



UNIT 2 FOURIER SERIES HARMONIC ANALYSIS

Harmonic Analysis The Process of finding the publics serves for a function quien by numerical values is known as harmonic enalysis. Formula. > * your or I your or Reque form: f(x)= ao + Z an cosnx + Z bn sinnx $a_0 = a\left(\frac{\Sigma y}{1}\right)$ $a_n = 2\left(\frac{\sum y \cos n}{N}\right) \Rightarrow a_n = 2\left(\frac{\sum y \cos n}{N}\right)$ $a_2 = 2 \left(\frac{\sum y \cos 2\pi}{N} \right)$ and so on. $b_n = 2\left(\frac{\sum y \sin nx}{N}\right) \Rightarrow b_1 = 2\left(\frac{\sum y \sin x}{N}\right)$ b2=2(IYSM2X) and so on. = 1 form: $f(x) = \frac{\alpha p}{2} + \sum_{n=1}^{\infty} \alpha n \cos \frac{n \pi x}{k} + \sum_{n=1}^{\infty} b n \sin \frac{n \pi x}{k}$ $a_0 = 2 \begin{pmatrix} \Xi y \\ N \end{pmatrix}$; $a_n = 2 \underbrace{\Xi y \operatorname{cosh} \pi \alpha}_{N}$; $b_n = \underbrace{\Xi y \operatorname{sin} n \pi \alpha}_{N}$ $a_1 = 2 \frac{\sum y \cos \pi x}{L}$ $b_1 = 2 \frac{\sum y \sin \pi x}{N}$ $a_2 = 2 \frac{\sum y \cos 2\pi x}{k}$ $b_2 = 2 \frac{\sum y \sin 2\pi x}{N}$





1. Find the fourier serves expansion defined in (0, T)						
by means of the table values quien below. find the						
sources upto the 2 nd harmonic.						
tsec 0 716 713 712 2713 57/6 T						
A temp. 1.98 1.30 1.05 1.30 -0.88 -0.25 1.98						
Setu:						
Esec O I T3 I 2 5T						
A temp 1.98 1.30 1.05 1.30 -0.88 - 0.25						
N = Number of terms = 6						
$T = 2\pi = 360$						
$2l = 2\pi \Rightarrow l = \pi$						
$2l = 2\pi \Rightarrow l = \pi$ $\therefore f(\pi) = \frac{\alpha_0}{2} + \frac{5}{n=1} \alpha_n (\alpha_0 \frac{n\pi x}{2}) + \frac{5}{5} b_n \sin\left(\frac{n\pi x}{2}\right)$						
$= \frac{\alpha_0}{2} + \frac{\beta_0}{2} \frac{\alpha_0}{n^{2}} \alpha_$						
Upto 2nd poamonic.						
$f(x) = \frac{a_0}{2} + a_1 \cos x + a_2 \cos 2x + b_1 \sin x + b_2 \sin 2x$						
Sub T=27 in the table						
tsec 0 60 120 180 240 300						
Atemp 1.98 1.30 1.05 1.30 -0.88 -0.25						



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(ral in his	and the state	the second				
Xart.	y==={(x)	y cosse	ycoszx	ysinx	ysin22		
0	1.98	1.98	1.98 1.98 1.000 2.000	* 2 6 p	tracon Re		
60 -	1.30	0.65	-0.65	-	-0.909		
120	1.05	-0.525	-0.525	0.9090	- 95 B		
180	1.30	-1-3	1.3	0.762	0 -0.762		
240	- 0.88	0.44	0.125	0.217	0. 217		
300	-0.25	-0.125 Sylasx	5.120	Zysinx	545027		
	ΣΥ = 4.5	= 1.12	= 2.67	= 3.014	=-0.322		
$a_0 = 2 \frac{\Sigma y}{N}$ $a_1 = 2 \frac{\Sigma y \cos x}{N}$ $a_2 = 2 \frac{\Sigma y \cos 2x}{N}$							
$= 2\left(\frac{45}{6}\right) = 2\left(\frac{1\cdot12}{6}\right) = 2\left(\frac{2\cdot57}{6}\right)$							
$a_0 = 1.5$ $a_1 = 0.373$ $0.2 = 0.89$							
$b_1 = \alpha \left(\frac{\sum y \sin x}{N} \right) \qquad b_2 = \alpha \left(\frac{\sum y \sin 2x}{N} \right)$							
$= 2\left(\frac{3.014}{6}\right) = 2\left(\frac{-0.328}{6}\right)$							
$b_1 = 1.005$ $b_2 = -0.109$							
$f(x) = \frac{a_0}{2} + a_1 \cos x + a_2 \cos 2x + b_1 \sin x + b_2 \sin 2x$							
= 0.75 + 0.373 005 x + 0.89 0052x + 1.005 sinx							
- 0.1095022							



