



## DEPARTMENT OF MATHEMATICS

### UNIT – II DESIGN OF EXPERIMENTS

#### COMPLETELY RANDOMISED DESIGN

procedure to find :-

- 2) Sum of all the terms ( $T$ ) & Total no. of Sample size ( $N$ )
- 3) Correction factor ( $C.F$ ),  $C.F = \frac{T^2}{N}$
- 4) TSS : Total sum of squares  

$$= (\text{sum of the squares of all the terms}) - C.F.$$
- 5) SSC : Sum of squares between samples
- 6) SSE : Error sum of squares  

$$= TSS - SSC$$
- 7) Anova table
- 8) Conclusion :
- 9) Formulating  $H_0$  &  $H_1$

1) A completely randomised design experiment with 10 plots and 3 treatments gave the following result.

plot No. :	1	2	3	4	5	6	7	8	9	10
treatment :	A	B	C	A	C	C	A	B	A	B
yield :	5	4	3	7	5	1	3	4	1	4

Analyse the result for treatment effects.



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Treatment				Yield				Treatment			
(n <sub>1</sub> ) A				5	4	3	1	A B C			
(n <sub>2</sub> ) B				4	4	4	-	5 4 3			
(n <sub>3</sub> ) C				3	5	1	-	4 4 5			
								3 4 1			
								1			
x <sub>1</sub>	x <sub>2</sub>	x <sub>3</sub>	Total	x <sub>1</sub> <sup>2</sup>	x <sub>2</sub> <sup>2</sup>	x <sub>3</sub> <sup>2</sup>					
5	4	3	12	25	16	9					
4	4	5	16	16	16	25					
3	4	1	11	9	16	1					
1	-	-	1	1	-	-					
<u>16</u>	<u>15</u>	<u>9</u>	40	<u>84</u>	<u>81</u>	<u>35</u>					
Σn <sub>1</sub>	Σn <sub>2</sub>	Σn <sub>3</sub>		Σn <sub>1</sub> <sup>2</sup>	Σn <sub>2</sub> <sup>2</sup>	Σn <sub>3</sub> <sup>2</sup>					

Step 1: Formulating H<sub>0</sub> & H<sub>1</sub>:

H<sub>0</sub>: There is no significance difference between the treatments.

H<sub>1</sub>: There is significance difference between the treatments.

Step 2: To find T & N:

$$T = \Sigma n_1 + \Sigma n_2 + \Sigma n_3$$

$$N = n_1 + n_2 + n_3$$

$$= 4 + 3 + 3 = 10$$



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Step 3: Correction factor, C.F.

$$C.F = \frac{T^2}{N} = \frac{40^2}{10} = 160$$

$$\begin{aligned} \text{Step 4: } TSS &= \sum x_1^2 + \sum x_2^2 + \sum x_3^2 - C.F \\ &= 84 + 81 + 35 - 160 \\ &= 40 \end{aligned}$$

$$\begin{aligned} \text{Step 5: } SSC &= \frac{(\sum x_1)^2}{n_1} + \frac{(\sum x_2)^2}{n_2} + \frac{(\sum x_3)^2}{n_3} - C.F. \\ &= \frac{16^2}{4} + \frac{15^2}{3} + \frac{9^2}{3} - 160 \\ &= 6 \end{aligned}$$

$$\begin{aligned} \text{Step 6: } SSE &= TSS - SSC \\ &= 40 - 6 = 34 \end{aligned}$$

Step 7: Anova table:

Source of Variation	Sum of Squares	Degrees of Freedom	Mean Square	F-Rat
Between samples (Column)	SSC : 6	$C-1 = 3-1 = 2$	$MSC : \frac{6}{2} : 3$	$F_c : \frac{4}{3} : 1.1$
Within samples (Error)	SSE : 34	$N-C = 10-3 = 7$	$MSE : \frac{34}{7} : 4.9$	$F_a : 11$



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Step 8: Conclusion:

$$F_c = 1.61 < 19.35 = F_{\alpha}, H_0 \text{ is accepted.}$$

∴ There is no significant difference between the treatments.

