



1) Factors & Multiples:

if a number divides another number
a is a factor of b.

H.C.F. \rightarrow two or more numbers.

greatest number divides each of them
exactly.

- 1) Factorisation \rightarrow express each one of given numbers as product of Prime factors
- 2) Division

\rightarrow
H.C.F of 2 numbers.

Divide Larger no
Smaller one. & divide the division
by remainder.

repeat the process till
Zero.

H.C.F of 2 or more numbers.

\rightarrow H.C.F of 2 num & 3rd num \rightarrow 3 Values

- 2) Product of 2 numbers = Product of H.C.F & L.C.M.
- 3) Co-Primes \rightarrow if their H.C.F is 1 then it is co-prime
- 4) H.C.F of Fractions
 - 1) H.C.F = $\frac{\text{H.C.F of Numerator}}{\text{L.C.M of Denominator}}$



1) Find H.C.F of $2^3 \times 3^2 \times 5 \times 7^4$, $2^2 \times 3^6 \times 5^2 \times 7^6$,
 $2^3 \times 5^3 \times 7^2$

$$\text{H.C.F} = 2^2 \times 5 \times 7^2 = 980.$$

2) Find H.C.F of 108, 288, 360.

108 =

$$\begin{array}{r} 2 \mid 108, 288, 360 \\ 2 \mid 54, 144, 180 \\ 3 \mid 27, 72, 90 \\ 3 \mid 9, 24, 30 \\ \hline 3, 8, 10 \end{array}$$

$$= 2 \times 2 \times 3 \times 3 = 36.$$

3) find H.C.F of 513, 1134 & 1215.

$$\begin{array}{r} 1 \\ 1134 \overline{) 1215} \\ \underline{1134} \end{array}$$

$$\begin{array}{r} 81 \overline{) 1134} \quad 14 \\ \underline{81} \end{array}$$

$$\begin{array}{r} 324 \\ 324 \\ \hline 0 \end{array}$$

H.C.F of 1134 & 1215
is 81.

H.C.F of 513 & 81

$$\begin{array}{r} 6 \\ 81 \overline{) 513} \\ \underline{486} \quad 3 \\ 27 \overline{) 81} \\ \underline{81} \\ 0 \end{array}$$

H.C.F = 27.



5) $2^2 \times 3^3 \times 5 \times 7^2 \times 11$, $2^3 \times 3^2 \times 5^2 \times 7^4$, $2 \times 3 \times 5^3 \times 7 \times 11$

L.C.M \Rightarrow Product of Power highest power

6) L.C.M of 72, 108 & 2100.

= 37800

7) $\frac{2}{3}$, $\frac{8}{9}$, $\frac{16}{81}$, $\frac{10}{27}$

H.C.F = $\frac{\text{H.C.F of } 2, 8, 16, 10}{\text{L.C.M of } 3, 9, 81, 27} = \frac{2}{81}$

L.C.M = $\frac{\text{L.C.M of } 2, 8, 16, 10}{\text{H.C.F of } 3, 9, 81, 27} = \frac{80}{3}$

8) H.C.F & L.C.M of 0.63, 1.05 & 2.1.

63, 105, 210.

H.C.F of 63, 105, 210 = 21. \Rightarrow 0.21,

L.C.M of 63, 105, 210 = 630.

9) 2 numbers are in ratio 15:11 if H.C.F is 13.

find numbers.

Req numbers be $15x$ & $11x$.

Then their H.C.F is 13

10) H.C.F of 2 number is 11 & L.C.M is 693
if one number 77 find other

$$\text{other no} = \frac{11 \times 693}{77} = 99.$$

11) Find the least number divisible by 6, 7, 8, 9 & 12
leaves the remainder 1 in each case.

$$\text{Req. no} = \text{L.C.M of } (6, 7, 8, 9, 12) + 1.$$

3	6	7	8	9	12
2	2	7	8	3	4
2	1, 7, 4, 3, 2				
1, 7, 2, 3, 1					

$$3 \times 2 \times 2 \times 7 \times 2 \times 3 = 504.$$

$$\text{required number} = 504 + 1 = 505.$$

12) Find least number exactly divisible by
12, 15, 18, 20 & 27.

= L.C.M of given numbers

3	12, 15, 20, 27
4	4, 5, 20, 9
5	1, 5, 5, 9
1, 1, 1, 9	

$$= 3 \times 4 \times 5 \times 9 = 540.$$



Find largest no of 4 digits exactly divisible by
12, 15, 18 & 27?

L.C.M = 540, as calculated.

Largest 4 digit " 9999

$$\Rightarrow \frac{9999}{540} = \text{Remainder } 279.$$

$$9999 - 279 = \boxed{9720}.$$



Remainder = 279

L.C.M of (12, 15, 18, 27) = 540