

DEDUCTION OF RADIATION LAWS FROM PLANCK'S LAW

1. Wien's Law:

1. Wien's law holds good when wavelength λ is small. (ν is large)

2. Therefore $\frac{hc}{\lambda KT} \gg 1$ and $e^{\frac{hc}{\lambda KT}} \gg 1$

3. Neglecting 1 in equation

$$E_{\lambda} d\lambda = \frac{8\pi h C}{\lambda^5 \left[e^{\left(\frac{hc}{\lambda KT}\right)} - 1 \right]} d\lambda = \frac{8\pi h C}{\lambda^5 e^{\left(\frac{hc}{\lambda KT}\right)}} d\lambda$$

Thus Planck's law reduces to Wien's law at **shorter wavelength**.

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2. Rayleigh- Jean's law:

1. Rayleigh- jean's law holds good when wavelength λ is large.(ν is small).
2. Therefore $\frac{hC}{\lambda KT} \ll 1$ and expanding we get

$$e^{\frac{hC}{\lambda KT}} = 1 + \frac{hC}{\lambda KT} + \frac{\left(\frac{hC}{\lambda KT}\right)^2}{2!} + \dots = 1 + \frac{hC}{\lambda KT}$$

$$E_{\lambda} d\lambda = \frac{8\pi hC}{\lambda^5 \left[1 + \frac{hC}{\lambda KT} - 1\right]} d\lambda = \frac{8\pi hC}{\lambda^5 \frac{hC}{\lambda KT}} d\lambda$$

$$E_{\lambda} = \frac{8\pi KT}{\lambda^4}$$

Thus Planck's law reduces to Rayleigh- jean's law at **longer wavelength**.

ADVANTAGES OF PLANCK'S THEORY

1. It explains the energy spectrum of the **black body radiation**.
2. It is used to deduce **Wien's displacement law** and **Rayleigh-Jean's law**.
3. It introduces a new concept, *i.e.*, *energy is **absorbed** or **emitted** in a **discrete manner*** in terms of quanta of magnitude of $h\nu$ *i.e.*,

$$E = nh\nu$$