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DEPARTMENT OF MATHEMATICS

UNIT V

DESIGN OF EXPERIMENTS

Experiment: A collection of data or measurements of some features of an object.

Treatments: Various objects of Comparison in a Comparative experiment are called bleatments.

Experimental unit: The Smallest division of the experimental material to which we apply the bleatments.

Blocks: The whole experimental units dre divided into subgroups called blocks.

Experimental error: It is the error occured due to random Causes or chance causes or non-assignable factors which are beyond own control.

Basic principles of experimental design

- 1. Randomisation
- 2. Replication
- 3. Local control

Basic Designs of experiment

- 1. Completely Randomised Design (C.R.D or one.way classification)
- 2. Randomised Block Design (R.B.D or Two. way classification)
- 3. Latin square Design (L. s. D or Three way classification)



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Analysis of Variance (ANOVA)

The analysis of variance is a widely used technique developed by Prof. R.A. Fisher.

tumber of populations (more than two) are equal.

Assumptions:

- 1. Each sample taken is a standom sample
- 2. Each one is independent of the other sample.
- 3. Populations from which samples are taken are normal.
- 4. Variances of the populations are equal.

Completely Randomised Design (One-way Classification):
This is a one factor experiment.

Procedure:

Step 1:

Null hypothesis: Ho: There is no significante difference between columns and errors.

Alternative hypothesis: H.: There is a significant difference between columns and errors.

Step 2:

- * Find N, number of given observation
- * Find T, total number of observation
- # Find correction factor $C.F = \frac{T^2}{N}$

Step 3: Find :

* Moson sum of squares of treatments $SST = \sum x_1^2 + \sum x_2^2 + \sum x_3^2 + \cdots - C.F$



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* Sum of Squares of columns

$$SSC = \frac{(\Sigma x_1)^2 + (\Sigma x_2)^2 + (\Sigma x_3)^2}{c_1} + \dots - C.F$$

* Sum of Squares of errors

SSE = SST - SSC

Stop 4: ANOVA Table:

Source of Variation	Degree of freedom	Sum of Squares	Mean Sum of Squares	Variance Yati O	Table Value
Between Columns		SSC	$MSC = \frac{SSC}{C-1}$	MSE (or)	Fx (c-1, N-c)
Between	N-c	SSE	$MSE = \frac{SSE}{N-C}$	MSE MSC	E(N-C,C-1)

Step 5: Decision :

If Sinae $|F| < F_{\alpha}$, we accept the hypothesis $|F| > F_{\alpha}$, we deject the hypothesis.

Problem:

(1) A sandom sample is selected from each of these makes of ropes and their breaking strength are measured with the following results. Test whether the breaking strength of the ropes differ significantly.

T II III
70 100 60
72 108 57
75 112 84
80 113 87
83 120 73

Solution :

Step 1: Null hypothesis : Ho : There is no significant difference between Column and errors .

difference between column and everors

Step 2:

$$N = 18$$

 $T = 1576$
 $C.F = T^{2}/N = \frac{1576^{2}}{18} = 137987.55$

Step 3:

х,	*,	×3	x,2	x,2	X3"
70	100	60	4900	10000	3600
72	110	65	5184	12100	4225
75	108	57	5625	11664	3249
80	112	84	6400	12544	3056
83	113	8 7	6889	12.769	7569
	120	73		14400	5329
	107			11449	
380	770	426	28 998	84926	31028

$$SST = 28998 + 84926 + 31028 - 137987.55$$

$$= 6964.45$$

$$SSC = \frac{(Sx_1)^2 + (Sx_2)^2 + (Sx_3)^2}{c_1} - C.F$$

$$= \frac{(380)^2}{5} + \frac{(770)^2}{7} + (426)^2 - 137987.55$$

$$SSC = 5838.44$$



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SSE - SST - SSC = 6764.45 - 58 36.49

Stop 4 : ANOVA Lable :

Source of Variation	Degree of freedom	Sum of Squares	Mean sum of sequeres	Variance Vatio	Table Value
Between	C-1 = 3-1 = 2	5838.44	MSC = SSC C-1 = 2919.22	1	F2 (2,15)
Between Errors	N-C=18-3	SSE =	MSE = SSE N-C = 75.067	= 58.86	

Since F > F2, we reject the hypothesis. .. There is a significant difference between Columns and errors