



(An Autonomous Institution) Coimbatore- 35

DEPARTMENT OF MATHEMATICS

UNIT- IV TESTING OF HYPOTHESIS

JEST OF SIGNIFICANCE OF SMALL GAMPLES !

VARIANCE RATIO TEST (OT) F- Test JOR EQUILITY OF VARIAN

Null Thypothesis : Ho: $\nabla_{1}^{2} = \nabla_{2}^{2}$ Test stastics : $F = \frac{S_{1}^{2}}{S_{2}^{2}}$ where $S_{1}^{2} > S_{2}^{2}$. where $S_{1}^{2} = \frac{n_{1}S_{1}^{2}}{n_{1}-1}$ of $S_{1}^{2} = \frac{\leq (\pi_{1} - \overline{\chi_{1}})^{2}}{n_{1}-1}$ & $\frac{S_{2}^{2} = \frac{n_{2}S_{2}^{2}}{n_{2}-1}$ of $S_{2}^{2} = \frac{\leq (\pi_{2} - \overline{\chi_{2}})^{2}}{n_{2}-1}$ Degree of treedom: (∇_{1}, ∇_{2}) where $\nabla_{1} = (n_{1}-1)$, $\nabla_{2} = (n_{2}-1)$

Note 1:- F Greater than zone always.
Note 2:- Suppose
$$S_2^2$$
 Greater than S_1^2 , then $F = \frac{S_2^2}{S_1^2}$
with degree 2 greadom, $V_1 = n_{2-1}$, $V_2 = n_{1-1}$
Applications:
F test' is used to test of the two samples have come
from the same population.





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) two landom sample 9 11 and 9 items show that the sample standard deviations 9 there weights as 0.8 & 0.5 supectively. Assuming that the weight distributions are normal, test the hypothesis that the twe variances are equal, against the alternative hypothesis that they are not Soln: Given · · n, = 11 , 31 = 0.8 n2 = 9 , 32 = 0.5 $S_1^2 = \frac{n_1 B_1^2}{n_1 - 1} = \frac{11(0 \cdot 8)^2}{11 - 1} = 0.404$ $g_{2^{2}} = \frac{\eta_{2}g_{2}}{\eta_{2}-1} = \frac{\eta(0.5)^{2}}{\eta-1} = 0.2812$ 312>5,2 step 1 > yourulate Ho & HI Ho: 51 = 52 CARE AND ALL A 1912 H1: 512 + 5.2 stip 2 -> Los at x = 5 y. slip 3 \rightarrow Test statistic, $F = \frac{S_1^2}{S_2^2} = \frac{0.704}{0.2812} = 2.5$ step 4 -> Degrees & freedom (19:12) (n.-1, n_2-1) = #2 =(10,8) Ceincalvalue, Ftab : Fx = 3.35 Step 5 → conclusion: F=2.5 < 3.35= Fx :. Ho is accepted at x: 5%.





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) Two kandom samples yave the zollowing lexulte: Sample size samplemean sum graqueres goleriation Jeon The means. 1 12 14 108 10 15 90 Yest whether The samples came from The same population . goln: Given: $n_1 = 12$, $x_1 = 14$, $\leq (x_1 - \bar{x}_1)^2 = 108$ $h_2 = 10, \ \bar{n}_2 = 15 \le (n_2 - \bar{n}_2)^2 = 90$ $S_1^2 = \frac{\sum (\eta_1 - \bar{\eta}_1)^2}{\eta_{1-1}} = \frac{108}{12 - 1} = 9.818$ $S_{2}^{2} = \frac{S(n_{2} - \bar{n}_{2})^{2}}{n_{2-1}} = \frac{90}{10-1} = 10$ S12 < S22 step 1: formulate Ho and HI !! Ho: 52=52 H_1 : $\nabla_1^2 \neq \sigma_2^2$ stip 2: Los at a = 5%. Step 3: test statistics, $F = \frac{S_2^2}{S_1^2} = \frac{10}{9.818}$ F = 1.018





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Step4: Degrees of freedom = (v, v2) = (no-1), n, -1) = (9,1)

critical value, Fx = 2.90

Step & : Conclusion:

F=1.018 < 2.90= Fa .

... Ho is accepted at 5% 205.

(i) t' Test :

step 1: Hormulate Ho & H1 : Ho: H, = H2 HI: H, + M2 dup 2: Los at 5 / .= x

glep 3: Test Statistic, $l = \overline{x_1} - \overline{x_2}$ $S \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$ Here n= 12, n2 = 10; 7,=14, 72=15 Now $s^2 = \Xi (x_1 - \bar{x}_1)^2 + \Xi (x_2 - \bar{x}_2)^2$ n1+n2 - 2 = 108+90 12+10-2 = 9.9 S = 3.14

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· + = 14-15 = -0.444 3.14 VI2 + 10 161 = 0. 744 stappy: Degrees of freedom, 2 = n, + no - 2 = 12+10-2 = 20 i. Ex = 2.086 step 5: concluinon, E= 0.444 × 2.086= Ex . Ho is accepted at 5%. Los. 3) Test whether the population variances are identical : Sumple I: 10 11 16 12 10 11 12 16 Sample I: 7 9 3 7 9 3 15 at 17-205 soln: given: n= = > n= = # ne (no- 2)2 "1, (1,- I) 2 0.3265 5.0625 1 10 2.0409 1. 5625 9 11 20.8944 3 14.0625 0.3265 16 7 0.0625 12 2.0409 5.0625 9 10 20.8944 1.5625 3 11 55.1841 0.0625 15 12 14.0625 101. 4143 16 53 5(12-72)2:101.71 41.5 98 $\frac{41.5}{\mathcal{Z}(3_{1}-\overline{n}_{1})^{2}} = 41.5 - \overline{n}_{1} \leq \underline{n}_{2}$ $: \underline{53}, \overline{7.54}$





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 $S_1^2 = \frac{\sum (n_1 - \overline{n}_1)^2}{n_1 - 1} = \frac{41 \cdot 5}{7} = 5.9286$ $S_{2}^{2} = \frac{S(\pi_{2} - \bar{\pi}_{2})^{2}}{n_{2} - 1} = \frac{101.7143}{6} = 16.9524$ 3,2 < 3,2 · step1: formulate Ho & HI: $H_{\mathcal{C}}$: $\nabla_1^2 = \nabla_2^2$ H1: 512 # 522 step 2: Los at \$= 1 %. Stip 3: Test statistic, $F = \frac{S_2^2}{S_1^2}$ = 16.9524 = 2.86 step 4 : Degrees 9 Freedom: (v, ve) 1. Jackson = (n2-1, n1-1) = (6, 4) Fa = 7.19 Main Day Step 5: Conclusion, F= 2.86 < 7.19 = Fx . Ho & accepted at Ho at 1 % Los. and La