



## DEPARTMENT OF MATHEMATICS

### UNIT – II TESTING OF HYPOTHESIS

#### CHI - SQUARE TEST :

$$\chi^2 = \sum \frac{[O_i - E_i]^2}{E_i}$$

where  $O_i \rightarrow$  Observed frequency

$E_i \rightarrow$  Experimental frequency or Expected frequency

Degrees of freedom,  $\nu = n - 1$

$$= \frac{\sum O_i}{n}$$

- 1) The table below gives the number of aircraft accidents that occurred during the various days of the week. Test whether the accidents are uniformly distributed over the week.

Days	: Mon	Tues	Weel	Thurs	Fri	Sat
No. of accidents:	14	18	12	11	15	14

Soln:

Given, total no. of accidents = 84

No. of days = 6

$\therefore$  Expected frequencies of the accidents  $= \frac{84}{6}$   
 $= 14$



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$O_i$	$E_i$	$(O_i - E_i)^2$	$\frac{(O_i - E_i)^2}{E_i}$
14	14	0	$0/14 = 0$
18	14	16	$16/14 = 1.14$
12	14	4	$4/14 = 0.285$
11	14	9	$9/14 = 0.642$
15	14	1	$1/14 = 0.071$
14	14	0	$0/14 = 0$
			<hr/>
			$\sum \frac{(O_i - E_i)^2}{E_i} = 2.14285$

Step 1: Formulate  $H_0$  &  $H_1$ :

$H_0$ : The accidents are uniformly distributed.

$H_1$ : The accidents are not uniformly distributed.

Step 2: Los at  $\alpha = 5\%$ .

Step 3: Test statistic,  $\chi^2 = \sum \frac{(O_i - E_i)^2}{E_i} = 2.1428$



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Step 4: Degrees of freedom,  $\nu = n - 1$

$$= 6 - 1$$

$$= 5$$

Tab value is  $11.07 = \chi^2_{\alpha}$

Step 5: Conclusion:

$$\chi^2 = 2.1428 < 11.07 = \chi^2_{\alpha}$$

$\therefore H_0$  is accepted at 5% los.  $\therefore$  The accidents are uniformly distributed.

2) A die was thrown 498 times. Denoting  $x$  to be the number appearing on the top face of it, the observed frequency of  $x$  is given below:

$x$ : 1    2    3    4    5    6

$f$ : 69   78   85   82   86   98

What opinion you would form for the accuracy of the die?

Soln: Given, Expected frequency,  $E_i = \frac{\text{total frequency}}{6}$

$$= \frac{498}{6} = 83$$



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$x$	$O_i$	$E_i$	$(O_i - E_i)^2$	$(O_i - E_i)^2 / E_i$
1	69	83	196	2.3614
2	78	83	25	0.3012
3	85	83	4	0.0481
4	82	83	1	0.0120
5	86	83	9	0.1084
6	98	83	225	2.7108
				<hr/>
				$\frac{\sum (O_i - E_i)^2}{E_i} = 5.5419$

step 1: Formulate  $H_0$  &  $H_1$ :

$H_0$ : A die is unbiased

$H_1$ : A die is not unbiased i.e. biased

step 2: Los at  $\alpha = 5\%$ .

step 3: Test Statistic,  $\chi^2 = \frac{\sum (O_i - E_i)^2}{E_i} = 5.542$ .



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step 4: Degrees of freedom,  $\nu = n - 1$   
 $= 6 - 1$   
 $= 5$

$$\therefore \chi^2_{\alpha} = 11.07$$

step 5: Conclusion;

$$\chi^2 = 5.542 < 11.07 = \chi^2_{\alpha}$$

$\therefore H_0$  is accepted at 5% Los. (a) A die is unbiased.

3) The number of automobile accident per week in a certain community as follows 12, 8, 20, 2, 14, 10, 15, 6, 9, 4 are the frequency in agreement with a belief that accident where the same during is 10 week.

Soln:  $E_i = \frac{100}{10} = 10$ ;  $\chi^2 = 26.6$ ; Degrees of freedom:  $10 - 1 = 9$

$\chi^2 > \chi^2_{\alpha}$  at 5% Los,  $H_0$  is rejected (a) The accident condition where not same during 10 week period.





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properties:

- i) The mean of  $\chi^2$  dist. is equal to the no. of degrees of freedom
- ii) The variance of  $\chi^2$  dist. is twice the degrees of freedom
- iii) If  $\chi^2$  is a chi-square variate with  $\nu$  degrees of freedom, then  $\chi^2/2$  is a gamma variate with parameter  $\nu/2$ .
- iv) Standard  $\chi^2$  variate tends to standard normal variate as  $n \rightarrow \infty$ .

Applications:

- i) To test if the hypothetical value of the population variance is  $\sigma^2 = \sigma_0^2$
- ii) To test the goodness of fit.
- iii) To test the independence of attributes.
- iv) To test the homogeneity of indep. estimates of the population variance.

Degrees of freedom: No. of values in a set which may be assigned arbitrarily.