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DEPARTMENT OF MATHEMATICS

UNIT - Y NUMERICAL SOLUTION OF ORDINARY DIFFERENTIAL EQUATIONS

FOURTH ORDER RUNGE KUTTA METHOD FOR SOLVING FIRST AND SECOND ORDER EQUATIONS! SECOND ORDER RK METHOD : Pas 131.20 01 11 21 the initial values of (a, y) for the differential eqn $\frac{dy}{dx} = J(x, y)$ then the first increment in y namely sy is calculated from the formula k, = h2(x,y) $k_2 = h_{\mathcal{F}} \int [n + \frac{h}{2}, y + \frac{k_1}{2}]$ Now y(n+h) = y(n)+ Ay (4) y1= y0+ Ay THIRD ORDER RK METHOD : 1020 C - (C A) P $K_i = h_i(n, y)$ $k_2 = h_8 [n + \frac{h}{2}, y + \frac{k_1}{2}]$







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 $K_3 = h_1 [n+h, y+2k_2-k_1]$ $\Delta y = \frac{1}{6} \left[k_1 + 4 k_2 + k_3 \right]$ Now YI= Yot AY FOURTH ORDER RK METHOD: k = h f(n, y)k1 = AZ [n+ + y + + -] $k_3 = h_{2} \left[n + \frac{h_{2}}{2}, y + \frac{k_{2}}{2} \right]$ $k_4 = h_{2} \left[n + h, y + k_{3} \right]$ Dy = 1/6 [k1+2k2+2k3+kg7 Now YI = Yot Ay () Griven dy = 23+y, yco)=2, Compute yco.2), yco.4)& yco.6) by RK method & Jourth order.



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Now Rinnethod for
$$(y_{1}, y_{1})$$

 $k_{1} = \frac{\hbar}{4}(y_{1}, y_{1}) = 0.4902$.
 $k_{2} = \frac{\hbar}{3}[y_{1} + \frac{\hbar}{2}, y_{1} + \frac{k_{1}}{2}] = 0.5430$
 $k_{3} = \frac{\hbar}{3}[x_{1} + \frac{\hbar}{2}, y_{1} + \frac{k_{2}}{2}] = 0.5483$
 $k_{4} = \frac{\hbar}{3}[x_{1} + \frac{\hbar}{3}, y_{1} + k_{3}] = 0.6111$
 $\Delta y = 0.5473$.
 $y_{2} = y_{1} + \Delta y$
 $= 2.4432 + 0.5473$
 $= 2.9905$

Now KK niethod for (2, 42) where 22=0.4, 42 = 2,9905



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