



SNS COLLEGE OF TECHNOLOGY

(An Autonomous Institution)

COIMBATORE-35

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ARTIFICIAL INTELLIGENCE FOR ELECTRICAL ENGINEERING UNIT 2

TOPIC:Propositional logic



TOPIC OUTLINE



Introduction to KBA
Logic: A General Idea
The Wumpus World Problem
Propositional Logic

Syntax

- Defines the allowable sentences
- **Atomic sentence** \rightarrow Contains a **single proposition symbol**, that can be true/false
- Convention- start with uppercase- $P, Q, R, W_{1,3}$ and *North*
- Symbols with fixed meanings: *True* is the always-true proposition and *False* is the always-false proposition
- **Complex sentences** are constructed from **simpler sentences**, using **parentheses** and **logical connectives**



Logical connectives(1/2)



- \neg (not) A sentence such as $\neg P$ is called the negation of P . A **literal** is either an atomic sentence (a **positive literal**) or a negated atomic sentence (a **negative literal**)
- \wedge (and) A sentence whose main connective is \wedge , such as $P \wedge Q$ is called a **conjunction**; its parts are the **conjuncts**
- \vee (or) A sentence using \vee , such as $(P \wedge Q) \vee R$, is a **disjunction** of the **disjuncts** $P \wedge Q$ and R



Logical connectives(2/2)

- \Rightarrow (**implies**). A sentence such as $(P \wedge Q) \Rightarrow \neg R$ is called an **implication (or conditional)**. Its **premise or antecedent** is $(P \wedge Q)$, and its **conclusion or consequent** is $\neg R$. Implications are also known as rules or if-then statements
- \Leftrightarrow (**if and only if**). The sentence $P \Leftrightarrow \neg Q$ is a **biconditional**

```
Sentence  $\rightarrow$  AtomicSentence | ComplexSentence
AtomicSentence  $\rightarrow$  True | False | P | Q | R | ...
ComplexSentence  $\rightarrow$  ( Sentence ) | [ Sentence ]
                  |  $\neg$  Sentence
                  | Sentence  $\wedge$  Sentence
                  | Sentence  $\vee$  Sentence
                  | Sentence  $\Rightarrow$  Sentence
                  | Sentence  $\Leftrightarrow$  Sentence
```

OPERATOR PRECEDENCE : $\neg, \wedge, \vee, \Rightarrow, \Leftrightarrow$



Semantics



- Defines the rules for determining the truth of a sentence with respect to a particular model
- Semantics for propositional logic must specify how to compute the truth value of any sentence, given a model
- For simple sentences:
 - *True* is true in every model and *False* is false in every model
 - The truth value of every other proposition symbol must be specified directly in the model
- For complex sentences, follow the five rules (m is model and “iff” means “if and only if”):
 1. $\neg P$ is true iff P is false in m
 2. $P \wedge Q$ is true iff both P and Q are true in m
 3. $P \vee Q$ is true iff either P or Q is true in m
 4. $P \Rightarrow Q$ is true unless P is true and Q is false in m
 5. $P \Leftrightarrow Q$ is true iff P and Q are both true or both false in m



Truth Tables

- Specify the truth value of a complex sentence for each possible assignment of truth values to its components

P	Q	$\neg P$	$P \wedge Q$	$P \vee Q$	$P \Rightarrow Q$	$P \Leftrightarrow Q$
false	false	true	false	false	true	true
false	true	true	false	true	true	false
true	false	false	false	true	false	false
true	true	false	true	true	true	true

