

SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution) Approved by AICTE, New Delhi, Affiliated to Anna University, Chennai Accredited by NAAC-UGC with 'A++' Grade (Cycle III) & Accredited by NBA (B.E - CSE, EEE, ECE, Mech & B.Tech.IT) COIMBATORE-641 035, TAMIL NADU

DEPARTMENT OF MATHEMATICS

UNIT III DIFFERENTIAL CALCULUS

Evolute : The locus of the centre of curvature of the given curve is called the evolute of the curve. Working procedure to find the evolute: 1. Write the parametric form of the given curve . 2. Find centre of curvature (x, y) 3. Eliminate the parameter from \$ and \$ 4. Taking locus of the above equation, we get the required evolute. Curve Parametric equation Cartesian equation $i x = at^2, y = 2at$ $0 \quad y^2 = 4ax$ Parabola (2) $x^2 = 4ay$ $2 \mathcal{H} = aat, \mathcal{Y} = at^2$ $\frac{2c^2}{a^2} + \frac{y^2}{b^2} = 1$ Ellipse $\alpha = \alpha \cos \phi, \ y = b \sin \theta$ $\frac{\chi^2}{a^2} - \frac{y^2}{b^2} = 1$ $x = a \ Seco, \ y = b \ tano$ Hyperbola Rectangular 244= 2 x = ct, y = chypesbola Astroid $n^{2/3} + y^{2/3} = a^{2/3}$ $x = a \cos^3 \theta, y = a \sin^5 \theta$

23MAT101 - MATRICES AND CALCULUS

Ms.C.SARANYA/AP/Mathematics



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DEPARTMENT OF MATHEMATICS

Problems:
Trind the equation of the evolute of the parabola
$$y^2 = 4ax$$
.
Soln:
The parametric equations of the parabola $y^2 = 4ax$ are $x = at^2$, $y = 2at$.
 $\frac{dx}{dt} = 2at$, $\frac{dy}{dt} = 2a$.
 $\frac{dx}{dt} = \frac{dy}{dx}/dt = \frac{2a}{2at} = \frac{1}{E}$.
 $y_2 = \frac{d^2y}{dx^2} = \frac{dy}{dx}(\frac{dy}{dx})$
 $= \frac{d}{dx}(\frac{1}{E})$
 $= \frac{-1}{E^2} \cdot \frac{dt}{dx}$
 $= -\frac{1}{E^2} \cdot \frac{dt}{dx}$
 $y_2 = -\frac{1}{at^3}$.

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$$\begin{split} \overline{x} &= x - \frac{y_{1}}{y_{2}} \left(1 + y_{1}^{2} \right) \\ &= at^{2} - \frac{1/k}{-1/2at^{3}} \left(1 + \frac{1}{k^{2}} \right) \\ &= at^{2} + \frac{1}{k^{2}} \left(2at^{3} \left(1 + \frac{1}{k^{2}} \right) \right) \\ &= at^{2} + 2at^{2} \left(1 + \frac{1}{k^{2}} \right) \\ &= at^{2} + 2at^{2} + 2a \\ &= at^{2} + 2at^{2} + 2a \\ \overline{x} &= 3at^{2} + 2a \\ \overline{x} &= 3at^{2} + 2a \\ \overline{y} &= y + \frac{1}{y_{2}} \left(1 + \frac{y_{1}^{2}}{k^{2}} \right) \\ &= 2at + \frac{1}{-1/2at^{3}} \left(1 + \frac{1}{k^{2}} \right) \\ &= 2at - 2at^{3} \left(1 + \frac{1}{k^{2}} \right) \\ &= 2at - 2at^{3} - 2at \\ \overline{y} &= -2at^{3} - 2at \\ \overline{y} &= -2at^{3} - 2at \\ \end{array}$$





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Taking cube of () & Squaring (2) we get,

$$\begin{pmatrix} (z^{*})^{5} = (\overline{x} - 2a)^{3} \\ \overline{z} + a^{2} \\ \overline{z} + a^{3} \\ (z^{*})^{2} = (\overline{y} + a^{2})^{2} \\ \overline{z} + a^{2} \\ \overline{z} + a^{2}$$

