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DEPARTMENT OF MATHEMATICS

UNIT-IV INTERPOLATION, NUMERICAL DIFFERENTIATION & INTEGRATION

DERIVATIVES FROM DIFFERENCE TABLES _ DIVIDED DIFFERENCES :

$$\frac{1}{h} \left[\Delta y_0 + \frac{2u-1}{2!} \Delta^2 y_0 + \frac{3u^2-6u+2}{3!} \Delta^3 y_0 + \frac{3u^2-6u+2}{3!} \Delta^3 y_0 + \frac{3u^2-6u+2}{3!} \Delta^4 y_0 + \frac{3u^2-6u+2}{4!} \Delta^4 y_0 + \frac{3u^$$

putting
$$x = x_0$$
, then $u = 0$ and above eqn. Leduces

to
$$\left(\frac{\text{cly}}{\text{dn}}\right)_{n=x_0} = \frac{1}{\hbar} \left[\Delta y_0 + \frac{1}{2} \Delta^2 y_0 + \frac{1}{3} \Delta^3 y_0 + \Delta^4 y_0 + \frac{1}{5} \Delta^5 y \right]$$

$$\frac{d^2y}{dx^2} = \frac{1}{h^2} \left[\Delta^2 y_0 + \frac{6u - 6}{3!} \Delta^3 y_0 + 12 u^2 - 36 u + 22 \frac{3}{4!} \Delta^2 y_0 + \dots \right]$$

$$\frac{d^{2y}}{dn^{2}} = \frac{1}{h^{2}} \left[\Delta^{2}y_{0} + \Delta^{3}y_{0} + \frac{11}{12} \Delta^{4}y_{0} + \frac{5}{6} \Delta^{5}y_{0} \right]$$

$$2 = 20$$





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$$\frac{d^{3}y}{d^{3}x^{3}} = \frac{1}{h^{3}} \left[\frac{6}{3!} \Delta^{3}y_{0} + \frac{34u - 36}{4!} \Delta^{4}y_{0} + \dots \right]$$

$$\frac{(c^{13}y)}{(d^{3}x^{3})_{1} = \chi_{0}} = \frac{1}{h^{3}} \left[\Delta^{3}y_{0} - \frac{3}{2} \Delta^{4}y_{0} + \frac{7}{4}\Delta^{5}y_{0} \right]$$

NEWTON'S BACKWARD DIFFERENCE FORMULA:

$$\frac{dy}{dn} = \frac{1}{h} \left[\nabla y_{n} + \frac{2u+1}{2!} \nabla^{2}y_{n} + \frac{3u^{2}+6u+2}{3!} \nabla^{3}y_{n} + \frac{4u^{3}+18u^{2}+22u+6}{4!} \nabla^{4}y_{n} + \cdots \right]$$
At $x = x_{n}$, $u = 0$

$$\frac{dy}{dn} = \frac{1}{h} \left[\nabla y_{n} + \frac{1}{2} \nabla^{2}y_{n} + \frac{1}{3} \nabla^{3}y_{n} + \frac{1}{4} \nabla^{4}y_{n} + \cdots \right]$$

$$x = x_{n}$$

$$\frac{d^{2}y}{da^{2}} = -\frac{1}{h^{2}} \left[\nabla^{2}y_{n} + \frac{6u + 6}{3!} \nabla^{3}y_{n} + \frac{12u^{2} + 36u + 22}{4!} \nabla^{4}y_{n} \right]$$





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$$\frac{d^{3}y}{dn^{3}} = \frac{1}{h^{2}} \left[\nabla^{2}y_{n} + \nabla^{3}y_{n} + \frac{11}{12} \nabla^{4}y_{n} + \frac{1}{12} \nabla^{4}y_{n} + \frac$$





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D Find
$$1^{1}(8)$$
 and $1^{11}(8)$ for the following data:

 $2^{1}(8) = 3.0$
 3.2
 3.4
 3.6
 3.8
 4.0
 $1^{1}(8) = -14$
 10.032
 -5.296
 -0.256
 14
 3.968
 3.2
 -10.032
 4.736
 3.6
 -5.296
 5.04
 1.888
 -3.012
 3.8
 6.672
 1.888
 -3.072
 -1.488
 -1.488
 -1.488
 -1.488
 -1.488

By Newton's forward formula

$$\frac{dy}{dx}|_{x=x_0} = \left(\frac{dy}{dx}\right)_{u=0}$$





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Here
$$h = 0.2$$

$$= \frac{1}{0.2} \left[3.968 - \frac{1}{2} (0.768) + \frac{1}{3} (-0.464) - \frac{1}{4} (2.048) + \frac{1}{5} (-5.12) \right]$$

$$= \frac{1}{0.2} \left[3.968 - 0.384 - 0.1547 - 0.512 - 1.024 \right]$$

$$= \frac{1}{0.2} \left[1.8933 \right]$$

$$= 9.4665$$

$$(\frac{d^2y}{dn^2})_{x=x_0} = \frac{1}{h^2} \left[\Delta^2 y_0 - \Delta^3 y_0 + \frac{11}{12} \Delta^4 y_0 - \frac{5}{6} \Delta^5 y_0 + \dots \right]$$

$$= \frac{1}{(0.2)^2} \left[0.768 - (-0.464) + \frac{11}{12} (2.048) - \frac{5}{6} (-5.12) \right]$$

$$= \frac{1}{0.04} \left[0.768 + 0.464 + 1.8773 + 4.267 \right]$$

$$= \frac{1}{0.04} \left[7.3763 \right] = 1846 40767 - 36.676$$