

SNSCOLLEGEOFTECHNOLOGY (AN AUTONOMOUS INSTITUTION) COIMBATORE - 35



UNIT 3 PARTIAL DIFFERENTIAL EQUATIONS Linear partial differential equations of second order with constant coefficients of homogeneous types

Linear PDE
$$\int_{1}^{2n^{N}} \cos^{N} \cos^$$

1|6



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UNIT 3 PARTIAL DIFFERENTIAL EQUATIONS

Linear partial differential equations of second order with constant coefficients of homogeneous types

Goreral solution is y=cF+PI RHS=0 (Z=CF) 1. Solve $(D^2 - 6DD' + AD'^2)z = 0$ Put D=m, D'=1 The auxillary equation 28, m2-6m+9=0 (m-3)(m-3) =0 m= 3,3 (equal) The solution is Z = CF= $\frac{1}{2}$, $(y+3z) + z = \frac{1}{2}(y+3z)$ $1 = \frac{1}{2} =$ The curvillary equation is, $m^2 = 5m + b = 0$ (m-3)(m-2)=0m=2/3CF = 7, (y+2x) + +2(y+3x) Replace $PI = \frac{1}{D^2 - 5DD' + bD'^2} e^{\pi ty}$ D-> a =1 = <u>|</u> x+y The solution is 2= CF+PI = == +1 (y+2x) + + 2(y+3x) + ==



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$$\begin{aligned} \mathbf{\hat{g}}_{1} | \mathbf{\hat{g}}^{H} \mathbf{\hat{g}} \mathbf{\hat{g}} \mathbf{\hat{g}} \mathbf{\hat{g}} \mathbf{\hat{g}} \mathbf{\hat{g}}^{H} \mathbf{\hat{g}} \mathbf{\hat{$$



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$$CF \Rightarrow f = f_{1}(y - \frac{1}{2}x) + f_{2}(y - 2x)$$

$$P_{1}(y) = F_{1}(y)$$

$$P_{2}(y) + f_{2}(y) + f_{2}(y) = g_{1}(y)$$

$$P_{1}(y) = f_{1}(y) = g_{1}(y) + f_{2}(y) = g_{1}(y)$$

$$P_{1}(y) = g_{1}(y) = g_{1}(y)$$

$$P_{2}(y) = g_{1}(y)$$

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$$P_{2}(y) = g_{1}(y)$$

$$P_{2}(y) = g_{2}(y)$$

$$P_{2}(y) = g_{2}($$

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UNIT 3 PARTIAL DIFFERENTIAL EQUATIONS

Linear partial differential equations of second order with constant coefficients of homogeneous types

$$FI_{2} = \frac{1}{gD^{2} - abb^{1} + b^{2}} e^{x+y} \Rightarrow D = 1, D' = 1$$

$$= \frac{1}{g(y)^{2} - g(y(y) + (y)^{2}} e^{x+y}$$

$$= e^{x+y}$$

$$\therefore The solution is Z = cF + PI$$

$$Z = \frac{1}{g(y+(\pm \pm \pm))} \pm \frac{1}{g(y+(\pm \pm \pm))} \pm \frac{1}{g} e^{3y} + e^{2t+y}$$

$$A \in is m^{2} - 3m + 2 = 0$$

$$(m - 2)(m - 1) = 0.$$

$$m = 1, m = 2$$

$$CF = B = Z = \frac{1}{g(y+x)} \pm \frac{1}{g(y+x)} \pm \frac{1}{g(y+2x)}$$

$$PI = \frac{1}{D^{2} - 3bb^{1} + 2b^{2}} e^{3x+2y}$$

$$= \frac{1}{(y)^{2} - 3(g(x) + 2(g))^{2}} e^{3x+2y}$$

$$= \frac{1}{g(y+x)} \pm \frac{1}{g(y+x)} \pm \frac{1}{g(y+2x)} - e^{3x+2y}$$

$$= \frac{1}{g(y+x)} \pm \frac{1}{g(y+x)} \pm \frac{1}{g(y+2x)} - e^{3x+2y}$$

$$FI = \frac{1}{g(y+x)} \pm \frac{1}{g(y+x)} \pm \frac{1}{g(y+2x)} - e^{3x+2y}$$

$$= \frac{1}{(m - 5)} (m + u) = 0 \quad m = 1, m = 5$$

$$\therefore CF = \frac{1}{3} = \frac{1}{g(y-4x)} \pm \frac{1}{g(y+5x)} \quad Deptofmathematics$$

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$$PI = \frac{1}{D^{2} - DD' - ROD'^{2}} e^{Sx + Y} \qquad D = 5 , D' = 1$$

$$= \frac{1}{(5)^{2} - (5(1) - 30(1))} e^{Sx + Y} = \frac{1}{2^{5} - 5 - 30} e^{Sx + Y}$$

$$= \frac{x}{RD - D'} e^{Sx + Y} = \frac{1}{2^{5} - 5 - 30} e^{Sx + Y}$$

$$= \frac{x}{RD - D'} e^{Sx + Y}$$

$$= \frac{x}{2(5) - 1} e^{Sx + Y}$$