

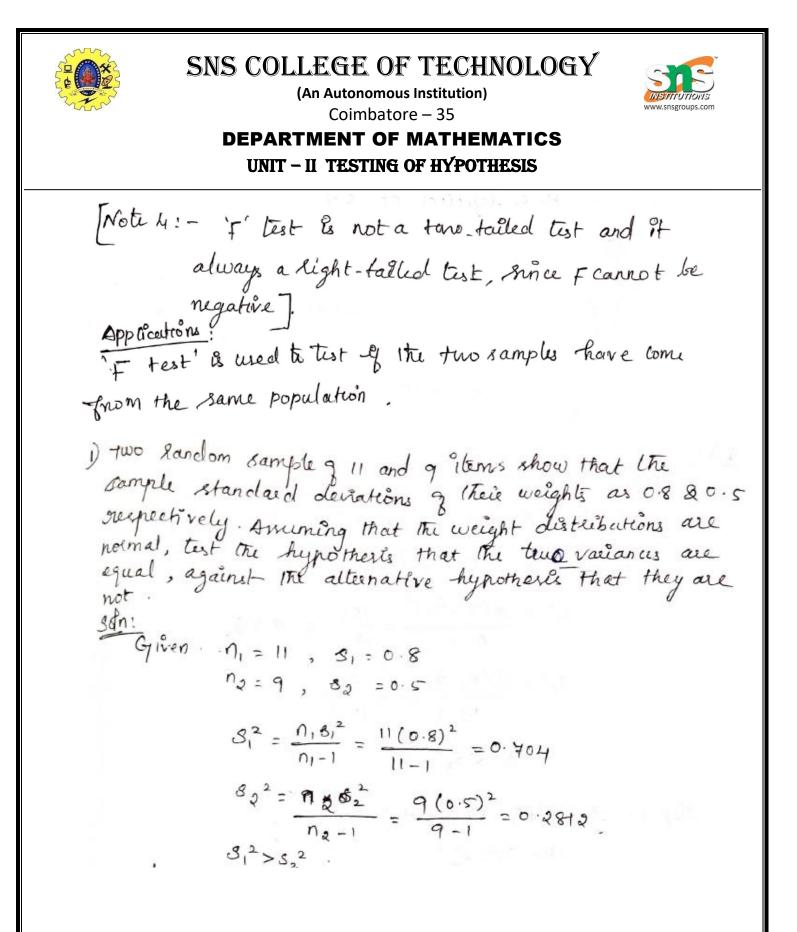


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DEPARTMENT OF MATHEMATICS UNIT – II TESTING OF HYPOTHESIS

VARIANCE RATIO TEST (OF) F. Test JOR EQUALITY OF VARIANO Null Thypothesis Ho! $\nabla_1^2 = \overline{\nabla_2}^2$ Test stastics : $F = \frac{S_1^2}{s_2^2}$ where $S_1^2 > S_2^2$. Ushere $S_1^2 = \frac{n_1 S_1^2}{n_1 - 1}$ of $S_1^2 = \frac{S(n_1 - \overline{n_1})^2}{n_1 - 1}$ $S_2^2 = \frac{n_2 S_2^2}{n_2 - 1} \quad \text{of} \quad S_2^2 = \frac{S(n_2 - \bar{n_2})^2}{n_2 - 1}$ Deglee & Freedom: (Ve, V2) where $V_1 = (n_1 - 1)$, $V_2 = (n_2 - 1)$ Note 1:- F Greater than zerone always. Note 2 :- Suppose S_2^2 greater than S_1^2 , then $F = \frac{S_2^2}{S_2^2}$ with degree of greadom, VI=ng-1, Vg=n,-1 Note 3: - of we want to test whether the two independent samples hanky dearn from the same population we have to test, * 'E' test (to find quality 3 population mean) * 'F' test (to find equality 3 population variances) * 'F' test , we use 'F' test first end then 't' test, if 'F' test is failed then 't' lest should not be used.







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Step 1 \rightarrow Jamulate Ho & H₁ Ho: $\overline{\sigma_{1}^{2}} = \overline{\sigma_{2}^{2}}$ H₁: $\overline{\sigma_{1}^{2}} \neq \overline{\sigma_{2}^{2}}$ Step 2 \rightarrow Los at $\alpha = 5 \gamma$. Step 3 \rightarrow Test Statistic, $F = \frac{S_{1}^{2}}{S_{2}^{2}} = \frac{0.704}{0.2812} = 2.5$ Step 4 \rightarrow Degrees q Jseedom $(S_{1}, S_{2}) = (1, n_{2} - 1) \neq 2$. = (10, 8)Cuincalvalue, F_{tab} : $F_{\alpha} = 3.35$ Step 5 \rightarrow Conclusion: $F = 2.5 < 3.35 = F_{\alpha}$ \therefore Ho is accepted at $\alpha : 5\gamma$.) Two random samples yave the following levells:

2 100 kanalom samples yave the following lexults: Sample Size samplemean sum q aqueres a deviation. Jeom The means. 1 12 14 108 2 10 15 90 Jest whether The samples came from The same population.



