

SNSCOLLEGEOFTECHNOLOGY



(AnAutonomousInstitution)
Coimbatore— 35

DEPARTMENTOFMATHEMATICS

UNIT-VLAPLACETRANSFORM

PARTIAL FRACTION : Ind 2-1 [5 (S+1) (S+2)] $\frac{3\ln 1}{5(5+1)(5+2)} = \frac{A}{5} + \frac{B}{5+1} + \frac{C}{5+2}$ 1 = A(S+1)(S+2)+ B(8+2)S+ CS(S+1) put s = -1 1 = A(0)+ B(-1)(1)+ c(0) $\Rightarrow B = -1$ put S = -2, 1 = A(0) + B(0) + C(-2)(-1)1 = 2C => c= 1/2 put s =0 1 = A(1)(2) + B(0) + C(0)=) 1=2A =) A=1/2 $\frac{1}{s(s+1)(s+2)} = \left[\frac{1/2}{s} - \frac{1}{s+1} + \frac{1/2}{s+2} \right]$ $L^{-1}\left[\frac{1}{S(S+1)(S+2)}\right] = L^{-1}\left[\frac{\gamma_2}{S}\right] - L^{-1}\left[\frac{1}{S+1}\right] + L^{-1}\left[\frac{\gamma_2}{S+2}\right]$ = 1 2-1 [=] - 2-1 [=] + 1 2 2-1 [=] $= \frac{1}{2} - e^{-t} + \frac{1}{2} e^{-2t}$ $= \frac{1}{3} \left[1 - 2e^{-t} + e^{-2t} \right]$



SNSCOLLEGEOFTECHNOLOGY



FARTING FRACTION

(AnAutonomousInstitution) Coimbatore 35

DEPARTMENTOFMATHEMATICS

UNIT-VLAPLACETRANSFORM

$$\frac{30 \ln 7}{(S+1-)(S-3)^2} = \frac{A}{S+1} + \frac{B}{S-3} + \frac{C}{(S-3)^2}$$

$$2S^2 + 4S + 5 = A (S-3)^2 + B(S-3)(S+1)C(S+1)$$

$$S=-1$$
,
2-4+5 = $A(-4)^2+B(-4)(0)+C(0)$

$$\Rightarrow A = 3/16$$

$$\Rightarrow$$
 B= $\frac{29}{16}$

$$\frac{1}{(s+1)(s-3)^2} \int = \frac{3}{16} L^{-1} \left[\frac{1}{s+1} \right] + \frac{29}{16} L^{-1} \left[\frac{1}{(s-3)} \right] + \frac{35}{4} L^{-1} \left[\frac{1}{(s-3)} \right]$$

$$= \frac{3}{16} e^{-t} + \frac{29}{16} e^{-3t} + \frac{35}{16} e^{-$$



SNSCOLLEGEOFTECHNOLOGY



(AnAutonomousInstitution)
Coimbatore— 35

DEPARTMENTOFMATHEMATICS

UNIT-VLAPLACETRANSFORM

3) It is
$$1-1 \left[\frac{S^2}{(S+1)(S^2+4)} \right]$$

Soln: $S^2 = A \left(S^2 + 4 \right) + BS + C \left(S^2 + 4 \right)$

$$S^2 = A \left(S^2 + 4 \right) + BS + C \left(S^2 + 1 \right)$$

Put $S = -1$

$$\Rightarrow 1 = A(5) + B(-1)(0) + C(0)$$

$$\Rightarrow A = \frac{1}{5}$$

put $S = 0$

$$\Rightarrow 0 = 4A + C \Rightarrow C = -4$$

$$\Rightarrow b = 4$$

$$1b = 20A + 12B - 3C$$

$$\Rightarrow B = \frac{4}{5}$$

$$1 - 1 \left[\frac{8^2}{(S+1)(S^2+4)} \right] = 1 - 1 \left[\frac{4}{5} \right] + \frac{4}{5} + \frac{4}{5} + \frac{5}{5} + \frac{5}{5} + \frac{1}{5} + \frac{1}{$$