

## DEPARTMENT OF MATHEMATICS

Course Code & Name : **23MAT101 -MATRICES AND CALCULUS**

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### Question Bank UNIT V-MUTIPLE INTEGRALS

#### Part A- Two Mark Questions

1	Evaluate $\int_0^5 \int_0^2 (x^2 + y^2) dx dy$	(WIPRO, 2023)	L -3
2	Evaluate $\int_0^1 \int_0^2 xy dx dy$	(WIPRO, 2023)	L -3
3	Evaluate $\int_2^3 \int_1^2 \frac{1}{xy} dx dy$	(WIPRO, 2023)	L -3
4	Sketch the region of integration in $\int_0^1 \int_0^x dy dx$ .	(TCS, 2022)	L -2
5	Change the order of integration in $\int_0^a \int_x^a f(x, y) dx dy$ .	(WIPRO, 2020)	L -2
6	Change the order of integration $\int_0^1 \int_0^y dx dy$ .	(WIPRO, 2020)	L -2
7	Obtain the value of $\int_0^a \int_0^b \int_0^c dx dy dz$ .	(TCS, 2022)	L -3
8	Evaluate $\int_1^3 \int_2^3 \int_1^2 x^2 yz dx dy dz$	(TCS, 2022)	L -3
9	Evaluate $\int_0^a \int_0^b \int_0^c x^2 + y^2 + z^2 dx dy dz$	(TCS, 2022)	L -3
10	Write any two applications of double integral		L-1

## PART B

1	Change the order of integration in the interval $\int_0^1 \int_{x^2}^{2-x} xy \, dx dy$ and hence evaluate it.	GATE-2017	L-4
2	Change the order of integration in the interval $\int_0^a \int_{x^2/a}^{2a-x} xy \, dx dy$ and hence evaluate it		L-4
3	Change the order of integration in $\int_0^a \int_y^a x^2 + y^2 \, dx dy$ and hence evaluate it.		L-4
4	Change the order of integration $\int_0^\infty \int_x^\infty \frac{e^{-y}}{y} dy dx$ hence evaluate it.	(GATE, 2021)	L -4
5	Find the area enclosed by the curves $y^2 = 4ax$ and $x^2 = 4ay$	(WIPRO, 2023)	L -3
6	Evaluate $\iint xy \, dx dy$ over the positive quadrant of the circle $x^2 + y^2 = 1$	(WIPRO, 2023)	L -3
7	Find the area of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$	(WIPRO, 2023)	L -3
8	Find the area bounded by the line $y = x$ and parabola $x^2 = y$	(WIPRO, 2023)	L -3
9	Find the area bounded by the lines $x = 0, y = 1, y = x$ using double integration	(WIPRO, 2023)	L -3
10	Evaluate $\iint (x - y) \, dx dy$ over the region between the line $y = x$ and parabola $x^2 = y$	(WIPRO, 2023)	L -3
11	Evaluate $\int_0^{\log 2} \int_0^x \int_0^{x+y} e^{x+y+z} \, dx dy dz$		L -3
12	Evaluate $\int_0^1 \int_0^{1-x} \int_0^{1-x-y} xy \, dx dy dz$		L -3
13	Evaluate $\iiint_V \frac{dz dy dx}{(x+y+z+1)^3}$ where V is the region bounded by $x = 0, y = 0, z = 0$ and $x + y + z = 1$		L -3
14	Using triple integration, find the volume of the sphere $x^2 + y^2 + z^2 = a^2$ .	(HCL, 2023)	L -4
15	Find the volume of the ellipsoid $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$ .	(HCL, 2023)	L -4
16	Find the volume of the tetrahedron bounded by $x = 0, y = 0, z = 0$ , $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$	(HCL, 2023)	L -4