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DEPARTMENT OF MATHEMATICS

UNIT-IV INTERPOLATION, NUMERICAL DIFFERENTIATION & INTEGRATION

NEWTON'S FORWARD AND BACKWARD DIFFERENCE FORMULA

(EQUAL [NTERVALS)

Let the function y = y(x) takes the values y_0, y_1, \dots, y_n at the points x_0, x_1, \dots, x_n where $x_i = x_0 + ih$.

Then Newton's Forward interpolation polynomial is given by $y(x) = P_0(x) = \frac{1}{2}(x)$

u(u-1)(u-2)...(u-(n-1)) $\Delta^n y_0$

where $u = \frac{\chi - \chi_0}{h}$; the difference between two enternals.





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Then Newton's Backward interpolation polynomial is given by

$$y(x) = P_n(x) = \frac{1}{2}(x)$$

$$= y_{n} + \frac{u}{1!} \nabla y_{n} + \frac{u(u+1)}{2!} \nabla^{2}y_{n} + \frac{u(u+1)(u+2)}{3!} \nabla^{3}y_{n}$$

$$+ \dots + u(u+1)(u+2) \dots (u+(n-1)) \nabla^{3}y_{n}$$

where u = 21-21

First order:

Ay = 42-41

Be cond order: horns

Third order.

$$\Delta^3 y_0 = \Delta^2 y_1 - \Delta^2 y_0$$

Bacleward. First older.

$$\nabla y_n = y_n - y_{n-1}$$

$$\nabla y_{n-1} = y_{n-1} - y_{n-2}$$

$$\nabla^2 y_n = \nabla y_n - \nabla y_{n-1}$$

Third order:

$$\nabla^3 y_n = \nabla^2 y_n - \nabla^2 y_{n-1}$$





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Jornard Enterpolation:

Here
$$n_0 = 4$$
; $y_0 = 1$; $n_0 = 2$
 $n_0 = \frac{n_0 - 4}{2}$
 n_0





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$$y(x) = y_{n} + \frac{u}{1!} \nabla y_{n} + \frac{u(u+1)}{2!} \nabla^{2}y_{n} + u(u+1)(u+2) \nabla^{3}y_{n}$$

$$= 10 + \left(\frac{n-10}{2}\right)(2) + \left(\frac{n-10}{2}\right)\left(\frac{n-10}{2}+1\right)\left(-\frac{3}{2}\right) + \left(\frac{n-10}{2}+1\right)\left(\frac{n-10}{2}+1\right)\left(\frac{n-10}{2}+1\right)$$

$$\left(\frac{n+10}{2}\right)\left(\frac{n-10}{2}+1\right)\left(\frac{n-10}{2}+1\right)\left(\frac{n-10}{2}+1\right)$$