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DEPARTMENT OF MATHEMATICS

Problems:
J. Show that the set
$$G_1 = \frac{1}{2} 1, -1, \frac{1}{5} - \frac{1}{3}$$
 consulting
of the gibs roots of usity is a commutative
placy under mattriprotection.
Sta:
Now Hipprotection (cayley) Table
* 1 -1 i -i
1 1 -1 i -i
-1 -1 i -i
i i -i -1 1
-i -i i 1 -1
). Closwie: Now $1, -1 \in G_1$, $+1 + -1 = -1 \in G_1$
 $\therefore G_1$ is closed.
i). Associative: $1, -1, i \in G_1$ ($1 + -1$) + $i = -i \in G_1$
 $1 + (-1 + i) = -i \in G_1$
 $1 + (-1 + i) = -i \in G_1$
 $1 + (-1 + i) = -i \in G_1$
 $1 + (-1 + i) = -i \in G_1$
 $1 + (-1 + i) = -i \in G_1$
 $1 + 1 = 1, -1 + 1 = 1, i + 1 = i, -i + 1 = i$
 $\therefore 1 \le +2 = Glestifty est.$
N). Inverse est.:
Inverse of $1 \le 1$ i.e. $1 + 1 = i \in G_1$





SNS COLLEGE OF TECHNOLOGY (An Autonomous Institution) Approved by AICTE, New Delhi, Affiliated to Anna University, Chennai Accredited by NAAC-UGC with 'A++' Grade (Cycle III) & amp; Accredited by NBA (B.E - CSE, EEE, ECE, Mech & amp; B.Tech.IT) COIMBATORE-641 035. TAMIL NADU **DEPARTMENT OF MATHEMATICS** 1040190 of i 28 -i ie. ix-i=1EG Inverse of -1 18 1 ce, -i+i=1EG y). commutative: $i_j - i \in G_i$ $i \neq -i = i \in G_i$ 「チョニャモム => 『* -] = - 『* " ... GI & commutative group under multiplication. 2], Peove that the set A = 71, w, wight an Vabellan gloup of order 3 under usual multiplication where 1,00, w? are cube loots of with y and $\omega^3 = 1$ $1 \omega \omega^2$ Soln. composition table 1, 2 2 www. $\omega^2 \omega^2 | \Omega$ All the ett. 90 the above table are the i). closure: elts. of A. Hence A is closed under moultiplication ii). A-880 Gatque : (1*w) * 0 = 0 = 1 EA 1 * (2 * 2 = 2 = 2 = 1 = A It satteftes the associative property. (1* co) * w2 = 1* (co * co2) iii). Identify elt. : 1, w, we EA $1*1=1, 1*\omega=\omega, \omega^{2}*1=\omega^{2}$) is the identify elt. of A iv). Inverse elt. Inverse of 1 38 1 20, 1+1=1 EA ω is ω^2 ie., $\omega + \omega^2 = \omega^3 = 1 E A$ $\omega^2 \frac{1}{12} \omega \frac{1}{12}, \omega^2 \star \omega = \omega^3 = 12 A$





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V). commutative : 1 * 00 = 00 & A W#1 = WE A Hence (A, +) is an abelgan group 3]. Let I be the set of integers. Let Zon be the Set of equivalence classes generated by the equivalence relation " congracence modulo m" tor any the Portages in. There (Zm, tm) and (Zm, Ym) are monords. Soln. FOR [1], [j] E Zm a). the is defined as [i] + [j] = [i+j) (mod m)] b). Xm & defend as [i] xm[j]=[(1xj) (mod m)] The composition table for m= 5 is given as $(Z_{5}, +_{5})$ (Z_{E}, Y_{E}) 0 1 2 3 4 ナト XEOIQ 3 4 0 1 2 3 4 0 0 0 0 0 0 0 1 2 3 4 1 Ð 1 0 1 2 3 4 2340 1 2 2 0 2 4 1 3 3401 2 3 0 3 1 4 3 2 012 3 4 4 0 4 4 3 2 - 1 1). closure proporty: In the above table (Z5, t5) and (Z5, X5 Sat78703 closure proporty. ii). Assocrative: clearly, (75, +5) and (75, ×5) satisfies association proporty. in, Identity ett. : TOJ 33 the identity elt. w.r. to LIT 38 the





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i). For a, be $a^{\dagger} \Rightarrow a \neq b = ab e a^{\dagger}$

ii). For a, b, c
$$\in a^+$$
. Then $a * (b * c) = a + \frac{bc}{a}$

$$a * b) * c = abc \rightarrow abc$$

Forom (1) and (2),

$$q * (b*c) = (a*b)*c$$

$$\frac{ae}{a} = a = e = a$$

iv). Invoyage elt: Let a & a⁺. Then Jaiea⁺ such that

$$\frac{aa^{-1} = e}{aa^{-1} = a} \Rightarrow a^{-1} = \frac{4}{a}$$

V). commutative: Let $a, b \in a^{+}$. Then $a \neq b = \frac{ab}{a}$ and $b \neq a = \frac{ba}{a}$





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