

SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution)
Coimbatore – 35

DEPARTMENT OF MATHEMATICS UNIT - IV INTERPOLATION, NUMERICAL DIFFERENTIATION & INTEGRATION

NUMERICAL ENTEGRATION BY TRAPEZOLDAL

TRAPEZOIDAL RULE:

$$\int_{x_0}^{x_n} y \, dx = \frac{h}{2} \left[(y_0 + y_n) + 2 (y_1 + y_2 + \dots + y_{n-1}) \right]$$

$$= \frac{h}{2} \left[A + 2B \right]$$

where A = Sum of the first & last ordinates

B = Sum of the remaining ordinates.

Ousing trapezoidal seule, evaluate of dn taking 8 intervals.

Here
$$f_{1} = \frac{b-q}{n}$$
 where $a = -1$, $b = 1$, and $n = 8$

$$\Rightarrow f_{1} = \frac{2}{8} = 0.25$$



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UNIT – IV INTERPOLATION, NUMERICAL DIFFERENTIATION & INTEGRATION

$$9: -1 -0.75 -0.5 -0.25 0 0.25 0.5 0.75 1$$
 $9: 0.5 0.64 0.8 0.9412 1 0.9412 0.8 0.64 0.5$

Trapezoidal rule,

$$\int_{-1}^{1} \frac{1}{1+n^2} dn = \frac{1}{2} \left[(y_0 + y_0) + 2(y_0 + y_0) + 2(y_0 + y_0 + y_0) \right]$$

$$= \frac{1}{2} \left[sum q the = first and last ordinates + 2 sum of the remaining ordinates$$

$$= \frac{0.25}{2} \left[(0.5 + 0.5) + 2(0.64 + 0.8 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412 + 0.9412$$

Dividing the lange into 10 equal parts, Lind the value of Sinn dn by (1) Teapezoidal rule



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By Tropezoidal sude;

$$\int_{0}^{10} \frac{1}{8} \sin n \, dn = \frac{h}{2} \left[(y_0 + y_0) + 2(y_1 + y_2 + \dots + y_{10}) \right]$$

We have $h = \frac{11}{2} = 0 = \frac{\pi}{20}$

$$+ 0.5878 + 0.7071 + 0.8090 + 0.8910 + 0.9811 + 0.9877)$$

$$= \frac{\pi}{20} \cdot \frac{1}{2} \left[12.7062 \right]$$

$$= 0.9980$$