



(An Autonomous Institution) Coimbatore - 35

#### DEPARTMENT OF MATHEMATICS

#### UNIT -Y NUMERICAL SOLUTION OF ORDINARY DIFFERENTIAL EQUATIONS

# MILNE'S PREDICTOR AND CORRECTOR METHODS

## FORMULAS:

Solve y'=n-y², 0≤n≤1, y(0)=0, y(0.2)=0.02, y(0.4)=0.0795 y(0.6)=0.1762 by Milne's method to find y(0.8) and y(1).

$$\frac{\text{Soln:}}{\text{Gln:}} \text{Gln:} \quad \chi_0 = 0 \quad \Rightarrow \quad \chi_0 = 0$$

$$\lambda_1 = 0.2 \Rightarrow y_1 = 0.02$$

$$\chi_{3} = 0.4 \rightarrow y_{2} = 0.0795$$
 $\chi_{3} = 0.6 \rightarrow y_{3} = 0.1762$ 

$$24 = 0.8 \Rightarrow -94 = ? + 64 = 0 = 0$$

$$25 = 1 \Rightarrow 95 = ?$$





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WKT Milne's predictor formula is

Ynt1, 
$$P = y_{n-3} + \frac{4h}{3} \left[ 2y'_{n-2} - y'_{n-1} + 2y'_{n} \right]$$
 $y_{4}, p = y_{0} + \frac{4h}{3} \left[ 2y'_{1} - y'_{2} + 2y'_{3} \right]$ 

G/n' 
$$y' = x - y^2$$
  
 $y_1' = x_1 - y_1^2 = 0.2 - (0.02)^2 = 0.1996$   
 $y_2' = x_2 - y_2^2 = 0.4 - (0.0795)^2 = 0.3937$   
 $y_3' = x_3 - y_3^2 = 0.6 - (0.1762)^2 = 0.5690$ 

$$y_{4,p} = 0 + 4(0.2) [2 \times 0.1996 - 0.3937 + 2 \times 0.5690] \\
 = 0.3049$$

$$y_4' = \alpha_4 - y_4^2 = 0.8 - (0.3049)^2 = 0.707$$





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$$y_{4,c} = y_{2} + \frac{h}{3} [y_{2} + 4y_{3} + y_{4}]$$

$$= 0.0795 + \frac{0.2}{3} [0.3937 + 4 \times 0.5690 + 0.707]$$

$$= 0.3046$$
: Connected value  $q$   $y$  at  $x = 0.8$  is  $0.3046$ .

To find  $y(i)$ :
$$y_{5,p} = y_{1} + \frac{4h}{3} [2y_{2} - y_{3} + 2y_{4}]$$

$$= 0.02 + 4 \times \frac{0.2}{3} [2 \times 0.3937 - 0.5690 + 2 \times 0.707)$$

$$= 0.4553$$

$$y_{5}^{2} = x_{5} - y_{5}^{2} = 1 - (0.4553)^{2} = 0.7327$$

$$y_{5,c} = y_{3} + \frac{h}{3} [y_{3} + 4y_{4} + y_{5}]$$

$$= 0.1762 + \frac{0.2}{3} [0.569 + 4 \times 707 + 0.7327]$$

$$= 0.4515$$
: Connected value  $q$   $y$  at  $x = 1$  is  $0.4515$ .





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(1) ruing Milne's method find  $y(4.4) \cdot yn. 5ny + y^2 - z = 0$ yiven y(4) = 1, y(4.1) = 1.0049, y(4.2) = 1.0097 and y(4.3) = 1.0143.

Soln!  $y_{4,p} = 1.01897$ ;  $y_{4,c} = 1.01874$ (2) using Runge Kutta method celevelate y(0.1), y(0.2) and y(0.3) eyn that  $\frac{dy}{dn} = \frac{2ny}{1+x^2} = 1$ , y(0) = 0. Taking these values as starting values find y(0.4) by Milne's method  $\frac{80}{1}$ ? y(0.1) = 0.1006 y(0.2) = 0.2052 y(0.3) = 0.3176 y(0.4) = 0.4413