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#### DEPARTMENT OF MATHEMATICS UNIT - IV INTERPOLATION, NUMERICAL DIFFERENTIATION & INTEGRATION

LAGRANGIAN INTERPOLATION

Let 
$$y=f(x)$$
 be a function which takes the values  $y_0, y_1, y_2, \dots, y_n$  corresponding to  $x_0, x_1, x_2, \dots, x_n$ .

Then Lagrangian interpolation form is  $y = f(x)$ 

$$= (x - x_1)(x - x_2) \cdots (x - x_n) \quad y_0 + (x_0 - x_1)(x_0 - x_2) \cdots (x_n - x_n) \quad y_1 + (x_n - x_0)(x_n - x_2) \cdots (x_n - x_n) \quad y_1 + (x_n - x_0)(x_n - x_2) \cdots (x_n - x_n)$$

$$= (x - x_0)(x_1 - x_2) \cdots (x_n - x_n) \quad y_1 + (x_n - x_n) \quad y_2 + (x_n - x_n) \quad y_3 + (x_n - x_n) \quad y_4 + (x_n - x_n) \quad y_1 + (x_n - x_n) \quad y_2 + (x_n - x_n) \quad y_3 + (x_n - x_n) \quad y_4 + (x_n - x_n) \quad y_5 + (x_n - x_n) \quad y_6 + (x_$$

Find the polynomial fix) by using Lagrange's Tomula and hence find (3) for





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$$\Re : 0 \quad 1 \quad 2.35$$

$$\Re(x) : 2 \quad 3 \quad 12 \quad 147$$

$$Soln: \quad \Re_0 = 0 \quad ; \quad \Re_0 = 2$$

$$\Re_1 = 1 \quad ; \quad \Re_1 = 3$$

$$\Re_2 = 2 \quad ; \quad \Re_2 = 12$$

$$\Re_3 = 5 \quad ; \quad \Re_3 = 147$$

By Lagrange's Interpolation Jornala, we have

$$y = J(n) = \frac{(n-n_1)(n-n_2)(n-n_3)}{(n_0-n_1)(n_0-n_2)(n_0-n_3)} y_0 + \frac{(n-n_1)(n_0-n_2)(n_0-n_3)}{(n_0-n_3)} y_1 + \frac{(n-n_0)(n_1-n_2)(n_1-n_3)}{(n_0-n_0)(n_0-n_1)(n_0-n_3)} y_2 + \frac{(n-n_0)(n_0-n_1)(n_0-n_3)}{(n_0-n_0)(n_0-n_1)(n_0-n_2)} y_3$$





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$$= \frac{(\varkappa-1)(\varkappa-2)(\varkappa-5)}{(0-1)(0-2)(0-5)} (2) + \frac{(\varkappa-0)(\varkappa-2)(\varkappa-5)}{(1-0)(1-2)(1-5)} (3)$$

$$+ \frac{(\varkappa-0)(\varkappa-1)(\varkappa-5)}{(2-0)(2-1)(2-5)} (12) + \frac{(\varkappa-0)(\varkappa-1)(\varkappa-2)}{(5-0)(5-1)(5-2)} (147)$$

$$= (\varkappa-1)(\varkappa-2)(\varkappa-5) (2) + \varkappa(\varkappa-2)(\varkappa-5) (3)$$

$$= (\varkappa-1)(\varkappa-2)(\varkappa-5) (12) + \varkappa(\varkappa-1)(\varkappa-2) (147)$$

$$= \varkappa^3 + \varkappa^2 - \frac{6}{10} \qquad 60$$

$$y = \sqrt{(3)} = \frac{(3-1)(3-2)(3-5)}{(3-1)(3-2)(3-5)} (3) + \frac{3(3-1)(3-2)}{4} (3-2) (3-2) (147)$$

$$= \frac{8}{10} - \frac{18}{4} + 24 + \frac{147}{60} = 35$$





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Find the missing been in the following table using Lagrange's intespolation.

2 0 1 2 3 4 Soln: 31.

# Inverse Interpolation:

The process of finding a value of x for the corresponding value of y is called inverse interpolation.

Inverse interpolation formula is

$$x = (y-y_1)(y-y_2) - - - (y-y_n) x_0 + \frac{(y-y_1)(y-y_2) - - - (y-y_n)}{(y-y_1)(y-y_2) - - - (y-y_n)}$$

$$(y_1-y_0)(y_1-y_2)-\dots (y_1-y_n)$$
  $(y_1-y_0)(y_1-y_2)-\dots (y_1-y_n)$ 





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) Find the age corresponding to the annuaty value 13.6 yeven the table

Age (x): 30 35 40 45 50 Annuity valuely): 15.9 14.9 14.1 13.3 12.5

 $\begin{array}{c} 3001 \\ \chi = (y-y_1) * (y-y_2)(y-y_3)(y-y_4) \\ \hline (y_0-y_1)(y_0-y_2)(y_0-y_3)(y_0-y_4) \\ \hline (y_0-y_0)(y-y_1)(y-y_2)(y_1-y_4) \\ \hline (y_0-y_0)(y_1-y_2)(y_1-y_2)(y_1-y_4) \\ \hline (y_2-y_0)(y_2-y_1)(y_2-y_3)(y_2-y_4) \\ \hline (y_2-y_0)(y_2-y_1)(y_2-y_2)(y_1-y_4) \\ \hline (y_1-y_0)(y_2-y_1)(y_2-y_2)(y_2-y_4) \\ \hline (y_1-y_0)(y_2-y_1)(y_2-y_2)(y_2-y_4) \\ \hline (y_1-y_0)(y_2-y_1)(y_1-y_2)(y_1-y_2) \\ \hline (y_2-y_0)(y_2-y_1)(y_2-y_2)(y_2-y_4) \\ \hline \end{array}$ 





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$$= \frac{(13.6 - 14.9)(13.6 - 14.1)(13.6 - 13.3)(13.6 - 12.5)}{(15.9 - 14.9)(15.9 - 14.1)(15.9 - 14.1)(15.9 - 12.5)} \times 30 + \frac{(13.6 - 14.9)(13.6 - 14.1)(13.6 - 13.3)(13.6 - 12.5)}{(14.9 - 15.9)(14.9 - 14.1)(14.9 - 13.3)(13.6 - 12.5)} \times 35 + \frac{(13.6 - 15.9)(13.6 - 14.9)(13.6 - 13.3)(13.6 - 12.5)}{(14.1 - 15.9)(14.1 - 14.9)(14.1 - 13.3)(13.6 - 12.5)} \times 40 + \frac{(13.6 - 15.9)(13.6 - 14.9)(13.6 - 14.1)(13.6 - 12.5)}{(13.3 - 15.9)(13.6 - 14.9)(13.6 - 14.1)(13.3 - 12.5)} \times 45 + \frac{(13.6 - 15.9)(13.6 - 14.9)(13.6 - 14.1)(13.6 - 13.3)}{(13.5 - 15.9)(13.6 - 14.9)(13.6 - 14.1)(13.6 - 13.3)} \times 50$$