

## SNS COLLEGE OF TECHNOLOGY (AN AUTONOMOUS INSTITUTION) COIMBATORE – 35



## **UNIT 3 PARTIAL DIFFERENTIALEQUATIONS**

Solutions of standard types of first order partial differential equations

Type-ii 
$$f(z_1p_1q)=0$$
.  
1. Solve:  $p(1+q)=qz\rightarrow0$   
Let  $u=x+ay$   
Huen  $p=dz$  and  $q=adz$   
 $0\rightarrow dz$   $(1+adz)=adz$   
 $1+adz=az$   
 $1+adz=az$   
 $adz=az-1$   
 $dz=az-1$   
 $du=az-1$   
 $du=az-1$ 



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Integrating, 
$$\int du = \int \frac{a}{az-1} dz$$
 $u = log(az-1) + log C$ 
 $x + ay = log (c(az-1))$ 

2) Solve  $I = I + p^2 + q^2$ 

Solve  $I = I + p^2 + q^2 \rightarrow 0$ 

Let  $u = x + ay \quad p = dz \quad q = adz$ 
 $0 \Rightarrow z^2 = I + \left(\frac{dz}{du}\right)^2 + \left(a \frac{dz}{du}\right)^2$ 
 $z^2 = I + \left(\frac{dz}{du}\right)^2 (I + a^2)$ 
 $z^2 - I = \left(\frac{dz}{du}\right)^2 (I + a^2)$ 

Integering on both sides

 $z - I = \frac{I}{I + a^2} (I + a^2)$ 
 $z - I = \frac{I}{I + a^2} (I + a^2)$ 

For this type, there  $z_0 = z_0$ 
 $z_0 - z_0 = z_0$ 

Given:  $z_0 - z_0 = z_0 - z_0$ 

Given:  $z_0 - z_0 = z_0 - z_0$ 
 $z_0 - z_0 = z_0$ 
 $z_0$