

1

## **SNS COLLEGE OF TECHNOLOGY**



(An Autonomous Institution) Approved by AICTE, New Delhi, Affiliated to Anna University, Chennai Accredited by NAAC-UGC with 'A++' Grade (Cycle III) & amp; Accredited by NBA (B.E - CSE, EEE, ECE, Mech & amp; B.Tech.IT) COIMBATORE-641 035, TAMIL NADU

DEPARTMENT OF MATHEMATICS

### UNIT II

ORTHOGONAL TRANSFORMATION OF A REAL SYMMETRIC MATRIX

Write the ordinatic form for the following  
matrix (i) 
$$\begin{bmatrix} 1 & 1 & -1 \\ 1 & 2 & 1 \\ -1 & 1 & 3 \end{bmatrix}$$
 (ii)  $\begin{bmatrix} 2 & 6 & -2 \\ 6 & 1 & -4 \\ -2 & -4 & -3 \end{bmatrix}$   
Soln:  
(i)  $A = \begin{pmatrix} a_{11} & a_{12} & a_{13} \\ (a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix} = \begin{pmatrix} 1 & 1 & -1 \\ 1 & 2 & 1 \\ -1 & 1 & 3 \end{pmatrix}$   
 $Q = a_{11} x_{1}^{2} + a_{22} x_{2}^{2} + a_{33} x_{3}^{2} + 2a_{12} x_{1} x_{2} + 2a_{23} x_{3} x_{3} + 2a_{31} x_{3} x_{1} + 2a_{23} x_{2} x_{3} + 2x_{1} x_{2} - 2x_{3} x_{1} x_{2} + 2x_{1} x_{2} - 8x_{2} x_{3} - 2x_{3} x_{1} + 2x_{1} x_{3} - 2x_{3} x_{3} - 2x_{3} x_{3} + 2x_{1} x_{3} - 2x_{3} x_{3} - 2x_{3} x_{3} + 2x_{1} x_{3} - 2x_{3} - 2x_{3} - 2x_{3} x_{3} - 2x_{3}$ 



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#### DEPARTMENT OF MATHEMATICS

Problems:  
Determine the nature of the following quadratic  
form 
$$x_1^2 + 2x_2^2$$
.  
Sola:  
Matrix of the quadratic form  

$$= \begin{pmatrix} (\omega c_b of x_1^2 + 2 \cos b of x_1 x_2 + \frac{1}{2} (\omega c_b of x_1^2) + \frac{1}{2} (\omega c_b of x_1 x_2) + \frac{1}{2} (\omega c_b of x_2 x_3) + \frac{1}{2} (\omega c_b of x_3 x_3) +$$



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DEPARTMENT OF MATHEMATICS

Index = number of positive sevare terms = 3  
Signature = Difference between positive and negative  

$$square terms$$
  
 $= 3-0 = 3$   
Nature = positive definite  
(ii)  $-y_1^2 + y_2^2 + 4y_3^2$   
 $rank = 3$   
Index = 2  
Signature =  $2 - 1 = 1$   
Nature = Indefinite  
(ii)  $3y_2^2 + 15y_3^2$   
 $= 0y_1^2 + 3y_2^2 + 15y_3^2$   
Tank = 2  
Signature =  $2$   
Nature = Positive Semi definite



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