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### DEPARTMENT OF MATHEMATICS

UNIT-V NUMERICAL SOLUTION OF ORDINARYDIFFERENTIAL EQUATIONS

JOURTH ORDER RUNGE-KUTTA METHOD FOR SOLVING FIRST AND SECOND ORDER EQUATIONS!

SECOND ORDER RK METHOD:

21 the initial values of (a,y) for the differential egn dy = f(x,y) then the first increment in y namely sy is calculated from the formula

$$k_2 = h_3 \int n + \frac{h}{2}, y + \frac{k_1}{2} \int$$

$$\Delta y = k_2 \text{ where } h = \Delta n$$

THIRD ORDER RK METHOD:

y(n a) - a rica





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$$K_3 = f_1 \left[ n_1 + f_1, y + 2k_2 - k_1 \right]$$
  

$$\Delta y = \frac{1}{6} \left[ k_1 + 4 k_2 + k_3 \right]$$
Now  $y_1 = y_0 + \Delta y$ 

FOURTH CROER RK METHOD:

$$k_1 = f_1 + f_2 + f_3 + f_4 + f_4 + f_5 + f_5 + f_6 + f_6$$





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Soln: Gn 
$$y'=x^3+y$$
 $x_0: 0; y_0=x. h=0.2.$ 

Now  $k_1=h \cdot h \cdot k_1 \cdot m_{0x} \cdot y_0: )=0.2 [x_0^3+y_0] = 0.2(0+x)=0.4$ 
 $k_2=h \cdot h \cdot k_2 \cdot m_{0x} \cdot y_0: )=0.2 \cdot h \cdot k_2 \cdot k_2 \cdot k_3 \cdot k_4 \cdot k_2 \cdot k_3 \cdot k_4 \cdot k_4 \cdot k_4 \cdot k_5 \cdot k_5 \cdot k_5 \cdot k_5 \cdot k_5 \cdot k_5 \cdot k_6 \cdot k_5 \cdot k_5 \cdot k_6 \cdot k_6 \cdot k_5 \cdot k_6 \cdot k_6$ 

= 2.4432





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$$k_2 = \hbar \frac{1}{2} \left[ x_1 + \frac{\hbar}{2}, y_1 + \frac{\kappa_1}{2} \right] = 0.5430$$

$$\Delta y = 0.5473.$$

$$y_2 = y_1 + \Delta y$$
  
= 2.4432+0.5473  
= 2.9905

Now RK neethod for (1/2, y2) where 1/2=0.4, y2=2.9905





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$$k_1 = h_1(x_3, y_2) = 0.6108$$
 $k_2 = h_1(x_2 + \frac{h}{2}, y_2 + \frac{k_1}{2}) = 0.6841$ 
 $k_3 = h_1(x_2 + \frac{h}{2}, y_2 + \frac{k_2}{2}) = 0.6914$ 
 $k_4 = h_1(x_2 + h, y_2 + k_3) = 0.7795$ 
 $\Delta y = 0.6902$ 
 $\Delta y = 0.6902$ 
 $y_3 = y_2 + \Delta y = 2.9905 + 0.6902 = 3.6807$ 

During RK method of 4th order solve 
$$y' = \frac{y^2 - n^2}{y^2 + n^2}$$
 with  $y(0) = 1$  at  $n = 0.2$ .

Soln: 1.1959

Sdn: 
$$y_1 = y(0.7) = 1.8762$$
  
 $y_2 = y(0.8) = 2.0142$ 

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