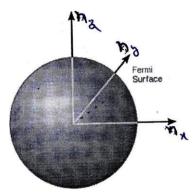




DENSITY OF STATES



The number of states with energy less than E_f is equal to the number of states that lie within a sphere of radius n_f in a region of K-space where n_x , n_y and n_z are positive.

$$N = 2 \times \frac{1}{8} \times \frac{4}{3} \pi n^{3}$$

$$N = 2 \times \frac{1}{8} \times \frac{4}{3} \pi n^{3} = \frac{3N}{\pi}$$

$$N = 2 \times \frac{1}{8} \times \frac{4}{3} \pi n^{3} = \frac{3N}{\pi} \Rightarrow \begin{bmatrix} n_{f} = (\frac{3N}{\pi})^{3} \end{bmatrix}$$

So the Fermi energy

$$E_{f} = \frac{\int_{2ma^{2}}^{f} dx}{2ma^{2}} = \frac{\int_{2ma^{2}}^{f} dx}{\int_{2ma^{2}}^{f} dx} = \frac{\int_{2ma^{2}}^{f} dx}{\int$$

Therefore density of states:
$$D(E) = \frac{1}{dE} = \frac{1}{2} \left(\frac{1}{h^2}\right)^2 \left(\frac{3\pi^2}{3\pi^2}\right) E_f$$

$$D(E) = \frac{V}{2\pi^2} \left(\frac{2m^3}{h^2}\right)^2 E_f^{\frac{1}{2}}$$

Therefore the total number of energy states per unit volume per unit energy range
$$Z(E) = \frac{D(E)}{V} = \frac{1}{2\pi^2} \frac{2m^{\frac{3}{2}-1}}{(h^2)^2} \frac{1}{E_f^2} = \frac{2\pi^2}{2\pi^2} \frac{8\pi^3 E_f^2}{h^3}$$

$$Z(E) = \frac{4\pi}{h^3} (2m)^2 \frac{2\pi^2}{h^3}$$

Therefore the number of energy states in the energy interval E and E+dE are

$$Z(E)dE = \frac{4\pi}{h^3} (2m)^{\frac{3}{2}} E_f^{\frac{1}{2}} dE$$





Important questions

- 1. a. Explain the salient features of classical free electron theory
 - b. On the basis of classical free electron theory, derive the expressions for i) drift Velocity, ii) current density iii) mobility?
 - c. What are drawbacks of classical free electron theory of materials?
- 2. a. Explain Fermi-Dirac distribution for electrons in a metal. Discuss its variation with temperature?
 - b. Explain the terms 'Mean free path' 'Relaxation time' and 'Drift velocity' of an electron in a metal?
 - c. Discuss the origin of electrical resistance in metals?
- 3. a. Derive the expression for electrical conductivity on the basis of quantum free electron theory?
 - b. Explain i) Fermi energy?
 - c. Evaluate the Fermi function for an energy KT above Fermi energy?