

SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution)
Approved by AICTE, New Delhi, Affiliated to Anna University, Chennai
Accredited by NAAC-UGC with 'A++' Grade (Cycle III) & Company (B.E - CSE, EEE, ECE, Mech & Company);

DEPARTMENT OF MATHEMATICS

COIMBATORE-641 035, TAMIL NADU

Conformal mapping:
1) Find the image of the following aregion under the translation $w = 1/z$
(i) half plane x > c when c > 0
(ii) the infinite strip + 2 y < 1/2 (iii) the infinite strip 0 < y < 1/2
Soln: 0 = 11 0 = 11
$x + iy = \frac{1}{u + iv} = \frac{1}{u + iv} \cdot \frac{u - iv}{u - iv}$
$x + iy = \frac{u - iv}{u^2 + v^2} = \frac{(u - i)^2}{u^2 + v^2} = \frac{(u - i)^2}{u^2 + v^2}$
$x = \frac{u}{u^2 + v^2}$, $y = \frac{-v}{u^2 + v^2}$
(i) Half plane x > c when c>o
$\frac{3}{4} \frac{1}{4} \frac{1}{4} = c$
$u = c (u^{2} + v^{2})$ $u = u^{2} + v^{2}$ $u = u^{2} + v^{2}$
$u^2 - u + v^2 = 0.$
$\left(u^{2} - \frac{u}{c} + \left(\frac{1}{ac}\right)^{2}\right) + v^{2} - \left(\frac{1}{ac}\right)^{2} = 0 \qquad 2ab = \frac{u}{c}$ $(u - \frac{1}{ac})^{2} + v^{2} - \left(\frac{1}{ac}\right)^{2} = 0 \qquad b = \frac{u}{ac}$
which is a circle with centre $(\frac{1}{2c}, 0)$ & $b = \frac{\sqrt{3c}}{2\sqrt{2c}}$
radius 1/2c. b=1





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DEPATMENT OF MATHEMATICS

(ii) the infinite strip
$$\frac{1}{4} = \frac{2y}{2} = \frac{1}{2}$$
 buil (i)

 $\frac{-v}{4} = \frac{1}{4}$ consists $\frac{1}{4} = \frac{1}{4} =$