

SNS COLLEGE OF TECHNOLOGY

(An Autonomous Institution)



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DEPARTMENT OF MATHEMATICS UNIT-IV FOURIER TRANSFORM

CONVOLUTION THEOREM : If FB(M)] & FEg(M)] are The Jourier teamsform } f(m) & g(m) respectively then The Fourier transform of the convolution of zins & gins & the product of their fourier teansforms. as FFBCND*g(n)7 = FCSD. G(S) = F[R(m)] F[g(m)] = to some isn an a Light feynseisndn. CONVOLUTION of ANY TWO FUNCTIONS: fins and yours in forme teamforms is denoted by (4*9) (m) = f(m) * g(m) and is defined by, (+*9) (m)= B(m)* g(m) = 1/071 J & & (E). g (m-E) of . $F_{c}(s) = F_{c}\left[f(n)\right] = \sqrt{\frac{2}{n}} \int_{0}^{\infty} \sigma^{n} \cos sn dn = \sqrt{\frac{2}{n}} \left[\frac{a}{a^{2}+s^{2}}\right]^{-1}$ Fic(s) = Ge [gen)] = V= Sebn as sindn = V= [b2152]

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1) Evaluate
$$\int_{0}^{\infty} \frac{dn}{(n^{2}+a^{2})(n^{2}+b)}$$
 using transforms for)
Find the Howine transform $g(n) = e^{-\alpha n} g(n) = e^{-bn}$
 $g(n) = e^{-bn}$
 $g(n) = e^{-an} g(n) = e^{-bn}$
 $g(n) = g(e^{-bn}) = \sqrt{\frac{2}{\pi}} \int_{0}^{\infty} e^{-bn}$
 $g(n) = \sqrt{\frac{2}{\pi}} \int_{0}^{\frac{1}{2}} \frac{dn}{(a^{2}+b^{2})}$
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 $g(n) = g(e^{-g(n)}) = \sqrt{\frac{2}{\pi}} \int_{0}^{\infty} e^{-bn}$
 $g(n) = \sqrt{\frac{2}{\pi}} \int_{0}^{\frac{1}{2}} \frac{d}{(a^{2}+b^{2})}$
 $g(n) = g(n) = \int_{0}^{\infty} \frac{d}{(n^{2}+b^{2})} \int_{0}^{\frac{1}{2}} \frac{d}{(a^{2}+b^{2})}$
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 $g(n) = g(n) = \int_{0}^{\infty} \frac{d}{(n^{2}+b^{2})} \int_{0}^{\frac{1}{2}} \frac{d}{(a^{2}+b^{2})} \int_{0}^{\frac{1}{2}} \frac{$



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 $\int_{0}^{\infty} e^{-(a+b)n} dn = \frac{2}{\pi} \int_{0}^{\infty} \frac{ab}{(a^{2}+s^{2})(b^{2}+s^{2})} ds$ $\frac{e^{-(a+b)n}}{-(a+b)} \int = \frac{aab}{\pi} \int \frac{a}{(a^2+s^2)(b^2+s^2)}$ $\frac{e^{-\omega}-e^{\circ}}{-(a+b)} = \frac{2ab}{\pi} \int \frac{\partial}{(a^2+s^2)(b^2+s^2)}$ $\frac{1}{a+b} \cdot \frac{\pi}{2ab} = \int \frac{\partial}{(a+b)^2} \frac{ds}{(b+b)^2}$ put s=n. $\frac{\pi}{n} = \int \frac{\partial}{\partial x^2} dx \frac{\partial}{\partial x^2} dx^2$ 2) Evaluate $\int_{0}^{\infty} \frac{n^2}{(n^2 + a^2)(n^2 + b^2)} dn$ using transforms. <u>John</u> WKT $f_s(s) = F_s[f(n)] = \sqrt{g} \int_{1}^{\infty} e^{-an} e^{n} sn dn = \sqrt{\frac{g}{11}} \left[\frac{s}{a^2 + s^2}\right]$ $G_{3}(s) = F_{s}[g(n)] = \sqrt{2} \int_{\pi}^{\infty} \int_{\pi}^{\infty} e^{-bn} sn dn = \sqrt{2} \int_{\pi}^{\infty} \int_{h=2}^{\infty} e^{-bn} sn dn = \sqrt{2} \int_{\pi}^{\infty} e^{-bn} sn dn = \sqrt{2} \int$ paeseval's Edentity: Heref (m) = e-an, g(n)=o-bn = frs(s) G(s)ds



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