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DEPARTMENT OF MATHEMATICS UNIT-IV INTERPOLATION, NUMERICAL DIFFERENTIATION **INTEGRATION**

LAGRANGIAN INTERPOLATION

Let y = f(x) be a function which takes the values $y_0, y_1, y_2, \dots, y_n$ corresponding Then Lagrangean interpolation form is to xo, x, 22..... 20 y = f(x)allarance them gauss phy nation $\frac{(\chi_0-\chi_1)(\chi_0-\chi_2)\cdots(\chi_0-\chi_n)}{(\chi_1-\chi_0)(\chi_1-\chi_2)\cdots(\chi_1-\chi_n)} \quad y_1 \neq 1$ Rest superinting Concoled 140 needs Su $\frac{(\chi - \chi_0)(\chi - \chi_1) \cdots (\chi - \chi_{n-1})}{(\chi_n - \chi_0)(\chi_n - \chi_1) \cdots (\chi_n - \chi_{n-1})} y_n$

Find the polynomial fix) by using Lagranges Jormula and hence find - J (3) 703 23MAT204-STATISTICS&NUMERICAL METHODS Mr.K.Palanivel//AP/MATHS/SNSCT



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By Lagrangis Interpolation Jornula, we have

$$y = -\frac{1}{2}(n) = \frac{(n-n_1)(n-n_2)(n-n_3)}{(n_0-n_1)(n_0-n_2)(n_0-n_3)} y_0 + \frac{(n-n_0)(n-n_2)(n_0-n_3)}{(n_1-n_0)(n_1-n_2)(n_1-n_3)} y_1 + \frac{(n-n_0)(n_1-n_2)(n_1-n_3)}{(n_2-n_0)(n_2-n_1)(n_2-n_3)} y_2 + \frac{(n-n_0)(n-n_1)(n-n_3)}{(n_2-n_0)(n_2-n_1)(n_2-n_3)} y_3$$

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$= \frac{(\chi-1)(\chi-2)(\chi-5)}{(0-1)(0-2)(0-5)} (2) + \frac{(\chi-0)(\chi-2)(\chi-5)}{(1-0)(1-2)(1-5)^{(3)}} + \frac{(\chi-0)(\chi-1)(\chi-2)}{(1-2)(1-5)^{(3)}} + \frac{(\chi-0)(\chi-1)(\chi-2)}{(2-0)(2-1)(2-5)} (12) + \frac{(\chi-0)(\chi-1)(\chi-2)}{(5-0)(5-1)(5-2)} (147) + \frac{(\chi-1)(\chi-2)(\chi-5)}{(1-2)(\chi-2)(\chi-5)} (12) + \frac{\chi(\chi-1)(\chi-2)(\chi-5)}{(1-2)} (12) + \frac{\chi(\chi-1)(\chi-2)}{(1-2)} (147) + \frac{\chi(\chi-1)}{(1-2)} (147) + \frac{\chi-1}{(1-2)} (147$

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Find the missing been in the following table using Lagrange's intespolation. 2 0 1 2 3 4 10 0 to 101 31 4 1 3 9 -- 8 Inverse Interpolation : The process of finding a value of x for the corresponding value of y is called inverse interpolation Inverse interpolation Jamula is $\chi = (y-y_1)(y-y_2)---(y-y_n)\chi_0 +$ (y-y) (yo-y2) - - (yo-yn) $(y-y_0)(y-y_2) - - (y-y_n) - R_1 +$ $(y_1 - y_0) (y_1 - y_2) - (y_1 - y_n)$ $(y - y_0)(y - y_1) - - \cdot (y - y_{n-1})$ (yn-yo) (yn-y1) --- (yn-yn-1) year .

$$(Y) \quad \text{SNS COLLEGE OF TECHNOLOGY} \\ (An Autonomous institution) \\ Coimbatore-35 \\ \textbf{DEPARTMENT OF MATHEMATICS} \\ \textbf{DEPARTMENT OF MATHEMATICS} \\ \textbf{DEPARTMENT OF MATHEMATICS} \\ \textbf{DEPARTMENT OF MATHEMATICS} \\ \textbf{STEGRATION} \\ \textbf{A} (T-V INTERPOLATION, NMERICALDIFFERENTIATION) \\ \textbf{A} (M The agic carresponding to the annually value 13.6
given the table
Age (x): 30 35 40 45 50
Annuity value(y): 15.9 14.9 14.1 13.3 12.5 \\ \textbf{M} = x = (Y-Y_1) * (Y-Y_2)(Y-Y_3)(Y-Y_4) (x_5-y_4) (x_5-y_4) (y_5-y_4)(y_5-y_4) (y_5-y_4) (y_5-y_6) (y_5-y_4) (y_5-y_5) (y_5-y_4) (y_5-y_4) (y_5-y_4) (y_5-y_6) (y_5-y_4) (y_5-y_6) (y_5-y_4) (y_5-y_6) (y_5-y_6) (y_5-y_4) (y_5-y_6) (y_5-y_$$

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= (13.6 - 14.9)(13.6 - 14.1)(13.6 - 13.3)(13.6 - 12.5)(15-9-14-9) (15-9-14-1) (15-9-14-1) (15-9-12-5) × 30 + $\frac{(13.6 - 15.9)(13.6 - 14.1)(13.6 - 13.3)(13.6 - 12.5)}{(14.9 - 15.9)(14.9 - 14.1)(14.9 - 15.3)(14.9 - 12.5)} \times 357$ $\frac{(13.6-15.9)(13.6-14.9)(13.6-13.3)(13.6-12.5)}{(14.1-12.5)} \times 407$ (13.6 - 15.9) (13.6 - 14.9) (13.6 - 14.1) (13.6 - 12.5)(13.3 - 15.9) (13.3 - 14.9) (13.3 - 14.1) (13.3 - 12.5)x 45+ $\frac{(13.6-15.9)(13.6-14.9)(13.6-14.1)(13.6-13.3)}{(12.5-15.9)(12.5-14.9)(12.5-14.1)(12.5-14.3)} \times 50$ = 431-600 == (1-05) 24 = 600, LORI & STORE OR

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