



# SNS COLLEGE OF TECHNOLOGY

Coimbatore-35  
An Autonomous Institution



Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A+' Grade  
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## VQAR 1- QUANTITATIVE APTITUDE AND REASONING

II YEAR/ III SEMESTER

UNIT 1 – QUANTITATIVE ABILITY I

TOPIC – Square and Cube Roots



# Algebra 2: Unit 8



## Roots and Radicals

Square and Cube Roots/ VQAR-1/M.Divya/ECE/SNSCT



## Roots and Radicals

Radicals (also called **roots**) are directly related to exponents.



## Roots and Radicals

The simplest types of radicals are **square roots** and **cube roots**.

Radicals beyond square roots and cube roots exist, but we will not discuss them as in depth.



## Roots and Radicals

The **rules** for radicals that you will learn **work for all radicals** – not just square roots and cube roots.



## Roots and Radicals

The symbol used to indicate a root is the radical symbol -  $\sqrt{\quad}$



## Roots and Radicals

Every radical expression has three parts...

- Radical symbol
- Index
- Radicand



## Roots and Radicals

Every radical expression has three parts...

The diagram shows the expression  $\sqrt[2]{49}$ . Three red arrows point to its components: one from the word "Index" to the number 2, one from the word "Radical" to the radical symbol  $\sqrt{\quad}$ , and one from the word "Radicand" to the number 49.





## Roots and Radicals

The **index** of a radical is a **whole number** greater than or equal to 2.



## Roots and Radicals

The index of a square root is always 2.



## Roots and Radicals

By convention, *an index of 2 is not written* since it is the smallest possible index.



## Roots and Radicals

The square root of 49 could  
be written as  $\sqrt[2]{49}$  ...

but is normally written as  $\sqrt{49}$  .



## Roots and Radicals

plural of index

All indices greater than 2 must be written.

The index of a cube root is always 3.



## Roots and Radicals

The cube root of 64 is written as  
 $\sqrt[3]{64}$  .



## Roots and Radicals

What does square root mean?

What does cube root mean?



## Roots and Radicals

The **square root** of a number (or expression) is another number (or expression)...

...which when multiplied by itself (squared) gives back the original number (or expression).





## Roots and Radicals

The **cube root** of a number (or expression) is another number (or expression) ...

...which when multiplied by itself three times (cubed) gives back the original number (or expression).



## Roots and Radicals

### Example:

$$\sqrt{49} = 7 \quad \text{because} \quad 7 \cdot 7 = 7^2 = 49$$

### Also

$$\sqrt{49} = -7 \quad \text{because} \quad (-7)(-7) = (-7)^2 = 49$$



## Roots and Radicals

### Example:

$\sqrt{49}$  has two answers:

7 is called the positive or **principal square root**.

-7 is called the negative square root.



## Intermediate Algebra MTH04



### Roots and Radicals

**Example:**

$$\sqrt[3]{64} = 4 \text{ because } 4 \cdot 4 \cdot 4 = 4^3 = 64$$

$$\sqrt[3]{-64} = -4 \text{ because}$$

$$(-4)(-4)(-4) = (-4)^3 = -64$$



## Roots and Radicals

**What are the first 10 whole numbers that are perfect squares?**

$1^2, 2^2, 3^2, 4^2, 5^2, 6^2, 7^2, 8^2, 9^2, 10^2$

**1, 4, 9, 16, 25, 36, 49, 64, 81, 100**



## Roots and Radicals

**What are the first 10 whole numbers that are perfect cubes?**

$1^3, 2^3, 3^3, 4^3, 5^3, 6^3, 7^3, 8^3, 9^3, 10^3$

**1, 8, 27, 64, 125, 216, 343, 512, 729, 1000**



## Roots and Radicals

If a number is a **perfect square**, then you can find its **exact square root**.

A **perfect square** is simply a number (or expression) that can be written as the **square** [raised to 2<sup>nd</sup> power] of another number (or expression).



