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DEPARTMENTOFMATHEMATICS UNIT-IV INTERPOLATION, NUMERICAL DIFFERENTIATION

INTEGRATION

LAGRANGIAN INTERPOLATION

Let y=f(x) be a function which takes the values yo, y, y2,, yn corresponding Then Lagrangean interpolation form is to 26, 21, 26, 20 y = f(x)Allerance From Gauss Entraded $(\mathcal{X}-\mathcal{X}_{0})(\mathcal{X}-\mathcal{X}_{2})\cdots(\mathcal{X}-\mathcal{X}_{n})$ $(\mathcal{X}-\mathcal{X}_{0})(\mathcal{X}-\mathcal{X}_{2})\cdots(\mathcal{X}-\mathcal{X}_{n})$ $(\varkappa_1 - \varkappa_0)(\varkappa_1 - \varkappa_2) - \cdots - (\varkappa_1 - \varkappa_n)$ Rest superinting (needed into need a most su $\frac{(\chi - \chi_0)(\chi - \chi_1) \cdots (\chi - \chi_{n-1})}{(\chi_{n} - \chi_0)(\chi_{n} - \chi_1) \cdots (\chi_{n-1})} y_n$

Find the polynomial fix) by using Lagrange's Jormula and hence find - (3) Jos 23MAT204-STATISTICS&NUMERICALMETHODS Dr.G.Nandini//AP/MATHS/SNSCT PAGE-10F6



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By Lagrange's Interpolation formula, we have

$$y = -\frac{1}{2}(n) = \frac{(n - n_1)(n - n_2)(n - n_3)}{(n_0 - n_1)(n_0 - n_2)(n_0 - n_3)} y_0 + \frac{(n - n_0)(n_0 - n_2)(n_0 - n_3)}{(n_1 - n_0)(n_1 - n_2)(n_1 - n_3)} y_1 + \frac{(n - n_0)(n_1 - n_2)(n_1 - n_3)}{(n_2 - n_0)(n_2 - n_1)(n_1 - n_3)} y_2 + \frac{(n - n_0)(n_1 - n_1)(n_1 - n_2)}{(n_3 - n_0)(n_1 - n_1)(n_1 - n_2)} y_3$$

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$$= \frac{(\chi-1)(\chi-2)(\chi-5)}{(0-1)(0-2)(0-5)} (2) + \frac{(\eta-6)(\chi-2)(\eta-5)}{(1-6)(1-2)(1-5)}^{(3)}$$

$$+ \frac{(\eta-6)(\eta-1)(\eta-5)}{(2-6)(2-1)(2-5)} (12) + \frac{(\eta-6)(\chi-1)(\eta-2)}{(5-6)(5-1)(5-2)} (147)$$

$$= \frac{(\eta-1)(\eta-2)(\eta-5)}{-10} (2) + \frac{\chi(\eta-2)(\eta-5)}{4} (3)$$

$$+ \frac{\chi(\eta-1)(\eta-2)(\eta-5)}{-10} (12) + \frac{\chi(\eta-1)(\eta-2)}{66} (147)$$

$$= \frac{\eta^{2}+\eta^{2}-\eta^{2}}{-6} (12) + \frac{3(3-2)(3-5)}{4} (3) + \frac{3(3-1)(3-2)}{4} (3) + \frac{3(3-1)(3-2)}{4} (3) + \frac{3(3-1)(3-2)}{4} (147)$$

$$= \frac{8}{10} - \frac{18}{4} + \frac{24}{60} + \frac{147}{60} = 35$$

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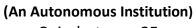
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Find the missing been in the following table using Lagrange's intespolation. 22 3 4 10 soln: 31 4 1-3 9 2-81 Inverse Interpolation : The process of finding a value of x for the corresponding value of y is called inverse interpolation Inverse interpolation Jaimula is $x = (y-y_1)(y-y_2)---(y-y_n) x_0 +$ (y-y) (yo-y2) - - (yo-yn) $(y_{1}-y_{0})(y_{1}-y_{2}) - - (y_{1}-y_{n})$ $(y_{1}-y_{0})(y_{1}-y_{2}) - - (y_{1}-y_{n})$ $(y - y_0)(y - y_1) - - \cdot (y - y_{n-1})$ (yn-yo) (yn-y1) ---- (yn-yn-1)







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UNIT-IV INTERPOLATION, NUMERICAL DIFFERENTIATION & **INTEGRATION**

) Find the age corresponding to the annualty value 13.6 yeven the table Age (x): 30 35 40 45 50 Annuity value(y): 15.9 14.9 14.1 13.3 12.5 $\frac{30}{(y_0-y_1)} \approx (y-y_2)(y-y_3)(y-y_4)}{(y_0-y_1)(y_0-y_2)(y_0-y_3)(y_0-y_4)} \approx (y_0-y_1)(y_0-y_2)(y_0-y_3)(y_0-y_4)}$ $(y - y_0)(y - y_1)(y - y_3)(y - y_4)$ $(y_{1} - y_{1})(y_{1} - y_{2})(y_{1} - y_{2})(y_{1} - y_{4})$ $\frac{(y_{-}y_{0})(y_{-}y_{1})(y_{-}y_{3})(y_{-}y_{4})}{(y_{2}-y_{0})(y_{2}-y_{1})(y_{2}-y_{3})(y_{2}-y_{4})} \chi_{2}^{*} +$ $(y - y_0)(y - y_1)(y - y_2)(y - y_4) = x_3 +$ $(y_{\mathbf{H}}-y_{0})(y_{3}-y_{1})(y_{3}-y_{2})(y_{3}-y_{4})$ $\frac{(y_{-},y_{0})(y_{-},y_{1})(y_{-},y_{2})(y_{-},y_{3})}{(y_{4}-y_{0})(y_{4}-y_{1})(y_{4}-y_{2})(y_{4}-y_{3})} \xrightarrow{\chi_{4}}$







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= (13.6 - 14.9)(13.6 - 14.1)(13.6 - 13.3)(13.6 - 12.5)(15-9-14-9) (15-9-14-1) (15-9-14-1) (15-9-12-5) × 30 + $\frac{(13.6 - 15.9)(13.6 - 14.1)(13.6 - 13.3)(13.6 - 12.5)}{(14.9 - 15.9)(14.9 - 14.1)(14.9 - 13.3)(14.9 - 12.5)} \times 357$ $\frac{(13.6-15.9)(13.6-14.9)(13.6-13.3)(13.6-12.5)}{(14.1-12.5)} \times 407$ (13.6 - 15.9) (13.6 - 14.9) (13.6 - 14.1) (13.6 - 12.5)(13.3 - 15.9) (13.3 - 14.9) (13.3 - 14.1) (13.3 - 12.5)x 45+ $\frac{(13.6 - 15.9)(13.6 - 14.9)(13.6 - 14.1)(13.6 - 13.3)}{(12.5 - 15.9)(12.5 - 14.9)(12.5 - 14.1)(12.5 - 14.3)} \times 50$ = 431-600 == (1-05) = = (100, 100) = (100, 100) 000

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