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#### **DEPARTMENT OF MATHEMATICS** UNIT - IV INTERPOLATION, NUMERICAL DIFFERENTLATION & **INTEGRATION**

DERIVATIVES FROM DIFFERENCE TABLES - DIVIDED DIFFERENCE  
AND FINITE DIFFERENCES:  

$$\frac{1}{75} \left[ \Delta y_0 + \frac{2u-1}{2!} \Delta^2 y_0 + \frac{3u^2 - 6u + 2}{3!} \Delta^3 y_0 + \frac{2u^2}{3!} \Delta^2 y_0 + \frac{3u^2 - 6u + 2}{3!} \Delta^3 y_0 + \frac{2u^2}{4!} + \frac{2u - 6}{4!} \Delta^4 y_0 + \frac{2u - 6}{4!} \right]$$
putting  $u = \chi_0$ , then  $u = 0$  and above eqn. Leduces  
he  
 $\left(\frac{dy}{du}\right)_{\chi=\chi_0} = \frac{1}{75} \left[ \Delta y_0 + \frac{1}{2} \Delta^2 y_0 + \frac{1}{3} \Delta^3 y_0 + \Delta^4 y_0 + \frac{1}{5} \Delta_5^3 \right]$ 

$$\frac{d^2y}{dx^2} = \frac{1}{72} \left[ \Delta^2 y_0 + \frac{6u - 6}{3!} \Delta^3 y_0 + \frac{12}{3!} \Delta^4 y_0 + \frac{2}{5} \Delta_5^3 \right]$$
 $\left(\frac{d^2y}{du^2}\right)_{\chi=\chi_0} = \frac{1}{72} \left[ \Delta^2 y_0 + -\Delta^2 y_0 + \frac{11}{12} \Delta^4 y_0 + \frac{5}{5} \Delta_5^3 \right]$ 



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$$\begin{aligned} \frac{d^{3}y}{dx^{3}} &= \frac{1}{h^{3}} \left[ \frac{6}{3!} \Delta^{3}y_{0} + \frac{24u-36}{4!} \Delta^{4}y_{0} + \cdots \right] \\ \frac{d^{3}y}{dx^{2}}_{n=\lambda_{0}} &= \frac{1}{h^{3}} \left[ \Delta^{3}y_{0} - \frac{3}{2} \Delta^{4}y_{0} + \frac{7}{4}\Delta^{5}y_{0} \right] \\ \frac{Newton's}{dx^{2}}_{n=\lambda_{0}} &= \frac{1}{h^{3}} \left[ \nabla^{3}y_{0} - \frac{3}{2} \Delta^{4}y_{0} + \frac{7}{4}\Delta^{5}y_{0} \right] \\ \frac{Newton's}{dx^{2}}_{n=\lambda_{0}} &= \frac{1}{h} \left[ \nabla^{3}y_{0} + \frac{2u+1}{2!} \nabla^{2}y_{0} + \frac{3u^{2}+6u+2}{3!} \nabla^{3}y_{0} + \frac{1}{3!} \nabla^{3}y_{0} + \frac{4u^{3}+18u^{2}+22u+6}{3!} \nabla^{3}y_{0} + \frac{1}{4!} \nabla^{4}y_{0} + \cdots \right] \\ \frac{dy}{dx^{2}} &= \frac{1}{h} \left[ \nabla^{2}y_{0} + \frac{1}{2!} \nabla^{2}y_{0} + \frac{1}{2!} \nabla^{2}y_{0} + \frac{1}{3!} \nabla^{3}y_{0} + \frac{1}{4!} \nabla^{4}y_{0} + \cdots \right] \\ \frac{d^{2}y}{dx^{2}} &= \frac{1}{h^{2}} \left[ \nabla^{2}y_{0} + \frac{6u+6}{3!} \nabla^{3}y_{0} + \frac{1}{2!} \nabla^{2}y_{0} + \frac{1}{2!} \nabla^{4}y_{0} + \cdots \right] \end{aligned}$$



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 $\begin{pmatrix} \frac{d^2 y}{da^2} \end{pmatrix} = \frac{1}{h^2} \left[ \nabla^2 y_{n+1} \nabla^3 y_{n+1} \frac{11}{12} \nabla^4 y_{n+1} \right]$  $\frac{d^{3}y}{dn^{3}} = \frac{1}{h^{2}} \left[ \frac{6}{3!} \nabla^{3} y_{n+1} \frac{244+36}{4!} \nabla^{4} y_{n+1} \cdots \right]$  $\left(\frac{d^{3}y}{d^{3}}\right)^{2} = \frac{1}{h^{3}} \left[\nabla^{3}y_{n} + \frac{3}{2}\nabla^{4}y_{n} + \frac{1}{4}\nabla^{2}y_{n}\right]$ 



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1) Find -1'(3) and -1"(3) for the following data: 2:3.03.23.43.63.8 4.0 7(2): -14 -10.032 -5.296 -0.256 6.672 14  $\chi$   $\gamma$   $\Delta y$   $\Delta^2 y$   $\Delta^3 y$   $\Delta^4 y$   $\Delta^5 y$ 0.4 4.328 4.0 14

By Newton's forward formula  $\left(\frac{dy}{dx}\right)_{x=x_0} = \left(\frac{dy}{dx}\right)_{u=0}$ 

= - [ [ Ayo - 1/2 Ayo + 1/3 A3yo - 1/4 A4yo + 1/5 ASyo - 1]



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Here 
$$h = 0.2$$
  

$$= \frac{1}{0.2} \left[ 3.968 - \frac{1}{2} \left( 0.768 \right) + \frac{1}{3} \left( -0.464 \right) - \frac{1}{4} \left( 2.048 \right) + \frac{1}{5} \left( -5.12 \right) \right]$$

$$= \frac{1}{0.2} \left[ 3.968 - 0.384 - 0.1547 - 0.512 - 1.024 \right]$$

$$= \frac{1}{0.2} \left[ 1.8933 \right]$$

$$= 9.4665$$

$$\left( \frac{d^{2}y}{dn^{2}} \right)_{x = x_{0}} = \frac{1}{52} \left[ \Delta^{2}y_{0} - \Delta^{3}y_{0} + \frac{11}{12} \Delta^{4}y_{0} - \frac{5}{6} \Delta^{5}y_{0} + \cdots \right]$$

$$= \frac{1}{(0.2)^{2}} \left[ 0.768 - \left( -0.464 \right) + \frac{11}{12} \left( 2.048 \right) - \frac{5}{6} \left( -5.12 \right) \right]$$

$$= \frac{1}{0.04} \left[ 0.768 + 0.4664 + 1.8773 + 4.267 \right]$$

$$= \frac{1}{0.04} \left[ 7.3763 \right] = 184.49757 - 36.8765$$

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