



(An Autonomous Institution) Coimbatore 35

DEPARTMENT OF MATHEMATICS

UNIT-IV INTERPOLATION, NUMERICAL DIFFERENTIATION & **INTEGRATION**

NUMERICAL ENTEGRATION BY SIMPSONS 1/3

Simpson's
$$y_3$$
 Rule:

$$\int_{x_0}^{x_n} y \, dn = \frac{h}{3} \left[(y_0 + y_n) + 4 \left[y_1 + y_3 + \dots + y_{n-1} \right] + 2 \left[y_2 + y_4 + \dots + y_{n-2} \right] \right]$$

$$= \frac{h}{3} \left[A + 4 B + 2 C \right]$$

where A = Sum of the first & last-ordinalis B = Sum of the odd ordinates. c = Sum of the even ordinates.

cie) an even number of equal subinterrals.

Dividing the lange into 10 equal parts, Lind the value I sinn on by Simpsons 1/8 stude





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By Simpson's
$$1/3$$
 stude,

$$\int \frac{11/2}{5 \sin n} \, dn = \frac{h}{3} \left[(y_0 + y_{11}) + 4 (y_1 + y_3 + y_6 + y_7 + y_9) + 2 (y_2 + y_4 + y_6 + y_8 + y_{10}) \right]$$

$$= \frac{11}{20} \cdot \frac{1}{3} \left[(0+1) + 4 (3.1962) + 2 (2.669) \right]$$

$$= 1.0000$$

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Soln: Here
$$y(x) = \frac{1}{4n+5}$$

 $h = \frac{5-0}{10} = \frac{1}{2} = 0.5$

$$\int \frac{dn}{4n+8} = \frac{h}{3} \left[(y_0 + y_0) + 2(y_2 + y_4 + y_6 + \cdots) + \frac{h}{3} \right]$$

$$A(y_1 + y_3 + y_5 + \cdots)$$





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