



(An Autonomous Institution) Coimbatore - 35

DEPARTMENT OF MATHEMATICS

UNIT - I TESTING OF HYPOTHESIS

VARIANCE RATIO TEST CON F- Test FOR EQUALITY OF VARIANCE

Null Thypothesis: Ho! $\nabla_1^2 = \overline{\nabla_2}^2$

Test stastics: $F = \frac{S_1^2}{\sigma^2}$ where $S_1^2 > S_2^2$.

where $S_1^2 = \frac{n_1 S_1^2}{n_1 - 1}$ of $S_1^2 = \frac{5(\alpha_1 - \overline{\lambda_1})^2}{n_1 - 1}$ &

 $g_2^2 = \frac{n_2 g_2^2}{n_2 - 1}$ or $g_2^2 = \frac{5(n_2 - \overline{n_2})^2}{n_2 - 1}$

Deglee & Freedom: (Ve, V2)

where $V_1 = (n_1 - 1)$, $V_2 = (n_2 - 1)$

Note 1:- F Greater than zyrone always.

Note 2: - Suppose So greater than Si2, then F = So

with degree of greadom, VI= no-1, ve = n,-1

Note 3: - of one want to best whether the two independent

samples hanky deawn from the same

population we have to test,

* It' test (to find equality of population mean)

* F' test , we use F' test first and then

't' test, " F' test is failed then 't' lest

should not be used.





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Note 4:- 'f' test & not a tone tailed test and it always a light-falled test, since F cannot be negative].

Applications:

From the same population.

i) two landom sample 9 11 and 9 ilems show that the sample standard deviations of their weights as 0.8 & 0.5 respectively. Assuming that the weight distributions are normal, test the hypothesis that the two variances are equal, against the alternative hypothesis that they are not.

Son:

Given: $n_1 = 11$, $s_1 = 0.8$ $n_2 = 9$, $s_2 = 0.5$

$$S_1^2 = \frac{n_1 s_1^2}{n_1 - 1} = \frac{11(0.8)^2}{11 - 1} = 0.404$$

$$S_2^2 = \frac{n_2 s_2^2}{n_2 - 1} = \frac{9(0.5)^2}{9 - 1} = 0.2812$$





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slip 3 > Test Statistic,
$$F = \frac{S_1^2}{S_2^2} = \frac{0.704}{0.2812} = 2.5$$





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sofn:

Given :

$$n_{1} = 12 , \overline{x_{1}} = 14 , \underline{\xi}(x_{1} - \overline{x_{1}})^{2} = 108$$

$$n_{2} = 10 , \overline{x_{2}} = 15 \underline{\xi}(x_{2} - \overline{x_{2}})^{2} = 90$$

$$s_{1}^{2} = \underline{\xi}(x_{1} - \overline{x_{1}})^{2} = \underline{108}$$

$$\overline{n_{1} - 1} = \frac{108}{12 - 1} = 9.818$$

$$S_{2}^{2} = \underline{\xi}(x_{2} - \overline{x_{2}})^{2} = \underline{90}$$

$$\overline{n_{2} - 1} = \frac{90}{10 - 1} = 10$$

Step 1: Formulati Ho and Hi:

Ho:
$$\nabla_1^2 = \sigma_2^2$$

Hi: $\nabla_1^2 \neq \sigma_2^2$

stip 2: Los at a = 5%.

Step 3: Test statistics,
$$F = \frac{S_2^2}{S_{12}} = \frac{10}{9.818}$$

$$F = 1.018$$





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critical value, Fx = 2.90

Step 5 : Conclusion:

.. Ho is accepted at 5% Los.

(11) t'- Test:

step 1: Hormulate Ho & Hi:

Ho: H1 = H2

HI; HI + Mr

otip 2: Los at 5/ = x

Here n= 12, n2 = 10; \$\overline{\pi}_1 = 14, \$\overline{\pi}_2 = 15

Now
$$g^2 = \frac{\sum (y_1 - \overline{y_1})^2 + \sum (y_2 - \overline{y_2})^2}{n_1 + n_2 - 2}$$





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$$3 = \frac{108 + 90}{12 + 10 - 2} = 9.9$$

$$\therefore E = \frac{14 - 15}{3.14 \sqrt{\frac{1}{12} + \frac{1}{10}}} = -0.444$$

Styr4: Degrees of freedom, r=n,+n,-2 = 12+10-2 = 20

:. Ex = 2.086 step 5: conclusion, E = 0.744 < 2.086 = Eq :. Ho is accepted at 5 y. Los.

3) Test whether the population variances are identical:

Sumple I: 10 11 16 12 10 11 12 16

Sample II: 7 9 3 7 9 3 15 at 17-Los

Soln: Given: N=8; N=7





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Schr.
$$2 \frac{1}{1} \sqrt{2} = \frac{1}{1} \sqrt{2$$





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$$S_1^2 = \frac{\sum (n_1 - \overline{n}_1)^2}{n_1 - 1} = \frac{41.5}{7} = 5.9286$$

$$8x^2 = \frac{5(92-92)^2}{92-1} = \frac{101.7143}{6} = 16.9524$$

Step1: Formulate Ho & Hi:

step 2: Los at \$ = 17.

Slip 3: Test statistic,
$$F = \frac{S_2^2}{S_1^2}$$

otep 4: Degrees q Freedom: (v, v2)

$$= (n_{2-1}, n_{1-1})$$

Step 5: Conclusion, F= 2.86 < 7.19 = Fx

.. Ho & accepted at Ho at 1 %. Los.