



DEPARTMENT OF MATHEMATICS

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- ① The Leslie model describes age-Specified Population growth, as follows. Let the oldest age attained by the females in some animal population be 9 years. Divide the population into three age classes of 3 years each. Let the Leslie matrix be,

$$L = l_{jk} = \begin{bmatrix} 0 & 2.3 & 0.4 \\ 0.6 & 0 & 0 \\ 0 & 0.3 & 0 \end{bmatrix}$$

- (i) What is the number of females in each class after 3, 6, 9 years if each class initially consists of 400 females?
- (ii) For what initial distribution will the number of females in each class change by the same proportion? What is this rate of change?

Solution:

$$\text{i) } X_3 = \begin{bmatrix} 1080 \\ 240 \\ 120 \end{bmatrix}, \quad X_6 = \begin{bmatrix} 600 \\ 648 \\ 72 \end{bmatrix}, \quad X_9 = \begin{bmatrix} 1519.2 \\ 360 \\ 194.4 \end{bmatrix}$$

$$\text{ii) } \lambda = 1.2, \quad X_1 = \begin{bmatrix} 1 \\ 0.5 \\ 0.125 \end{bmatrix}$$

Class I, II, III : 738, 369, 92