



(An Autonomous Institution)
Coimbatore— 35

DEPARTMENT OF MATHEMATICS

UNIT-IV TESTING OF HYPOTHESIS

JEST OF SIGNIFICANCE OF LARGE SAMPLES:

JEST FOR BINGLE MENN:

Null Hypothesis, 110:
$$\mu$$
= μ 0

Test statistics, $z = \frac{5i - \mu}{\sigma/v_0}$ cor) $z = \frac{5i - \mu}{s/v_0}$

1) A sample of goo members is Jourd to have a moun of 3.4 cm and s.D. 2.61 cms. Is the sample from a clarge population of mean 3.25 cm and 8.D. 2.61 cms. If the population a mean 3.25 cm and 8.D. 2.61 cms. If the population a normal and Its mean is untended find the 95% confedential (Jeducial) limits of true mean.

Soln: Given: n = 900, n = 3.4, H = 3.25, 0 = 2.61

Sleps: Formulating Ho & Hi: Ho: H= 3.25 (+mo tailed text)

Step 2: Level of rightficance = 5% = 0.05

slep 3: Test statestic, z = 12-4

=1.724

step 4: critical value at 5% is Zx=1.96.

steps: conclusion: since 121=1.724 < 1.96=24,
Ho & accepted at 54. Level of significance.

.. The sample & taken Jeon population where mean 3.25 cm.





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Outpotation showed their average to be 42.8 years with a s.D. g 6.89 years. Fest The hypothesis Ho: H= 40 . HI: H>40 at a: c.cl Level & significons Sofn! yiven: n= 200, n= 42.8, H=40, V= 689 step 1: Formulating Ho and H ,: H1: 4>40 (one fail test - light) steps: Level a significance, x= 0.01. 3 laps: Test statistic, 7 = 51- H estep 4: Critical value at 1.1. (one tailed - sight) B Z = 2.33 step 5: Conclusion: since 121=5.444 > 2.33=2, : Ho & rejected at 14 Level 9 significance . The hypothesis, M, : H>40 is accepted.





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The mean height of college students in a city are normally distributed with 3.D. 6 cms. A sample of 100 students has mean height of 158 cms. Test the hypothesis that the mean height of college students in the city 160 cms. Also obtain 99% confidence limits for the true mean.

Solo: Given: n=100, \$\overline{\pi} = 158, \mu=160, \sigma=6

Step 1: Formulating to and \$H\$;

Ho: \$\mu=160

H1: \$\mu=160\$ (two tailed test)

Step 2 : Level q significance, α=1/4

step 3 : Test statistic, × = 1/4

- 1/50

- 158-160

- 6/√100

- 3.33

Step 4: Ceitical value at 17. (two side test) is

steps: Condusion; Source 121=3.33 > 2.58=20 : Ho is rejected at 1% Level of significance. ... The mean height of the cottage students in the city is 160 cms is not true.





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JEST FOR DIFFERENCE FOR TWO MEANS:

Null hypothesis:
$$H_0: H_1 = H_2$$

Test Statistic, $Z = \frac{\overline{\chi_1} - \overline{\chi_2}}{\sqrt{\overline{\eta_1}^2 + \overline{\eta_2}^2}}$

$$= \frac{\overline{\chi_1} - \overline{\chi_2}}{\sqrt{\overline{\eta_1}^2 + \overline{\eta_2}^2}}$$

$$= \frac{\overline{\chi_1} - \overline{\chi_2}}{\sqrt{\overline{\eta_1}^2 + \overline{\eta_2}^2}}$$

Lor) $Z = \frac{\overline{\chi_1} - \overline{\chi_2}}{\sqrt{\frac{S_1^2}{\eta_1} + \frac{S_2^2}{\eta_2}}}$

The means of two timple large samples of loco or! 2000 members are 67.5 inches and 68 inches resp. Can the samples be regarded as drawn from the same population of standard deviation of 25 inches. Test at 5% level of rightful cance (105)

30/n:
-given: n, = 1000, 7, = 67.5,

n2 = 2000, 72 = 68, 8 = = 2.5

step 1: Foundating Ho and H1:

Ho: \mu. = \mu = H2

H1: \mu, \neq \mu = (two tailed test)

Step 2: Level 2 significance, \alpha = 51/. = 0.05





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Slep 3: Test statistic,
$$z = \frac{\pi_1 - \pi_2}{\sqrt{n_1 + n_2}}$$

$$= \frac{67.5 - 68}{2.5 \sqrt{\frac{1}{1000} + \frac{1}{2000}}}$$

$$= -5.164$$

$$1z1 = 1 - 5.164$$

$$= 5.164$$
Step 4: cretical value, at 5% Ctro sided test)
is $z_x = 1.96$.

Step 5: Conclusion: $z = 5.164 > 1.96 = z_x$

$$\therefore \text{ Ho is righted at 5%. Los}$$

$$\therefore \text{ The samples cannot be regarded as deawn}$$

$$\Rightarrow \text{ The samples cannot be regarded as deawn}$$

$$\Rightarrow \text{ The samples cannot be regarded as deawn}$$

$$\Rightarrow \text{ The same population } z = 5.0.25 \text{ inches}$$

MA rimple sample of height of 6400 sailors has a mean of 67.85 inches and s.D. of 2.56 inches while a simple sample of heights of 1600 setolices has a mean of 68.55 inches and s.D. of 2.50 inches. Do the data, indicate that soldiers are on the average taller than sailors? use 51. Los.





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90/n: given: Shilors:n, = 6400, \$1, =67.85, 8, = 2.56 Soldier: no = 1600, 7/2 = 68.55, 50 = 2.52 Step 1: Farmulating Ho and H, Ho: H, = HQ. HI: MI < Me cone tailed test- Left) step 2: Los at 5% as x=0.05 step 3: Test statistic, Z = x1- x5 = 67.85-68-55 (2.56)2 + (2.52)2 6400 + (2.52)2 = -9.91 121=1-9.91) step 4: critical value at 5% (one tail test) B Xx = 1.645 step 5: Conclusion: z= 9.91>1.645=zx .. Ho is rejected at 5% & Los .. The data indicates that soldiers are on the average taller than sailors.

mean of 170 cm & 3.D. of 64 cm, while a simple sample of theights of 1600 Ancelcans has a mean of 172 cm & 3.D. of 6.3 cm. No the clata indicate that Americans are the ary. talks than the coulish men ? [z = 11.32, H, < H2, American are tolks than English men]