## Roots and Radicals

### Examples:

$$16 = 4^2$$

$$25 = 5^2$$

$$1.44 = 1.2^2$$

$$\frac{9}{121} = \left(\frac{3}{11}\right)^2$$

principal square root

$$\sqrt{16} = 4$$

$$\sqrt{25} = 5$$

$$\sqrt{1.44} = 1.2$$

$$\sqrt{\frac{9}{121}} = \frac{3}{11}$$





## Roots and Radicals

### Examples:

$$36b^2 = (6b)^2$$

$$m^6 = (m^3)^2$$

principal square root

$$\sqrt{36b^2} = 6b$$

$$\sqrt{m^6} = m^3$$



## Roots and Radicals

If a number is a **perfect cube**, then you can find its **exact cube root**.

A **perfect cube** is simply a number (or expression) that can be written as the **cube** [raised to 3<sup>rd</sup> power] of another number (or expression).



## Roots and Radicals

**Examples:**

$$64 = 4^3$$

$$125 = 5^3$$

$$1.728 = 1.2^3$$

$$\frac{216}{125} = \left(\frac{6}{5}\right)^3$$

**principal cube root**

$$\sqrt[3]{64} = 4$$

$$\sqrt[3]{125} = 5$$

$$\sqrt[3]{1.728} = 1.2$$

$$\sqrt[3]{\frac{216}{125}} = \frac{6}{5}$$



## Roots and Radicals

### Examples:

$$8c^3 = (2c)^3$$

$$m^6 = (m^2)^3$$

$$-27y^{12} = (-3y^4)^3$$

principal cube root

$$\sqrt[3]{8c^3} = 2c$$

$$\sqrt[3]{m^6} = m^2$$

$$\sqrt[3]{-27y^{12}} = -3y^4$$



## Roots and Radicals

**Not all numbers or expressions have an exact square root or cube root as in the previous examples.**



## Roots and Radicals

If a number is **NOT** a perfect square, then you **CANNOT** find its **exact square root**.

If a number is **NOT** a perfect cube, then you **CANNOT** find its **exact cube root**.

You can **approximate** these square roots and cube roots of real numbers with a **calculator**.



## Roots and Radicals

### Examples:

$$\sqrt{40} \approx 6.325$$

$$\sqrt{135} \approx 11.619$$

$$\sqrt[3]{40} \approx 3.42$$

$$\sqrt[3]{74} \approx 4.198$$



## Roots and Radicals

If a number is **NOT** a perfect square, then you might also be able to **SIMPLIFY** it.

What is the **process** to simplify a square root?





## Roots and Radicals

If the expression is not a perfect square ...

1. see if you can **rewrite** the expression as a **product** of two smaller factors...
2. where **one of the factors is a perfect square.**



## Roots and Radicals

3. Then, **extract** the the square root of the factor that is a perfect square ...
4. **and multiply that answer times the other factor still under the radical symbol.**



## Roots and Radicals

### Examples – Simplifying Square Roots:

perfect square

$$\sqrt{40} = \sqrt{4 \cdot 10} = 2\sqrt{10}$$

$$\sqrt{135} = \sqrt{9 \cdot 15} = 3\sqrt{15}$$

$$\sqrt{50x^7} = \sqrt{25x^6 \cdot 2x} = 5x^3\sqrt{2x}$$



## Roots and Radicals

If a number is **NOT** a perfect cube, then you might also be able to **SIMPLIFY** it.

What is the **process** to simplify a cube root?



## Roots and Radicals

If the expression is not a perfect cube ...

1. see if you can **rewrite** the expression as a **product** of two smaller factors...
2. where **one of the factors is a perfect cube.**



## Roots and Radicals

3. Then, **extract** the the cube root of the factor that is a perfect cube...
4. **and multiply that answer times the other factor still under the radical symbol.**



## Roots and Radicals

### Examples – Simplifying Cube Roots:

perfect cube

$$\sqrt[3]{80} = \sqrt[3]{8 \cdot 10} = 2\sqrt[3]{10}$$

$$\sqrt[3]{405} = \sqrt[3]{27 \cdot 15} = 3\sqrt[3]{15}$$

$$\sqrt[3]{24x^8} = \sqrt[3]{8x^6 \cdot 3x^2} = 2x^2\sqrt[3]{3x^2}$$



## Roots and Radicals

**Not all square roots can be simplified!**

**Example:**  $\sqrt{77}$

**cannot be simplified!**

- **77 is not a perfect square ...**
- **and it does not have a factor that is a perfect square.**

Square and Cube Roots/ VQAR-1

Square and Cube Roots/ VQAR-1/M.Divya/ECE/SNSCT