



(An Autonomous Institution)
Coimbatore— 35

DEPARTMENT OF MATHEMATICS

UNIT-IV TESTING OF HYPOTHESIS

DEST OF SIGNIFICENCE OF SMALL BAMPLES!

VARIANCE RATIO TEST (OT) F- Test JOR EQUALITY OF YARIAN

Null Thypothesis: Ho: \(\nabla_1^2 = \nabla_2^2\)

Test startics: $F = \frac{8^2}{5^2}$ where $5^2 > 5^2$.

where $S_1^2 = \frac{n_1 s_1^2}{n_{i-1}}$ of $S_1^2 = \frac{5(\alpha_1 - \overline{\lambda_1})^2}{n_{i-1}}$ &

 $S_2^2 = \frac{n_2 S_2^2}{n_2 - 1}$ of $S_2^2 = \frac{5(n_2 - \bar{n}_2)^2}{n_2 - 1}$

Deglee & Freedom: (Ve, V2)

where 1: (n,-1), 12=(n,-1)

Note 1:- F Greater than zone always.

Note 2: - Suppose S_2^2 greater than S_1^2 , then $F = \frac{S_2^2}{S_1^2}$ with degree of greadom, $V_1 = n_2 - 1$, $V_2 = n_1 - 1$

From the same population.





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) two landom sample 9 11 and 9 items show that the sample standard deviations 9 their weights as 0.8 & 0.5 number vely. Assuming that the weight distributions are normal, test the hypothesis that the true variances are equal, against the alternative hypothesis that they are not Sign!
Given · · n, = 11 , 31 = 0.8

n2 = 9 , 82 = 0.5 $B_1^2 = \frac{0.61^2}{0.1-1} = \frac{11(0.8)^2}{11-1} = 0.404$ 822 = 1 862 = 9(0.5)2 = 0.2812 step 1 > Formulate Ho & H, Ho: 5, = 52 ower to the popular H1: 52 + 52 stip 2 .- > Los at x = 5 y. slip 3 > Test Statistic, F = 812 = 0.704 = 2.5 stip 4 -> Degrees & Freedom (1,12) (n.-1, n2-1) #2 Ceincalvalue, Ftab: Fx = 3.35 Step 5 -> conclusion: F=2.5 < 3.35 = Fx :. Ho is accepted at x:5%.





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) Two exposors complex ways the adjourned levelle.
) Two eardon samples yave the following levels: Sample size samplemean sum q squeezs q deviation seem the means.
Sample size samplemean sum quigues que un sum que sum sum sum que sum
1 12 14 108
2 10 15 90
2 10 15
Yest whether The samples came from the same
population.
golin:
Given:
$n_1 = 12$, $x_1 = 14$, $\leq (x_1 - \overline{x}_1)^2 = 108$
h
no = 10, no = 15 & (no- 70)2 = 90
$3_1^2 = \frac{\sum (\gamma_1 - \overline{\gamma_1})^2}{n_1 - 1} = \frac{108}{12 - 1} = 9.818$
$n_{i-1} = \frac{1}{12-1} = 9.818$
$S^{2} = S(n_{1} - \overline{n}_{1})^{2}$
$S_{2}^{2} = \frac{5(n_{2} - \overline{n}_{2})^{2}}{n_{2-1}} = \frac{90}{10-1} = 10$
3,2 < S22
Step 1: Formulati Ho and Hi:
Ho: 0,2 = 0,2
H1: V12 + 022
stip 2: Los at a = 5%.
Step 3: Test statistics, $F = \frac{S_a^2}{S_{12}} = \frac{10}{9.818}$
F = 1.018





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critical value, Fx = 2.90

Sty & : Conclusion:

.. Ho is accepted at 5% Los.

(11) 4 - Test:

glip 3: Test Statistic,
$$l = \frac{\pi_1 - \pi_2}{S \sqrt{n}}$$
, $\forall \frac{\pi_1}{n} = \frac{\pi_2}{N_1}$

Here $n_1 = 12$, $n_2 = 10$; $\overline{\lambda}_1 = 14$, $\overline{\lambda}_2 = 15$

Now $S^2 = \frac{2(\pi_1 - \overline{\lambda}_1)^2 + 2(\pi_2 - \overline{\lambda}_2)^2}{n_1 + n_2 - 2}$

$$= \frac{108 + 90}{12 + 10 - 2} = 9.9$$

$$S = 3.14$$





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$$S_1^2 = \frac{\sum (n_1 - \overline{n}_1)^2}{n_1 - 1} = \frac{\mu_1 \cdot 5}{7} = 5.9286$$

$$S_2^2 = \frac{\sum (n_2 - \overline{n}_2)^2}{n_2 - 1} = \frac{101.7143}{6} = 16.9524$$

$$S_1^2 < S_2^2.$$

$$Step 1: \text{ formulate Ho & Hi:}$$

$$Ho: \nabla_1^2 = \nabla_2^2$$

$$H_1: \nabla_1^2 \neq G_2^2$$

$$Step 2: \text{ Los at } S = 1 \text{ J.}$$

$$Step 3: \text{ Test statistic, } F = \frac{S_2^2}{S_1^2}.$$

$$= \frac{16.9524}{5.9286} = 2.86$$

$$Step 4: \text{ Respects } q \text{ freedom:} (v_1, v_2)$$

$$= (n_2 - 1, n_1 - 1)$$

$$= (6, 4)$$

$$Step 5: \text{ Conclusion, } F = 2.86 < 7.19 = Fx$$

$$\therefore \text{ Ho & accepted at Ho at } 1 \text{ J. Los.}$$