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2. Find	One	forse	series	upto	Secon	d harmonie	for the
follad	following data						
×	0	BUR	SILE	x	4713	जा3	27
=(x)	1.0	1.4	1.9	1,4	いち	1.2	<i>۱</i> , D,
Soln N=6							
$2l = 2x \neq l = x$ $f(x) = \underbrace{ao}_{2} + \underbrace{\tilde{\Sigma}}_{1} a_{1} \cos x + \underbrace{\tilde{\Sigma}}_{2} b_{1} \sin x$ $f(x) = \underbrace{ao}_{2} + \underbrace{a_{1}}_{1} \cos x + a_{2} \cos x + b_{1} \sin x + b_{2} \sin 2x$							
\$(x)	100 00	2+ a1	cosx + a:	2 (194	B UE	tone all.	JARGONDIE - REC
x	y	= {(2)	reary 5	4 9	(082×	ysink	ysin2x
D	١	σ,	5 1 0	2	82	uc 0 81	00
60° 0	»> ,5. 1	·4	0.7		-0.7 (0.866 1.212	1.212
120	-0.51	.9	-0.95		-0.95).866 1.645	-1.645
081	-1 1.	. 7	-1.7		(, 1	0 0	D
240-	-0.5 1	.6	-0.45		- 0.45-	0.8641.299	1.299
300	0-5 1	.2	0.6		-0.6-0	.866 -1.039	-1.039
	Σy		Sy coost		ycos2x	Zysine	Iysin2R
	1 -	8.1	= -1.1	=	03	= 0.5196	=-0.1732
$a_b = g\left(\frac{sy}{N}\right) = g\left(\frac{g\cdot 7}{b}\right) = g\cdot 9$							
$a_1 = 2\left(\frac{\sum y (\text{DSX})}{N}\right) = 2\left(\frac{-1 \cdot 1}{6}\right) = -0 \cdot 37$							





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 $a_{2}=2\left(\frac{5}{N}+\frac{9(0329)}{6}\right) = 2\left(\frac{-0.3}{6}\right) = -0.1$ $b_{1}=2\left(\frac{5ysinn}{N}\right)=2\left(\frac{0.5196}{6}\right)=0.17$ $b_2 = 2\left(\frac{\Sigma Y S U N Z N}{N}\right) = 2\left(\frac{-0.1732}{b}\right) = -0.06$ 3. find the fourier series as for as the second hamonic to represent the function given in the following data × 0 ١ 2 2 5 4 Ч 9 18 24 20 28 26 Seln: N=b 21=6 = L=3 $f(x) = \frac{\alpha_0}{2} + \frac{\beta}{2} \alpha_1 \cos\left(\frac{\alpha x x}{3}\right) + \frac{\beta}{n=1} bn \sin\left(\frac{\alpha x x}{3}\right)$ $= \frac{a_0}{2} + \alpha_1 \cos\left(\frac{\pi x}{3}\right) + \alpha_2 \cos\left(\frac{2\pi x}{3}\right) + b_1 \sin\left(\frac{\pi x}{3}\right)$ $+b_2 s \Im \left(\frac{2\pi x}{3}\right)$



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×	y=\$(x)	4005 xx	ycos 272	ysin nr	y 608 2××			
D	D	9	anor 3MAI	0	O			
١	18	9	-9	1050 7	15.6			
2	24	-18	-24	20.9	0			
3	28	- 28	28	D	O			
4	26	-13	-13	-22.6	22.6			
5	20	10	-10	-17.4	-17.4			
	Σy	Σy cos(<u>xx</u>)	Σy cos (27x)	Ey sin (AT)	Sysin (25x)			
			-19 Jo -19	2745 ³⁻⁴ or	= 20.8 .1			
	$a_0 = a(\frac{5y}{N}) = 2(\frac{125}{6}) = 41.66$							
$Q_{1} = 2\left(\frac{\Sigma Y \log(n \times 13)}{N}\right) = 2\left(\frac{-25}{5}\right) = -8.33$								
$a_2 = 2\left(\frac{5y\cos(2\pi x)}{N}\right) = 2\left(\frac{-19}{6}\right) = -6.33$								
$b_1 = 2\left(\frac{2}{N}\frac{y\sin(\frac{\pi x}{3})}{N}\right) = 2\left(\frac{-3.4}{6}\right) = -\frac{3.4}{5}$								
$b_{2} = 2\left(\frac{2y \sin(\frac{2xx}{3})}{N}\right) = 2\left(\frac{20.8}{6}\right) = 0.009$								
$(x) = 20.83 - 8.33 \cos(\frac{xx}{3}) - 6.33 \cos(\frac{2xx}{3})$								
- 1.33 sin (xx) + 0.009 sin (2.7x)								