Group I :  $n_1 = 9$   
Group II :  $n_2 = 7$ .



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$$\text{Now } \bar{x}_1 = \frac{18 + 20 + 36 + 50 + 49 + 36 + 34 + 49 + 41}{9} = 34.$$

$$\bar{x}_2 = \frac{29 + 28 + 26 + 35 + 30 + 44 + 46}{7} = 34.$$

$x_1$	$x_1 - \bar{x}_1$	$(x_1 - \bar{x}_1)^2$	$x_2$	$(x_2 - \bar{x}_2)$	$(x_2 - \bar{x}_2)^2$
18	-19	361	29	-5	25
20	-14	289	28	-6	36
36	-1	1	26	-8	64
50	13	169	35	1	1
49	12	144	30	-4	16
36	-1	1	44	10	100
34	-3	9	46	12	144
49	12	144			
41	4	16			

$$\sum (x_1 - \bar{x}_1)^2 = 1134$$

$$\sum (x_2 - \bar{x}_2)^2 = 386.$$

$$\begin{aligned} \text{Now } S^2 &= \frac{\sum (x_1 - \bar{x}_1)^2 + \sum (x_2 - \bar{x}_2)^2}{n_1 + n_2 - 2} \\ &= \frac{1134 + 386}{9 + 7 - 2} = 108.54 \end{aligned}$$

$$\Rightarrow S = 10.41$$



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Step 1: Formulating  $H_0$  and  $H_1$

$$H_0: \mu_1 = \mu_2$$

$$H_1: \mu_1 \neq \mu_2 \text{ (two tailed test)}$$

Step 2: Los at  $\alpha = 5\%$ .

Step 3: Test statistic,  $t = \frac{\bar{x}_1 - \bar{x}_2}{S \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$

$$= \frac{37 - 34}{10.42 \sqrt{\frac{1}{9} + \frac{1}{7}}}$$

$$= 0.5713$$

Step 4:  $t_{tab}$  for degrees of freedom,  $\nu = n_1 + n_2 - 2$

$$= 9 + 7 - 2$$

$$\nu = 14$$

$$(ii) t_{tab} = (t_{\alpha}) = 2.145$$

Step 5: Conclusion:  $t = 0.5713 < 2.145 = t_{\alpha}$

$\therefore H_0$  is accepted at 5% Los.

$\therefore$  there is no significant difference in the avg. marks of the two groups of students.



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2) A samples of two types of electric bulbs were tested for length of life and the following data were obtained.

Samples	size	mean	SD
I	8	1134	35
II	4	1024	40

Test at 5%.

Soln: Given:

sample I :  $n_1 = 8$ ,  $\bar{x}_1 = 1134$ ,  $s_1 = 35$

Sample II :  $n_2 = 4$ ,  $\bar{x}_2 = 1024$ ,  $s_2 = 40$ .

step 1: Formulating  $H_0$  and  $H_1$ .

$$H_0: \mu_1 = \mu_2$$

$H_1: \mu_1 \neq \mu_2$  (two tailed test)

step 2: Los at  $\alpha = 5\%$ .

step 3: Test statistic,  $t = \frac{\bar{x}_1 - \bar{x}_2}{S \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$

$$\text{Now } S^2 = \frac{n_1 s_1^2 + n_2 s_2^2}{n_1 + n_2 - 2}$$



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$$= \frac{8(35)^2 + 7(40)^2}{8+7-2}$$

$$= 1615.38$$

$$s = 40.19$$

$$\therefore t = \frac{1134 - 1024}{40.19 \sqrt{\frac{1}{8} + \frac{1}{7}}}$$

$$= \frac{110}{20.8} = 5.288$$

step 4:  $t_{tab}$  for degrees of freedom,  $v = n_1 + n_2 - 2$

$$= 8 + 7 - 2$$
$$= 13$$

(ii)  $t_{tab}: t_{\alpha} = 2.160$

step 5: Conclusion:  $t = 5.288 > 2.160 = t_{\alpha}$

$\therefore H_0$  is rejected at 5%.