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DEPARTMENT OF MATHEMATICS

UNIT-IV INTERPOLATION, NUMERICAL DIFFERENTIATION & INTEGRATION

NEWTON'S FORWARD AND BACKWARD DIFFERENCE HORMULA

(EQUAL ENTERVALS)

Let the function y= \f(n) bakes the values yo you, you at the points no, x,.... In where xi = no+ ih.

Then Newton's Jorward interpolation polynomial is $y(x) = P_n(x) = f(x)$ ywen by

= yo+ u Ayo+ u(u-1) D2yo+ u(u-1) (u-2) A3yo+ 1 u(u-1) (u-2)...(u-(n-1)) Dnyo

where $u = \frac{n-n_0}{h}$; the difference between two Enterrals.





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Then Newton's Backward interpolation polynomical is given by
$$y(x) = P_n(x) = \frac{1}{2}(x)$$

$$= y_{n} + \frac{u}{1!} \nabla y_{n} + \frac{u(u+1)}{2!} \nabla^{2}y_{n} + \frac{u(u+1)(u+2)}{3!} \nabla^{3}y_{n}$$

$$+ \dots + u(u+1)(u+2) \dots (u+(n-1)) \nabla^{3}y_{n}$$

where u = 21-21

Forward Note:

First order:

130 = 4, - 40

Ay = 42-41

Be cond order: horns

1240 = Ay- Ayo

Third order.

1340 = 124, -1240

Bacleward. First older.

 $\nabla y_n = y_n - y_{n-1}$

 $\nabla^2 y_n = \nabla y_n - \nabla y_{n-1}$

Third order:

 $\nabla^3 y_n = \nabla^2 y_n - \nabla^2 y_n = \nabla^2$





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Jornard Enterpolation:

Here
$$n_0 = 4$$
; $y_0 = 1$; $n_1 = 2$.

 $u = \frac{n_1 - 4}{2}$
 $u = \frac{n_2 - 4}{2}$
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$$y(x) = y_{n} + \frac{u}{1!} \nabla y_{n} + \frac{u(u+1)}{2!} \nabla^{2}y_{n} + u(u+1)(u+2) \nabla^{3}y_{n}$$

$$= 10 + \left(\frac{n-10}{2}\right)(2) + \left(\frac{n-10}{2}\right)\left(\frac{n-10}{2}+1\right)\left(-\frac{3}{2}\right) + \left(\frac{n-10}{2}+1\right)\left(\frac{n-10}{2}+1\right)\left(\frac{n-10}{2}+1\right)$$

$$\left(\frac{n+10}{2}\right)\left(\frac{n-10}{2}+1\right)\left(\frac{n-10}{2}+1\right)\left(\frac{n-10}{2}+1\right)$$