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10 classes(digits)



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• This is what a regular feed-forward neural network will look like

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- This is what a regular feed-forward neural network will look like
- There are many dense connections here

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- This is what a regular feed-forward neural network will look like
- There are many dense connections here
- For example all the 16 input neurons are contributing to the computation of *h*₁₁



- This is what a regular feed-forward neural network will look like
- There are many dense connections here
- For example all the 16 input neurons are contributing to the computation of *h*₁₁
- Contrast this to what happens in the case of convolution

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• Only a few local neurons participate in the computation of h_{11}

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• For example, only pixels 1, 2, 5, 6 contribute to h_{11}







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- We are taking advantage of the structure of the image(interactions between neighboring pixels are more interesting)





 h_{14}

- Only a few local neurons participate in the computation of h_{11}
- For example, only pixels 1, 2, 5, 6 contribute to h_{11}
- The connections are much sparser
- We are taking advantage of the structure of the image(interactions between neighboring pixels are more interesting)
- This **sparse connectivity** reduces the number of parameters in the model

• But is sparse connectivity really good thing ?

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* Goodfellow-et-al-2016

- But is sparse connectivity really good thing ?
- Aren't we losing information (by losing interactions between some input pixels)

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• Well, not really



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- The two highlighted neurons $(x_1 \& x_5)^*$ do not interact in *layer* 1



- But is sparse connectivity really good thing ?
- Aren't we losing information (by losing interactions between some input pixels)
- Well, not really
- The two highlighted neurons $(x_1 \& x_5)^*$ do not interact in *layer* 1
- But they indirectly contribute to the computation of g_3 and hence interact indirectly

• Another characteristic of CNNs is **weight sharing**

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- Another characteristic of CNNs is **weight sharing**
- Consider the following network

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- Another characteristic of CNNs is **weight sharing**
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4x4 Image



- Another characteristic of CNNs is **weight sharing**
- Consider the following network
- Do we want the kernel weights to be different for different portions of the image?



4x4 Image





4x4 Image

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- Do we want the kernel weights to be different for different portions of the image?
- Imagine that we are trying to learn a kernel that detects edges





4x4 Image

- Another characteristic of CNNs is **weight sharing**
- Consider the following network
- Do we want the kernel weights to be different for different portions of the image?
- Imagine that we are trying to learn a kernel that detects edges
- Shouldn't we be applying the same kernel at all the portions of the image?

• In other words shouldn't the *orange* and *pink* kernels be the same

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• In other words shouldn't the *orange* and *pink* kernels be the same

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• Yes, indeed



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• Yes, indeed





- In other words shouldn't the *orange* and *pink* kernels be the same
- Yes, indeed
- This would make the job of learning easier(instead of trying to learn the same weights/kernels at different locations again and again)

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- In other words shouldn't the *orange* and *pink* kernels be the same
- Yes, indeed
- This would make the job of learning easier(instead of trying to learn the same weights/kernels at different locations again and again)
- But does that mean we can have only one kernel?

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- Yes, indeed
- This would make the job of learning easier(instead of trying to learn the same weights/kernels at different locations again and again)
- But does that mean we can have only one kernel?
- No, we can have many such kernels but the kernels will be shared by all locations in the image

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- Yes, indeed
- This would make the job of learning easier(instead of trying to learn the same weights/kernels at different locations again and again)
- But does that mean we can have only one kernel?
- No, we can have many such kernels but the kernels will be shared by all locations in the image
- This is called "weight sharing" one arrows arrows

• So far, we have focused only on the convolution operation

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- So far, we have focused only on the convolution operation
- Let us see what a full convolutional neural network looks like





• It has alternate convolution and pooling layers

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- It has alternate convolution and pooling layers
- What does a pooling layer do?



- It has alternate convolution and pooling layers
- What does a pooling layer do?
- Let us see



Input

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Input

1 filter



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1 filter

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	-	

1	4	2	1	
5	8	3	4	
7	6	4	5	
1	3	1	2	



1 filter







1 filter



8





8 4

7



8 4

7 5

*



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1	4	2	1			
5	8	3	4	maxpool	8	4
7	6	4	5	2x2 filters (stride 2)	7	5
1	3	1	2			

Input

1 filter

1	4	2	1
5	8	3	4
7	6	4	5
1	3	1	2

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1 filter

1	4	2	1	
5	8	3	4	maxpool
7	6	4	5	2x2 filters (stride 1)
1	3	1	2	

 $\mathbf{2}$

3 4

4

 $1 \quad 2$

1

5

maxpool

2x2 filters (stride 2)

8 4

7 5

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1	4	2	1			
5	8	3	4	maxpool	8	4
7	6	4	5	2x2 filters (stride 2)	7	5
1	3	1	2			



1 filter



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1 filter



maxpool

2x2 filters (stride 2)

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 $\mathbf{2}$

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8 3

6 4 5

3 1 2

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1	4	2	1			
5	8	3	4	maxpool	8	4
7	6	4	5	2x2 filters (stride 2)	7	5
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1 filter









1 filter



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1 filter



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1 filter



maxpool

2x2 filters (stride 2)

8 4

7 5

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 $\mathbf{2}$

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4 5

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maxpool

2x2 filters (stride 2)

8 4

7 5

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Input

1 filter

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4 5

1 2

1

 $\mathbf{4}$







1 filter



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1 filter



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1	4	2	1			
5	8	3	4	maxpool	8	4
7	6	4	5	2x2 filters (stride 2)	7	5
1	3	1	2			



1 filter



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• Instead of max pooling we can also do average pooling

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We will now see some case studies where convolution neural networks have been successful

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LeNet-5 for handwritten character recognition



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Param =?

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Param = 150

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$$\begin{array}{ll} R = 0, F = 0, \\ Param = 150 \end{array} \qquad \begin{array}{ll} R = 0, F = \\ Param = ? \end{array}$$

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$$K = 6, P = 0, \qquad K = 6, P = 0$$

Param = 150 Param = 0

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• How do we train a convolutional neural network ?

	Input		
b	с	d	
е	f	g	
h	i	j	





• A CNN can be implemented as a feedforward neural network

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- A CNN can be implemented as a feedforward neural network
- wherein only a few weights(in color) are active

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- A CNN can be implemented as a feedforward neural network
- wherein only a few weights(in color) are active
- the rest of the weights (in gray) are zero









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	Input		
b	с	d	
е	f	g	
h	i	j	





- A CNN can be implemented as a feedforward neural network
- wherein only a few weights(in color) are active
- the rest of the weights (in gray) are zero



Kernel

• We can thus train a convolution neural network using backpropagation by thinking of it as a feedforward neural network with sparse connections



- A CNN can be implemented as a feedforward neural network
- wherein only a few weights(in color) are active
- the rest of the weights (in gray) are zero

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Module 11.4 : CNNs (success stories on ImageNet)

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ImageNet Success Stories (roadmap for rest of the talk)

• AlexNet

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ImageNet Success Stories(roadmap for rest of the talk)

- AlexNet
- ZFNet

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ImageNet Success Stories(roadmap for rest of the talk)

- AlexNet
- ZFNet
- \bullet VGGNet

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