

# SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution) Approved by AICTE, New Delhi, Affiliated to Anna University, Chennai Accredited by NAAC-UGC with 'A++' Grade (Cycle III) & amp; Accredited by NBA (B.E - CSE, EEE, ECE, Mech & amp; B.Tech.IT) COIMBATORE-641 035. TAMIL NADU

#### **DEPARTMENT OF MATHEMATICS**

path:

A path in a graph is a requerce VI, V2, ..., VK Of Vortgas, each adjacent to the heart.

rendth of the path:

The No. of edges apparing in the sequence of path

Be called the length of the path. it output a cycle. Or cults: A closed path in which all the odges are destind is called a concient.

cycle c:

A correct 9n which all the vortices are distinct is a cyclec.

An dejected graph is said to be connected 9% connected gaph: any pale of nodes are reachable from one another. any pass of bodos.

A gample digraph & hand to be strongly Strongly connected : connected of too any pass of nodes of the graph both the nades of the pass are reachable from one anothor.

A simple digraph is said to be weakly weakly connected: Connected 96 96 96 12 13 connected as an undbrected graph pr which the durect an of the edges is neglected.

A semple degraph is said to be unilaterally Unflatenally connected: connected, of good any pass of nodes of the graph at least one of the nodes of the passi's reachable from the other node. Note: 1). A uc is we but a we is not necessarily UC.

A BC 13 both USWC 2)



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#### **DEPARTMENT OF MATHEMATICS**

Theorem 4:  
A Simple graph with 
$$p$$
 vertices and  $k$  composed  
Carrot have more trans  $(p-k)(p-k+1)$  edges.  
A Simple graph with  $p$  vertices and  $k$  composed  
can have atmost  $(p-k)(p-k+1)$  edges.  
Recol:  
Let  $n_1, n_{23}, ..., n_k$  be the no. of vertices  $fh$  each  
of  $k$  components  $q$  the graph  $q$ .  
Then  $n_1 + n_2 + ... + n_k = n = 1$   $V(q_1)$   
 $\frac{k}{j=1}$   $n_j = n \rightarrow (1)$   
Nows  $\frac{k}{k} (n_j - 1) = (n_1 - 1) + (n_2 - 1) + ... + (n_k - 1)$   
 $\frac{k}{j=1} (n_j - 1) = n - k$   
Squaring on bothscides.  
 $\left[\int_{j=1}^{k} (n_j - 1)^2 = (p - k)^2$   
 $(n_1 - 1)^2 + (n_2 - 1)^2 = (p - k)^2$   
 $(n_1^2 + n_2^2 + ... + n_k) - n_k = h^2 + k^2 - 2nk$   
 $(n_1^2 + n_2^2 + ... + n_k) - 2n_j - 2n_2 - ... - 2n_k + 1 + 1 + 1 + ... + 1 \le \frac{k}{j=1}$   $n_1^2 - 2n_j - 2n_j - 2n_j - ... - 2n_k + 1 + 1 + 1 + ... + 1 \le \frac{k}{j=1}$   $n_1^2 - 2n_j + ... + n_k) + k \le n^2 + k^2 - 2nk$   
 $\frac{k}{j=1} n_1^2 - 2(n_j + n_2 + ... + n_k) + k \le n^2 + k^2 - 2nk$   
 $\frac{k}{j=1} n_1^2 - 2(n_j + n_2 + ... + n_k) + k \le n^2 + k^2 - 2nk$   
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 $\frac{k}{j=1} n_1^2 - 2(n_j + n_j + ... + n_k) + k \le n^2 + k^2 - 2nk$   
 $\frac{k}{j=1} n_1^2 - 2(n_j + n_j + ... + n_k) + n_j = 2n_j - n_j - ... = 2n_j - n_j - ...$ 

**Discrete Mathematics** 



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**DEPARTMENT OF MATHEMATICS** 

Maximum No. of edges of G  

$$= \frac{k}{1=1} \frac{p_{1}(p_{1}-1)}{2}$$

$$= \frac{k}{1=1} \frac{p_{1}^{2}(p_{1}-1)}{2}$$

$$= \frac{k}{1=1} \frac{p_{1}^{2}-p_{1}}{2}$$

$$= \frac{k}{2} \left[ \frac{k}{1=1} p_{1}^{2} - \frac{k}{1=1} p_{1}^{2} \right]$$

$$= \frac{k}{2} \left[ p_{1}^{2} + k_{1}^{2} - 2bk + 2b - k - h \right]$$

$$= \frac{1}{2} \left[ p_{1}^{2} - n + k_{1}^{2} - k - 2bk + 2n \right]$$

$$= \frac{1}{2} \left[ p_{1}^{2} - n + k_{1}^{2} - k - 2bk + 2n \right]$$

$$= \frac{1}{2} \left[ p_{1}^{2} - n + k_{1}^{2} - k - 2bk + 2n \right]$$

$$= \frac{1}{2} \left[ (n - k)^{2} + (n - k) \right]$$
Savdinum No.  

$$= \frac{1}{2} \left[ (n - k)^{2} + (n - k) \right]$$
The avean 5:  
Reave and 5:  
Reave that a simple graph with n vertices and has  
more than (n-1)(n-2) edges.  
To prove of is a connected.  
Suppose a is not connected.  
Buppose a is not connected.  
By them: H, a simple graph with n vertices  
and k compenents can have at most  

$$\frac{1}{2} (n - k) (n - k + 1)$$

$$1E(6n) = \frac{1}{2} (n - 2) (n - 2 + 1)$$

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$$1E(6n) = \frac{1}{2} (n - 2) (n - 2) which is a
Hence, G is connected.$$