



DEPARTMENT OF MATHEMATICS

UNIT – I TESTING OF HYPOTHESIS

STUDENT'S t -TEST :

PROCEDURE :

- Step 1: Formulate H_0 and H_1 ,
- Step 2: Los at $\alpha\%$.
- Step 3: ^{compute} Test statistic t .
- Step 4: Calculate t_{tab} for degrees of freedom at level α
- Step 5: Conclusion.

TEST FOR SINGLE MEAN:

Null hypothesis : $H_0: \mu = \mu_0$.

Test Statistic, $t = \frac{\bar{x} - \mu}{s/\sqrt{n-1}}$ if SD is given.

$t = \frac{\bar{x} - \mu}{s/\sqrt{n}}$ if SD is not given.

To find s :

$$s^2 = \frac{\sum (x_i - \bar{x})^2}{n-1}$$

Degrees of freedom: $\nu = n-1$

NOTE: Confidence limit: $\bar{x} \pm t_{\alpha} \frac{s}{\sqrt{n-1}}$



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1) A random sample of 10 boys had the following IQ's.
70, 120, 110, 101, 88, 83, 95, 98, 107, 100. Do these
data support the assumption of a population mean IQ's
of 100? Find a reasonable range in which most of the
mean IQ's value of sample 10 boys.

Soln: given : $n = 10$, $\mu = 100$

$$\bar{x} = \frac{70 + 120 + 110 + 101 + 88 + 83 + 95 + 98 + 107 + 100}{10}$$

$$= 97.2$$

To find s : $s^2 = \frac{\sum (x - \bar{x})^2}{n - 1}$

$$x : 70 \quad 120 \quad 110 \quad 101 \quad 88 \quad 83 \quad 95 \quad 98 \quad 107 \quad 100$$

$$x - \bar{x} : -27.2 \quad 22.8 \quad 12.8 \quad 3.8 \quad -9.2 \quad -14.2 \quad -2.2 \quad 0.8 \quad 9.8 \quad 2.8$$

$$(x - \bar{x})^2 : 739.84 \quad 519.84 \quad 163.84 \quad 14.44 \quad 84.64 \quad 201.64 \quad 4.84 \quad 0.64 \quad 96.04 \quad 7.84$$

$$\sum (x - \bar{x})^2 = 1833.6$$

$$\therefore s^2 = \frac{\sum (x - \bar{x})^2}{n - 1} = \frac{1833.6}{10 - 1}$$

$$= 203.73$$

$$\Rightarrow s = 14.27$$



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Step 1: Formulating H_0 and H_1 :

$$H_0: \mu = 100$$

$$H_1: \mu \neq 100 \text{ (two tailed test)}$$

Step 2: LOS. at $\alpha = 5\% = 0.05$.

Step 3: Test statistic, $t = \frac{\bar{x} - \mu}{s/\sqrt{n}}$

$$= \frac{97.2 - 100}{14.29/\sqrt{10}}$$

$$= -0.62$$

$$|t| = 0.62$$

Step 4: t_{tab} for degree of freedom, $\nu = n - 1$

$$\nu = 10 - 1 = 9$$

(ii) $t_{tab} : 2.262 (t_{\alpha})$

Step 5: Conclusion: $t = 0.62 < 2.262 = t_{\alpha}$

$\therefore H_0$ is accepted at 5% LOS.

(i.e.) the population mean IQ's is 100.



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Confidence limit:

$$\mu = \bar{x} \pm t_{\alpha} \frac{s}{\sqrt{n-1}}$$

$$= 97.2 \pm 2.262 \times \frac{14.27}{\sqrt{10-1}}$$

$$= 97.2 \pm 10.759$$

$$= 107.95, 86.45$$

2) A sample of 26 tube lights gives a mean life of 990 hours with a standard deviation of 20 hours. The company claims that the mean life of tube lights is 1000 hours. Is the sample upto the specifications?

Soln: Given: $n=26$, $\bar{x}=990$, $s=20$, $\mu=1000$

step 1: Formulating H_0 and H_1 :

$$H_0: \mu = 1000$$

$$H_1: \mu < 1000 \text{ (one-tailed test)}$$

step 2: LOS at $\alpha = 5\%$.

step 3: Test Statistic, $t = \frac{\bar{x} - \mu}{s/\sqrt{n-1}}$



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$$= \frac{990 - 1000}{20/\sqrt{26-1}} = -2.5$$

$$|t| = 2.5$$

Step 4: t_{tab} for degree of freedom, $v = n - 1 = 26 - 1 = 25$

(w) $t_{tab}: t_{\alpha} = 1.7080$ (two tailed at 10%) (u) $t_{\alpha} \neq 0$ at 5%

Step 5: Conclusion: $t = 2.5 > 1.7080 = t_{\alpha}$ (at 5% level of significance)

$\therefore H_0$ is rejected at 5% LOS.

(a) The sample is ~~not~~ upto the specifications.

3) The weights of 10 peoples of a locality are found to be 70, 67, 62, 68, 61, 68, 70, 64, 64, 66 kg. It is reasonable to believe that the average weights of people locality greater than 64 kg. Test at 5% LOS.

Soln: Given: $n = 10$, $\mu = 64$

$$\bar{x} = \frac{70 + 67 + 62 + 68 + 61 + 68 + 70 + 64 + 64 + 66}{10}$$

$$\bar{x} = 66$$

To find s :

$$s^2 = \frac{\sum (x_i - \bar{x})^2}{n-1}$$



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x :	70	67	62	68	61	68	70	64	64	66
$x - \bar{x}$:	4	1	-4	2	-5	2	4	-2	-2	0
$(x - \bar{x})^2$:	16	1	16	4	25	4	16	4	4	0

$$\sum (x - \bar{x})^2 = 90$$

$$\therefore s^2 = \frac{\sum (x - \bar{x})^2}{n-1} = \frac{90}{10-1} = 10$$

$$s = 3.16$$

Step 1: Formulating H_0 and H_1 :

$$H_0: \mu = 64$$

$$H_1: \mu \geq 64 \text{ (one tailed test - right)}$$

Step 2: Los at $\alpha = 5\%$.

Step 3: Test statistic, $t = \frac{\bar{x} - \mu}{s/\sqrt{n}}$

$$= \frac{66 - 64}{3.16/\sqrt{10}}$$

$$= 2.02$$



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step 4: t_{tab} for degree of freedom, $\nu = n - 1$

$$= 10 - 1$$

$$= 9$$

as $t_{tab}: t_{\alpha} = 1.833$ (at two tailed at 10 %)
(no table)

$t_{\alpha} = 1.833$ (at one tailed at 5 %)

step 5 : Conclusion: $t = 2.02 > 1.833 = t_{\alpha}$

$\therefore H_0$ is rejected at 5 % LOS

(a) the avg. weight of people locality is greater than 64.1 kg.