

SNS COLLEGE OF TECHNOLOGY (AN AUTONOMOUS INSTITUTION) COIMBATORE- 35



DEPARTMENT OF MATHEMATICS

UNIT II-COMBINATORICS

PIGEONHOLE PRINCIPLE

Strong induction [Second prantiple of mathematical In the form, we use the same bashe Stop as before, but we use a different Inductive step.

i). Assume that P(j) is tout too j=12, ..., to

ii) we have to prove that P(K+1) is true

well oskling peroposity:

Every honempty set of non-negative integers . has a least element.

Pigeonhole psunciple

If (n+1) pigeon occupies n holes then at least one hole has more than the prigeon

Assume that those are (14) pfigeons and n holes. To prove atteast one hole has more than one pigeon. we prove this by method of contradiction.

Suppose not, atleast one hole has not more than

From 1898 each and every hope has exactly one progeon. one pageon. Stra those are in holes, which implies we have totally n phycons which is a contradiction to own

Hence atleast one hope has more than one pageon. assumption.

bioneralizzed prigeonbole prévilple

If 'm' pigeon occupies in holes then atleast one hole has more than $\left[\frac{m-1}{n}\right]$ to property.

Home [x] denotes the greatest entegen 10% than on equal to x, which is a Heal number.

Scanned with CamScanner

(Hot) (Hot)



SNS COLLEGE OF TECHNOLOGY (AN AUTONOMOUS INSTITUTION) COIMBATORE- 35



DEPARTMENT OF MATHEMATICS

UNIT II-COMBINATORICS

PIGEONHOLE PRINCIPLE

1. Show that among 100 people, atleast 12,06 them word born in the same month. m = number of projects = No. of people = 100 n = No. of Holos = No. of month = 12 By appenalized PHP, $\int \frac{m-1}{n} + t$ $= \left[\frac{100-1}{12}\right] + = 9 \quad \text{worle born 9n the tame month.}$

a). Show that of an alletionariles on a laborary contain a total of 40,325 pages, then one of the electronagues must have atleast 1614 pages.

No. of pageons: m = No. of pages = 40,325 No. of holos: n = No. of dectionwiles = 25 By Generalizzed PHP,

Y Generalizated PHP3
$$\left[\frac{m-1}{n}\right]+1 = \left[\frac{40,325-1}{25}\right]+1$$

$$= 1614 \text{ Pages 9n the disctionances}$$

I show that In a group of 6 people, at least 3 must be mutual follends (OH) alleast 3 must be strangers.

I show that of 7 word are used to paint 50 bacycles, atleast 8 bacycles wall be the same m = ND of Colored = 7 D = ND of Colored = 7colows.

By Generalized PHP, $\left[\frac{m-i}{n}\right] + 1 = \left[\frac{50-i}{7}\right] + 1$ = 8 braycles will be the Same colous.

Scanned with CamScanner