



(An Autonomous Institution) Coimbatore 35

DEPARTMENT OF MATHEMATICS

UNIT-IV INTERPOLATION, NUMERICAL DIFFERENTIATION & **INTEGRATION**

NUMERICAL ENTEGRATION BY SIMPSONS 1/3

Simpson's
$$y_3$$
 RULE:

$$\int_{x_0}^{x_n} y \, dn = \frac{h}{3} \left[(y_0 + y_n) + 4 (y_1 + y_3 + \dots + y_{n-1}) + 2 (y_2 + y_4 + \dots + y_{n-2}) \right]$$

$$= \frac{h}{3} \left[A + 4 B + 2 C \right]$$

where A = Sum of the first & last-ordinalis B = Sum of the odd ordinates. c = Sum of the even ordinates.

cie) an even number of equal subinterrals.

Dividing the lange into 10 equal parts, Lind the value I Sinn on by Simpsons 1/8 stude





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Soln:
$$\chi$$
: 0 $\pi/20$ $\sqrt{\pi/20}$ $\sqrt{\pi/$

By Simpson's
$$1/3$$
 stude,

$$\int \frac{11/2}{5} \sin n \, dn = \frac{h}{3} \left[(y_0 + y_{11}) + 4 (y_1 + y_3 + y_6 + y_7 + y_9) + 2 (y_2 + y_4 + y_6 + y_8 + y_{10}) \right]$$

$$= \frac{11}{20} \cdot \frac{1}{3} \left[(0+1) + 4 (3.1962) + 2 (2.669) \right]$$

$$= 1.0000$$

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Find the value of loge 5 from
$$\int \frac{dn}{4n+5}$$
 by simpson's Y3 suche $(n=10)$.

Soln: Here $y(x) = \frac{1}{4n+5}$

$$h = 5-0 = \frac{1}{2} = 0.5$$

7:0.2 0.1429 0.1111 00909 0.0769 0.0667 0.0588 0.0526 0.047

By Simpson's 1/3 rub;

$$\int \frac{dn}{4n+8} = \frac{h}{3} \left[(y_0 + y_0) + 2(y_2 + y_4 + y_6 + \cdots) + \frac{h}{3} \right]$$

$$A(y_1 + y_3 + y_5 + \cdots)$$





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$$= \frac{1}{6} \left[\frac{3.4148}{4148} \right]$$

$$= 0.4025 - (1)$$

$$\int \frac{dn}{4n+5} = \frac{\log(4n+5)}{4} \int \frac{dn}{4n+5} = \frac{1}{4} \left(\frac{\log 2s - \log 5}{5} \right)$$

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$$= \frac{1}{4} \left(\frac{\log 5}{5} \right)$$

$$= \frac{1}{4} \log 5 = 0.4025$$

$$\Rightarrow \frac{\log 5}{3} = 1.61$$