

(An Autonomous Institution) Coimbatore-641035.



UNIT 3- GRAPHS

Euler and Hamilton Graphs

Euler Graph and Hangitton Graph: Euler an path:

A path of a graph G B called an Eulerian path. If it contains each edge of the graph exactly once.

Eulerian corcult (09) Eulerian cycle:

A circult on cycle of a graph G is called an Eulerian concelle on cycle, of graph G is called an edge of G exactly once and starting and ending Points are same.

Eulerian graph: Any graph containing an Eulerian curcuit or cycle: is called an Eulerian graph. Note: A connected graph is Euler if each of its voritices is of Hamiltonian Graph: Hamiltonian path:

A path of a graph 61 is called a Hamiltonian Path, if it indudes each vertex of 61 exactly once Hamiltonian concult on cycle

A circuit of a graph G is called a Hamiltonian concurt (cycle) of it includes each vertex of G exactly once, except the starting & ending vertices.

Hansi Honsan graph:

Any graph containing a Hamiltonian concert on cycle is called a Hamiltonian graph.

T Cave an example of a graph which be

- 1). Eulergan but not Hangitongan
- ii). Hampittongan but not Eulerlan
- iii) Both Eulertian and Hameltongan
- iv). Non Eulercian and Non Hameltongan.

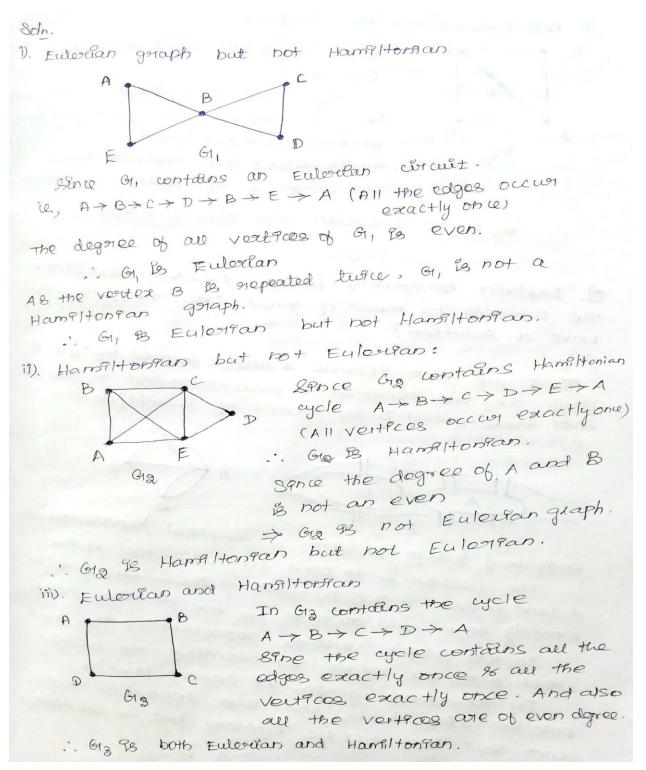


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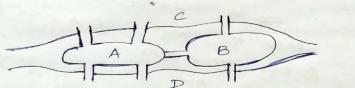
D

iv). Non-Eulerian and Non-Hampitonsan: A $M = \int_{G_{4}}^{B} B = G_{4}$ As the vertex B 95 stepeated twice, H = g = 1 aph 3 = 0 c + 1 c

GIL 18 NON-Eulerian and non-Ham9/tongan.

2]. Explain Kongeberg buildge problem. Represent the problem by mean of graph. Does the problem bave a solution?

Sol<u>n</u>. There are two followeds A and B formed by a lifer. They are connected to each other and to the lifer tanks c and D by means of 7- bildges.



Kongsbeig Budge publiens Graphical Representation The public is to start from any one of the 4 land areas A, B, C, D walk a corose couch budge exactly once and stetuen to the starting point. In this graph, vertices representing the land areas and the edges representing the bridges. In the above graph, we cannot tind a Eweran would be dege repeated twice Hence Kongebeig budge Public bas no solution.



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S. Fond all possible Eulergan Path and Eulerean
ayole of the gun. graph. Is it Euler graph?
A PI 9 B Posseble Euler paths:
$0 \rightarrow A \rightarrow D$
e_{μ} e_{5} e_{1} b_{2} b_{3} b_{4} c_{4} b_{5} b_{7} b_{7
THE READER CARDY D
$0 \stackrel{0}{\stackrel{\circ}{3}} \stackrel{0}{iv} D \rightarrow C \rightarrow B \rightarrow A \rightarrow D \rightarrow B$
$\forall D \to B \to C \to D \to A \to B$
$VIJ. D \rightarrow A \rightarrow B \rightarrow C \rightarrow D \rightarrow B$
Euler cycles: i) $B \rightarrow D \rightarrow C \rightarrow B \rightarrow A \rightarrow D \rightarrow B$
$\begin{array}{c} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 $
$\begin{array}{c} \text{if} & B \rightarrow C \rightarrow D \rightarrow T \\ \text{if} & B \rightarrow A \rightarrow D \rightarrow C \rightarrow B \rightarrow D \rightarrow B \end{array}$
$\mathcal{W} \to \mathcal{V} \to \mathcal{B} \to \mathcal{A} \to \mathcal{D} \to \mathcal{B} \to \mathcal{D}$
$V \to B \to C \to D \to A \to B \to D$
$VI) D \to A \to B \to C \to D \to B \to T$
and a pot a Euler graph.
is siterian both and Handitonian cycle, if it
AJ. Find thronthoused of the graphs given below. Also identify
which graph is Hansiltonstan. B
A D
POSSEble Hamiltonnan paths: posseble Hamilton an cycles:
i). $A \rightarrow B \rightarrow C \rightarrow D$ j. $A \rightarrow B \rightarrow C \rightarrow D \rightarrow A$
ii) $A \rightarrow D \rightarrow C \rightarrow B$ ii) $A \rightarrow D \rightarrow C \rightarrow B \rightarrow A$
$\begin{array}{c} \text{iii} & B \rightarrow C \rightarrow D \rightarrow A \\ \text{iii} & B \rightarrow C \rightarrow D \rightarrow A \rightarrow B \\ \end{array}$
iV , $B \rightarrow A \rightarrow D \rightarrow A$ iM , $B \rightarrow A \rightarrow D \rightarrow A \rightarrow B$
$\begin{array}{cccc} V & C \rightarrow D \rightarrow A \rightarrow B & & \\ V & C \rightarrow B \rightarrow A \rightarrow D & & \\ V & C \rightarrow B \rightarrow A \rightarrow D & & \\ V & C \rightarrow B \rightarrow A \rightarrow D & \\ \end{array}$
$\begin{array}{cccc} V_{1} & C \rightarrow B \rightarrow A \rightarrow D & V_{1} & C \rightarrow B \rightarrow A \rightarrow D \rightarrow C \\ V_{1} & D \rightarrow A \rightarrow B \rightarrow C & V_{1} & D \rightarrow A \rightarrow B \rightarrow C \rightarrow D \end{array}$
$V_{111}^{(11)} D \rightarrow C \rightarrow B \rightarrow A \qquad V_{111}^{(11)} D \rightarrow C \rightarrow B \rightarrow A \rightarrow D$
Gun. graph & Hangitonsan graph.