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### **DEPARTMENTOFMATHEMATICS**

UNIT-V LAPLACETRANSFORM

# PERIODIC FUNCTIONS:

A junct fit is said to be periodic if

{(t+7)= f(t) for all values of t and for certain

values of T. The smallest value of T for which

{(t+7)= f(t) for all t is called the period of the func.

gO! The Junct state cost are periodic Junctions, both having period 271.

Sht = Sh(t+211) = Sh (t+411)=...

consider the func. Jet)= St y oxtx2 and Jet+47=Jet; L4-t y 2<tx4 :. Jet) is a periodic func. with period 4.

# 17 g períodic functions:

Letter) be a periodic function with period T. Then  $1 + (t) = \frac{1}{1 - e^{-ST}} \int_{0}^{T} e^{-St} f(t) dt.$ 





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Then LT of 
$$f(t) = (\frac{2t}{3})$$
, osts 3 &  $f(t+3) = f(t)$   
Soln:  $f(t)$  & a postable func. with period 3.  
WITH LFG(t)  $T = \frac{1}{1-e^{-5T}} \int e^{-5t} + f(t) dt$ 

$$= \frac{1}{1-e^{-3S}} \int_{3}^{3} e^{-5t} \left(\frac{2t}{3}\right) dt = \frac{1}{1-e^{-3S}} \left(\frac{2}{3}\right) \int_{3}^{2} e^{-5t} dt$$

$$= \frac{1}{1-e^{-3S}} \left(\frac{2}{3}\right) \left[\frac{1-e^{-5t}}{-s} - \frac{e^{-5t}}{s^{2}}\right]^{3}$$

$$= \frac{1}{1-e^{-3S}} \left(\frac{2}{3}\right) \left[\frac{3e^{-3S}}{-s} - \frac{e^{-3S}}{s^{2}} + \frac{1}{s^{2}}\right]$$

$$= \frac{1}{1-e^{-3S}} \left(\frac{2}{3}\right) \left[\frac{1-e^{-3S}}{s^{2}} - \frac{3e^{-3S}}{s}\right]$$
Then the LT of  $f(t)$  if  $f(t) = e^{t}$ , or  $f(t) = f(t+2)$ .

Solution  $f(t)$  is a periodic function with period  $f(t) = f(t+2)$ .

Left(t)  $f(t)$  is a periodic function with period  $f(t)$  in  $f($ 





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3) Find LT of 
$$f(t) = \int_{z-t}^{z} \int_{1 < t < 2}^{z} \int_{1 < t < 2}$$

 $\frac{\int dn!}{S(1-e^{-2aS})}$ 





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