



**DEPARTMENT OF MATHEMATICS**

**UNIT-IV INTERPOLATION, NUMERICAL DIFFERENTIATION**

**&**

**INTEGRATION**

*NUMERICAL INTEGRATION BY TRAPEZOIDAL*

*TRAPEZOIDAL RULE :*

$$\int_{x_0}^{x_n} y \, dx = \frac{h}{2} [(y_0 + y_n) + 2(y_1 + y_2 + \dots + y_{n-1})]$$
$$= \frac{h}{2} [A + 2B]$$

where A = sum of the first & last ordinates

B = sum of the remaining ordinates.

① using trapezoidal rule, evaluate  $\int_{-1}^1 \frac{dx}{1+x^2}$  taking 8 intervals.

Soln: Gfn:  $y(x) = \frac{1}{1+x^2}$

Here  $h = \frac{b-a}{n}$  where  $a = -1$ ,  $b = 1$ , and  $n = 8$

$$\Rightarrow h = \frac{2}{8} = 0.25$$



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$x$	-1	-0.75	-0.5	-0.25	0	0.25	0.5	0.75	1
$y$	0.5	0.64	0.8	0.9412	1	0.9412	0.8	0.64	0.5

Trapezoidal rule,

$$\int_{-1}^1 \frac{1}{1+x^2} dx = \frac{h}{2} [(y_0 + y_n) + 2(y_1 + y_2 + \dots + y_{n-1})]$$

$$= \frac{h}{2} [\text{sum of the first and last ordinates} \\ + 2 \times \text{sum of the remaining ordinates}]$$

$$= \frac{0.25}{2} [(0.5 + 0.5) + 2(0.64 + 0.8 + 0.9412 + \\ 0.9412 + 0.8 + 0.64)]$$

$$= \frac{0.25}{2} \times 12.5248$$

$$= 1.5656$$

(2) Dividing the range into 10 equal parts, find the value

of  $\int_0^{\pi/2} \sin x dx$  by (i) Trapezoidal rule



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Soln:

$x$	$0$	$\pi/20$	$2\pi/20$	$3\pi/20$	$4\pi/20$	$5\pi/20$
$y = \sin x$	$0$	$0.1564$	$0.3090$	$0.4540$	$0.5878$	$0.7071$
$x$	$6\pi/20$	$7\pi/20$	$8\pi/20$	$9\pi/20$	$10\pi/20$	
$y = \sin x$	$0.8090$	$0.8910$	$0.9511$	$0.9877$	$1$	

By Trapezoidal rule;

$$\int_0^{\pi/2} \sin x \, dx = \frac{h}{2} [(y_0 + y_{10}) + 2(y_1 + y_2 + \dots + y_{10})]$$

Here  $h = \frac{\pi/2 - 0}{10} = \frac{\pi}{20}$

$$= \frac{h}{2} [(0 + 1) + 2(0.1564 + 0.3090 + 0.4540 + 0.5878 + 0.7071 + 0.8090 + 0.8910 + 0.9511 + 0.9877)]$$

$$= \frac{\pi}{20} \cdot \frac{1}{2} [12.7062]$$

$$= 0.9980$$