2) The following table shows the lives in hours of four brands of electric lamps.

A: 1610 1616 1650 1680 1700 1720 1800

B: 1580 1640 1640 1700 1750

C: 1466 1550 1600 1620 1640 1660 1640 1820

D: 1510 1520 1530 1570 1600 1680

perform an analysis of variance and test the homogeneity of the means lives of the 4 brands of lamps. Given:  $\bar{x}_{ij} = \frac{1640}{10}$   $A_j(\min, \max)$



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$x_1$	$x_2$	$x_3$	$x_4$	Total	$x_1^2$	$x_2^2$	$x_3^2$	$x_4^2$
-3	-6	-18	-13	-40	9	36	324	169
-3	0	-9	-12	-24	9	0	81	144
1	0	-4	-11	-14	1	0	16	121
4	6	-2	-7	1	16	36	4	49
6	11	0	-4	13	36	121	0	16
8	-	2	4	14	64	-	4	16
16	-	10	-	26	256	-	100	-
-	-	18	-	18	-	-	324	-
<u>29</u>	<u>11</u>	<u>-7</u>	<u>-43</u>	<u>-6</u>	<u>391</u>	<u>193</u>	<u>853</u>	<u>515</u>
$\Sigma x_1$	$\Sigma x_2$	$\Sigma x_3$	$\Sigma x_4$		$\Sigma x_1^2$	$\Sigma x_2^2$	$\Sigma x_3^2$	$\Sigma x_4^2$

Step 1: Formulating  $H_0$  and  $H_1$

$H_0$ : There is no significance difference between the 4 brands of electric bulbs.

$H_1$ : There is significance difference between the 4 brands of electric bulbs.



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Step 2: To find  $T$  &  $N$

$$T = \sum n_1 + \sum n_2 + \sum n_3 + \sum n_4$$

$$= 29 + 11 - 3 - 43 = -6$$

$$N = n_1 + n_2 + n_3 + n_4$$

$$= 7 + 5 + 8 + 6 = 26$$

Step 3: Correction Factor.

$$C.F = \frac{T^2}{N} = \frac{-6^2}{26} = 138.46$$

Step 4:  $TSS = \sum n_1^2 + \sum n_2^2 + \sum n_3^2 + \sum n_4^2 - C.F$

$$= 391 + 193 + 853 + 515 - 138.46$$

$$= 1950.61$$

Step 5:  $SSC = \frac{(\sum n_1)^2}{n_1} + \frac{(\sum n_2)^2}{n_2} + \frac{(\sum n_3)^2}{n_3} + \frac{(\sum n_4)^2}{n_4} - C.F.$

$$= \frac{29^2}{7} + \frac{11^2}{5} + \frac{-3^2}{8} + \frac{-43^2}{6} - 138.46$$

$$= 120.14 + 24.2 + 1.125 + 308.16 - 138.46$$

$$= 452.2404$$

Step 6:  $SSE = TSS - SSC$

$$= 1950.61 - 452.2404$$

$$= 1498.375$$





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step 7 : Anova table :

Source of Variations	Sum of squares	Degree of freedom	Mean squares	F-Ratio
Between Samples (C)	SS C 222.165 452.2404	C-1 : 4-1 : 3	MSC 222.165 3 : 150.7468	150.7468 F = 104.1381 68.10
Within Samples (E)	SSE 1498.375	N-C : 26-4 : 22	MSE 1498.375 22 : 68.10	= 1.8744 = 2.2136 F <sub>α</sub> (3, 22) = 3.05

Step 8 : Conclusion :

$$F = 2.2136 < 3.05 = F_{\alpha}, H_0 \text{ is accepted.}$$

∴ there is no significant difference between the 4 brands of electric bulbs.