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DEPARTMENT OF MATHEMATICS

UNIT III DIFFERENTIAL CALCULUS

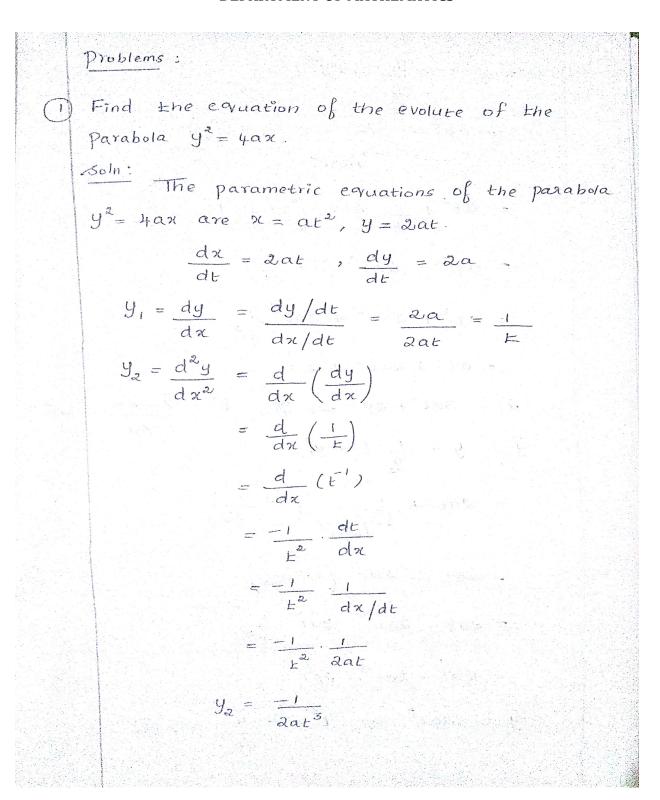
| | NO COMPANY OF A DESCRIPTION OF THE PROPERTY OF | | |
|--|--|---|---|
| | The locus of the centre of curvature of the given curve is called the evolute of the curve. Working procedure to find the evolute: 1. Write the parametric form of the given curve. 2. Find centre of curvature (x, y). 3. Eliminate the parameter from x and y 4. Taking locus of the above equation, we get the Required evolute. | | |
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| | Curve | Cartesian equation | Parametric equation |
| | Parabola | $y^2 = 4ax$ | |
| | to confirm the second | (2) x2 = 4ay | 2) n = 2at, y = at |
| | Ellipse | $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ | $x = a \cos \theta$, $y = b \sin \theta$ |
| | Ну рельога | $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ | x = a Seco, y = btano |
| The second secon | Rectangular hypesbola | $xy = c^2$ | x = ct, y = c |
| es in a control of the property of the control of t | Astroid | $n^{2/3} + y^{2/3} = a^{2/3}$ | $x = a \cos^3 \theta$, $y = a \sin^5 \theta$ |





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$$\begin{aligned}
\overline{x} &= x - \frac{y_1}{y_2} (1 + y_1^2) \\
&= at^2 - \frac{1/k}{-1/2at^3} \left(1 + \frac{1}{k^2}\right) \\
&= at^2 + \frac{1}{k} 2at^3 \left(1 + \frac{1}{k^2}\right) \\
&= at^2 + 2at^2 \left(1 + \frac{1}{k^2}\right) \\
&= at^2 + 2at^2 + 2a \\
\overline{\alpha} &= 3at^2 + 2a \implies \emptyset \quad t^2 = \overline{x} - 2a \\
\overline{y} &= y + \frac{1}{y_2} (1 + y_1^2) \\
&= 2at + \frac{1}{-1/2at^3} \left(1 + \frac{1}{k^2}\right) \\
&= 2at - 2at^3 \left(1 + \frac{1}{k^2}\right) \\
&= 2at - 2at^3 - 2at \\
\overline{y} &= -2at^3 \implies x^3 = -\frac{y}{2a} \implies x^3 = -\frac{y}{2a}
\end{aligned}$$



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