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soln :
Given:
$n_1 = 12$, $2\bar{n}_1 = 14$, $\leq (2\bar{n}_1 - \bar{n}_1)^2 = 108$
$n_2 = 10, \ \overline{n}_2 = 15 \ \leq (n_2 - \overline{n}_2)^2 = 90$
$S_1^2 = \frac{\mathcal{E}(n_1 - \bar{n}_1)^2}{n_1 - 1} = \frac{108}{12 - 1} = 9.818$
$S_{2}^{2} = \frac{\sum (n_{2} - \overline{n}_{2})^{2}}{n_{2-1}} = \frac{90}{10-1} = 10$
$S_1^2 < S_2^2$
step 1: Formulati Ho and H,:
Ho: $\nabla_1^2 = \sigma_2^2$
$H_1: \nabla_1^2 \neq \sigma_2^2$
stip 2: Los at $\alpha = 5/$.
Step 3: Test statistics, $F = \frac{S_2^2}{S_1^2} = \frac{10}{9.818}$
F = 1.018

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Step 4 : Degrees of freedom = (v, v,) = (ng-1), n, -1) = (9,11) critical value, Fx = 2.90 Step 5 : Conclusio: F=1.018 < 2.90= Fa . .". Ho is accepted at 5% Los. (i) t' Test : step 1: Youmulate Ho & HI .: Ho: H1 = H2 HI: HI + MI oup 2: Los at 5 y .= x step 3: Test statistic, $b = \overline{n_1 - n_2}$ $S \sqrt{\frac{1}{n_1 + n_2}}$ Here n= 12, n2 = 10; \$1 = 14, \$2=15 Now $s^2 = \Xi(n_1 - \bar{n}_1)^2 + \Xi(n_2 - \bar{n}_2)^2$ $n_1 + n_2 - 2$





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UNIT – II TESTING OF HYPOTHESIS

$$= \frac{108 + 90}{12 + 10 - 2} = 9.9$$

$$S = 3.14$$

$$\therefore E = \frac{14 - 15}{3.14} = -0.444$$

$$IEI = 0.444$$

$$Step 4: Degrees g freedom, $v = n_1 + n_2 - 2$

$$= 12 + 10 - 2$$

$$= 20$$

$$\therefore E_{x} = 2.086$$

$$Step 5: Concluinon, E = 0.4444 < 2.086 = E_{y}$$

$$\therefore Ho is accepted at $5y$. Los$$$$

3) Test whether the population variances are identical: Sample I: 10 11 16 12 10 11 12 16 Sample I: 7 9 3 7 9 3 15 at 17-205 Soln: Given: n= 8; n2 = 7

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Soln: Given	: n,= 8 ; n2	= H		
N	(n,-x) 2	22 1	(m2 - m2)2	
10	5.0625	넉	0.3265	
11	1. 5625	9	2.0409	
	14.0625	3	20.8944	
16	0.0625	7	0.3265	
12 10	5.0625	9	2.0409	
11	1.5625	3	20.8944	
12	0.0625	15	55.1841	
16	14,0625		101, 4143	
, 98	41.5	53	5(12-72)? (01.71	
$\bar{\eta}_{1} = \frac{98}{2} = \frac{2(\eta_{1} - \bar{\eta}_{1})^{2}}{2} = 41.6^{-1} \bar{\eta}_{2} = \frac{1}{2}$				
$\overline{\eta_{1}: \frac{2\eta_{2}}{n} = \frac{98}{8}} = \frac{41.5}{\mathcal{E}(\eta_{2}-\overline{\eta_{1}})^{2} = 41.5} = \frac{53}{3.5} = \frac{53}{5} \cdot \frac{1}{3} \cdot \frac{54}{5}$				





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 $\frac{1}{N_1^2} = \frac{\sum (\pi_1 - \pi_1)^2}{n_1 - 1} = \frac{41.5}{7} = 5.9286$ $S_{2}^{2} = \frac{S(\pi_{2} - \pi_{2})^{2}}{n_{2} - 1} = \frac{101.7143}{6} = 16.9524$ S12 < S,2. Step1: Joenulate Ho& HI: H_{r} : $\nabla_{r}^{2} = \nabla_{q}^{2}$ H1: 512 + 522 step 2: Los at \$ = 1 %. Slip 3 : Test statistic, $F = \frac{S_2^2}{C_2^2}$ = 16-9524 = 2.86 5.9286 step 4 : Degrees 9 Freedom: (12, 12) = (n, -1, n, -1) = (6, 7) : Fx = 7.19 Step 5: Conclusion, F= 2.86 < 7.19 = Fx . Ho & accepted at Ho at 1 %. Los.