

### SNS COLLEGE OF TECHNOLOGY, COIMBATORE –35 (An Autonomous Institution) DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING LINEAR REGRESSION MODELS AND LEAST SQUARES



Supervised Learning:

- Find the class labels or value of the new input, given the dataset.
- MACHINE LEARNING –
- Reinforcement learning: Learn to act in a way that maximizes the future rewards (or minimizes a cost function) –
- In game theory: Learn to act in a way that maximized the future rewards, in an environment that contains other machines.

#### Linear regression

- Linear regression is one of the easiest and most popular Machine Learning algorithms.
- It is a statistical method that is used for predictive analysis.
- Linear regression makes predictions for continuous/real or numeric variables such as sales, salary, age, product price, etc.

The linear regression model provides a sloped straight line representing the relationship between the variables. Consider the below image:





## SNS COLLEGE OF TECHNOLOGY, COIMBATORE –35 (An Autonomous Institution)



## DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING

#### Types of Linear Regression

• Linear regression can be further divided into two types of the algorithm:

#### • Simple Linear Regression:

If a single independent variable is used to predict the value of a numerical dependent variable, then such a Linear Regression algorithm is called Simple Linear Regression.

#### • Multiple Linear regression:

If more than one independent variable is used to predict the value of a numerical dependent variable, then such a Linear Regression algorithm is called Multiple Linear Regression.

#### Linear Regression Line

• A linear line showing the relationship between the dependent and independent variables is called a **regression line**.

#### Positive Linear Relationship:

If the dependent variable increases on the Y-axis and independent variable increases on X-axis, then such a relationship is termed as a Positive linear relationship.

#### Negative Linear Relationship:

If the dependent variable decreases on the Y-axis and independent variable increases on the X-axis, then such a relationship is called a negative linear relationship.

Cost function-

- The different values for weights or coefficient of lines  $(a_0, a_1)$  gives the different line of regression, and the cost function is used to estimate the values of the coefficient for the best fit line.
- Cost function optimizes the regression coefficients or weights. It measures how a linear regression model is performing.
- We can use the cost function to find the accuracy of the **mapping function**, which maps the input variable to the output variable. This mapping function is also known as **Hypothesis function**.

#### Gradient Descent:

• Gradient descent is used to minimize the MSE by calculating the gradient of the cost function.



# SNS COLLEGE OF TECHNOLOGY, COIMBATORE –35 (An Autonomous Institution)



## DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING

- A regression model uses gradient descent to update the coefficients of the line by reducing the cost function.
- It is done by a random selection of values of coefficient and then iteratively update the values to reach the minimum cost function.

Model Performance:

- **R-squared method:**
- R-squared is a statistical method that determines the goodness of fit.
- It measures the strength of the relationship between the dependent and independent variables on a scale of 0-100%.
- The high value of R-square determines the less difference between the predicted values and actual values and hence represents a good model.
- It is also called a **coefficient of determination**, or **coefficient of multiple determination** for multiple regression.

Simple Linear regression algorithm has mainly two objectives:

- Model the relationship between the two variables. Such as the relationship between Income and expenditure, experience and Salary, etc.
- Forecasting new observations. Such as Weather forecasting according to temperature, Revenue of a company according to the investments in a year, etc. LEAST SQUARES
- The Least Squares Regression Line is the line that makes the vertical distance from the data points to the regression line as small as possible.

The best line of fit is one that minimizes the variance (the sum of squares of the errors). 19CST301 & INTRODUCTION TO MACHINE LEARNING Mrs.L.Poornima Devi



## SNS COLLEGE OF TECHNOLOGY, COIMBATORE -35 (An Autonomous Institution) DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING



- Ordinary least squares regression (OLS) is usually just called "regression" in statistics.
- In the linear regression formula,

The slope is the a in the equation y = b + ax.

PEARSON CORRELATION EQUATION for calculating is used

#### LEAST SQUARE FITTING

- Least squares fitting (also called least squares estimation) is a way to find the best fit curve or line for a set of points.
- In this technique, the sum of the squares of the offsets (residuals) are used to estimate the best fit curve or line instead of the absolute values of the offsets.
- The resulting equation gives you a y-value for any x-value, not just those x and y values plotted with points.

**Ordinary Least Squares** 

• Ordinary least squares regression is a way to find the line of best fit for a set of data. It does this by creating a model that minimizes the sum of the squared vertical distances (residuals).