



(An Autonomous Institution) Coimbatore 35

DEPARTMENT OF MATHEMATICS

UNIT-VNUMERICAL SOLUTION OF ORDINARY DIFFERENTIAL EQUATIONS

MILNE'S PREDICTOR AND CORRECTOR METHODS

FORMULAS:

Solve y'=n-y², 0≤n≤1, y(0)=0, y(0.2)=0.02, y(0.4)=0.0795 y(0.6)=0.1762 by Milne's method to find y(0.8) and y(1).

Soln:
$$y_0 = 0 \rightarrow y_0 = 0$$

$$\lambda_1 = 0.2 \Rightarrow y_1 = 0.02$$

$$\chi_{3} = 0.4 \rightarrow y_{2} = 0.0795$$
 $\chi_{3} = 0.6 \rightarrow y_{3} = 0.1762$

$$2\psi = 0.8 \Rightarrow -9\psi = ? + 60.07 = 0$$

$$2s = 1 \Rightarrow 9s = ?$$





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WKT Milne's predictor gormula is

Yn+1,
$$P = y_{n-3} + \frac{4h}{3} \left[2y'_{n-2} - y'_{n-1} + 2y'_{n} \right]$$
 $y_{4}, p = y_{0} + \frac{4h}{3} \left[2y'_{1} - y_{2}'_{1} + 2y'_{3} \right]$

G/n'
$$y' = x - y^2$$

 $y_1' = x_1 - y_1^2 = 0.2 - (0.02)^2 = 0.1996$
 $y_2' = x_2 - y_2^2 = 0.4 - (0.0795)^2 = 0.3937$
 $y_3' = x_3 - y_3^2 = 0.6 - (0.1762)^2 = 0.5690$

$$y_{4,p} = 0 + 4(0.2) [2 \times 0.1996 - 0.3937 + 2 \times 0.5690]$$

= 0.3049

$$y_4' = \alpha_4 - y_4^2 = 0.8 - (0.3049)^2 = 0.707$$





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$$y_{4,c} = y_{2} + \frac{h}{3} [y_{2}' + 4y_{3}' + y_{4}']$$

$$= 0.0795 + \frac{0.2}{3} [0.3937 + 4 \times 0.5690 + 0.707]$$

$$= 0.3046$$

$$: Connected value $g y \text{ at } n = 0.8 \text{ is } 0.3046.$

$$To find $y(i)$:
$$y_{5,p} = y_{1} + \frac{4h}{3} [2y_{2}' - y_{3}' + 2y_{4}']$$

$$= 0.02 + 4 \times \frac{0.2}{3} [2 \times 0.3937 - 0.5690 + 2 \times 0.707)$$

$$= 0.4553$$

$$y_{5}' = x_{5} - y_{5}^{2} = 1 - (0.4553)^{2} = 0.7327$$

$$y_{5,c} = y_{3} + \frac{h}{3} [y_{3}' + 4y_{4}' + y_{5}']$$

$$= 0.1762 + \frac{0.2}{3} [0.569 + 4 \times 707 + 0.7327]$$

$$= 0.4575$$

$$\therefore \text{ Connected value } q \text{ y at } n = 1 \text{ is } 0.4575.$$$$$$





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() rwing Milne's method find
$$y(4.4)$$
 yn. $5\pi y' + y^2 - 2 = 0$

yiven $y(4) = 1$, $y(4.1) = 1.0049$, $y(4.2) = 1.0097$ and

 $y(4.3) = 1.0143$.

Soln! $y_{4,p} = 1.01897$; $y_{4,c} = 1.01874$

(2) using Runge Kutta method calculate $y(0.1)$, $y(0.2)$ and $y(0.3)$ yn that $\frac{dy}{d\pi} = \frac{2\pi y}{1 + x^2} = 1$, $y(0) = 0$. Taking these values as starting values find $y(0.4)$ by Milne's method $y(0.2) = 0.2052$
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Pay Rk method.

 $y(0.3) = 0.3176$
 $y(0.4) = 0.4413$